



Systèmes de Référence Temps-Espace



# Peignes de fréquences optiques pour génération micro-onde à très bas bruit de phase

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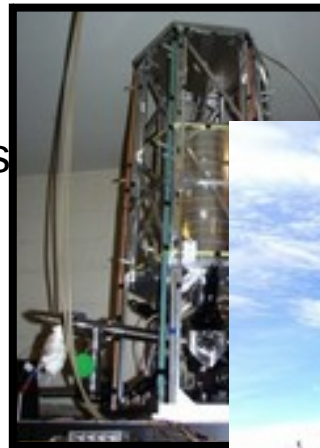
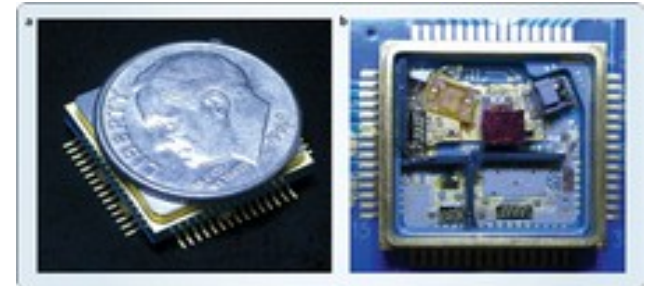
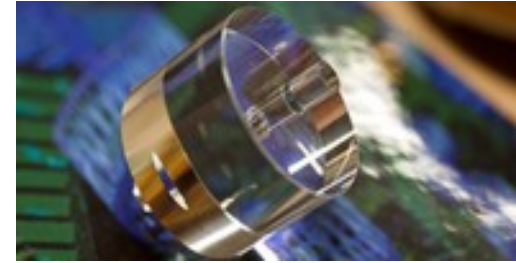
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# Low-noise $\mu$ wave : motivation

## Existing very low $\phi$ -noise $\mu$ -wave sources ( $\sim 10$ GHz):

- **Room temp Sapphire osc.**  
(Raytheon, formerly Poseidon Australia):  
-40dBc/Hz @ 1Hz, -170dBc/Hz @ 100kHz from carrier
- **Cryogenic Sapphire oscillator**  
(UWA, FEMTO-ST, ULISS):  
-100dBc/Hz @ 1Hz, -140dBc/Hz @ 100kHz from carrier
- **Opto Electronic Oscillator**  
(JPL/OEwaves):  
-40dBc/Hz @ 1Hz, -160dBc/Hz @ 10kHz  
(large resonances after that)



## Applications:

- atomic frequency standards
- radar
- VLBI
- synchronization of particle accelerators
- time reference distribution
- telecommunication
- ...

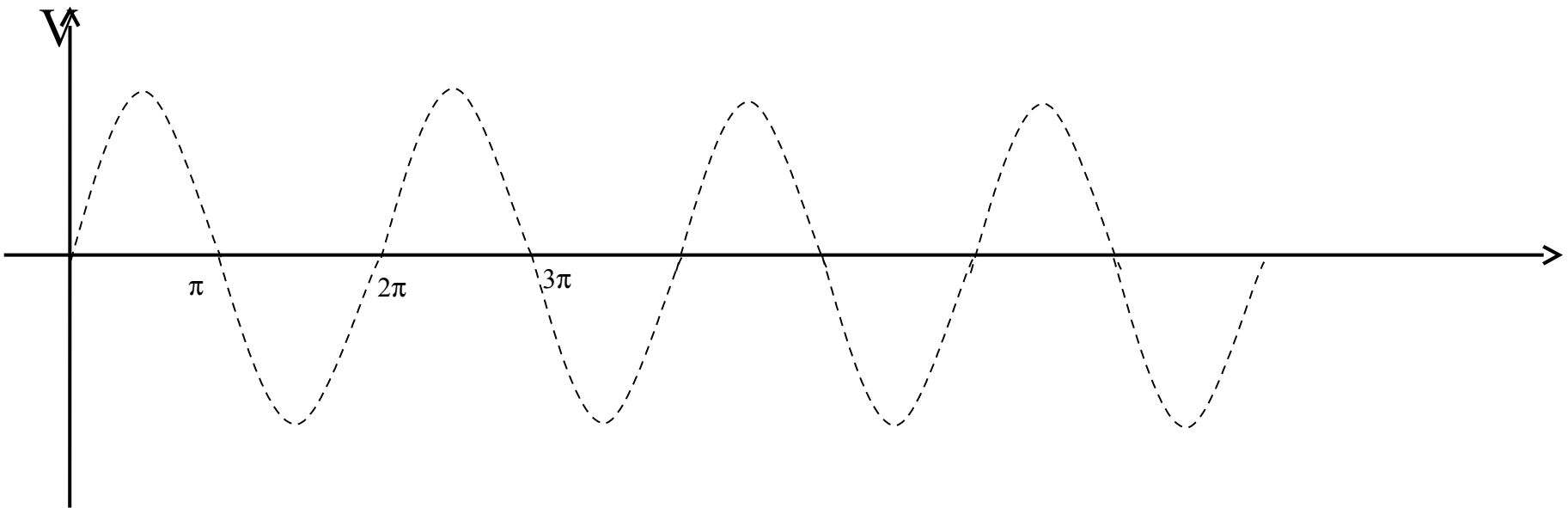
# Frequency division, effect on phase noise

$f_c$  [Hz]  $\rightarrow$   $f_c/N$  [Hz] then  $\Delta\phi \rightarrow \Delta\phi/N$  [rad]

$$S_{\phi}(f) \text{ [dBc/Hz]} \rightarrow S_{\phi}(f) - 20 \cdot \log_{10}(N) \text{ [dBc/Hz]}$$

Large noise reduction if N is large...

Exemple : divide by 2



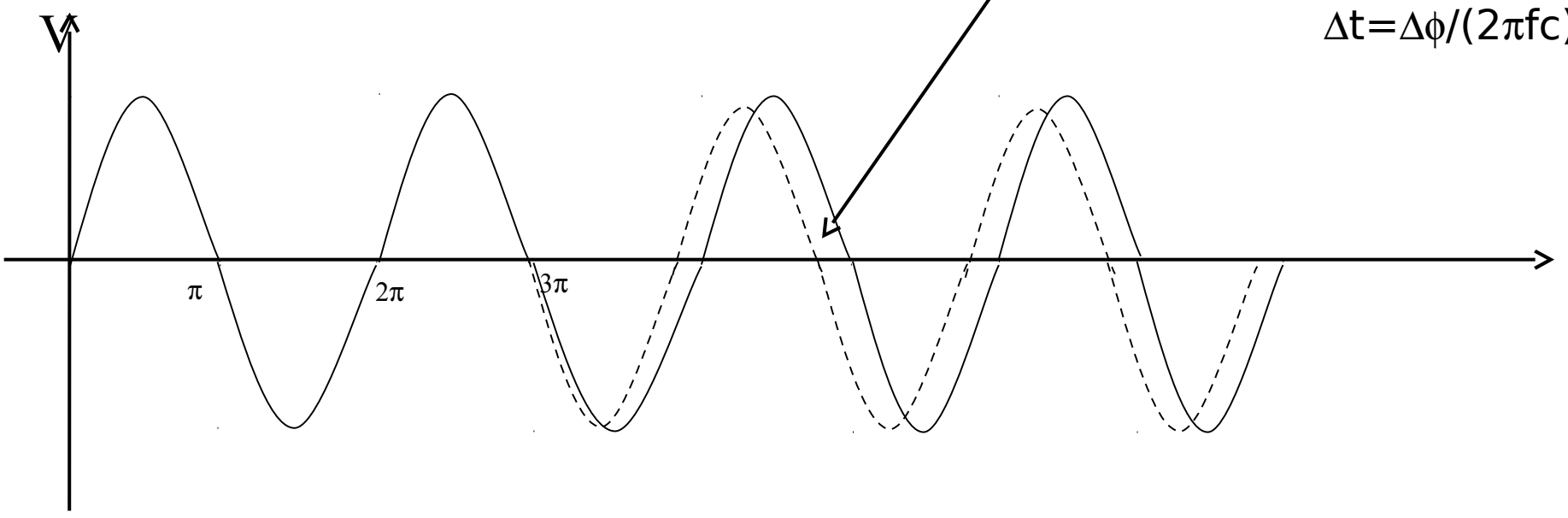
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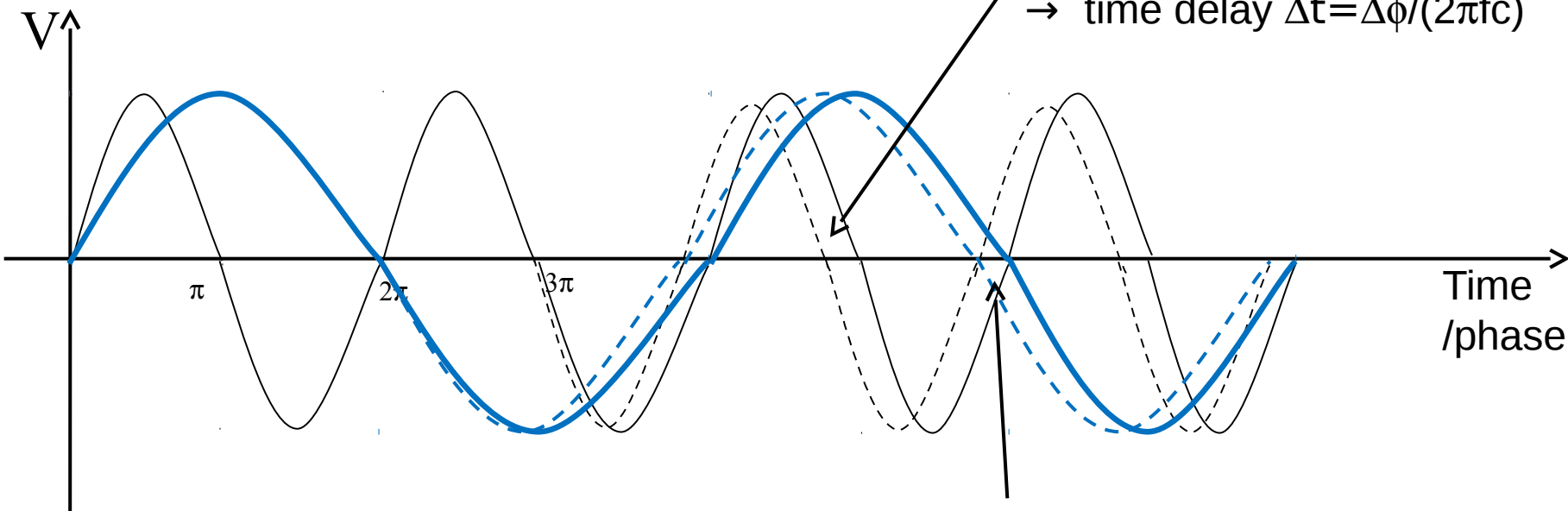
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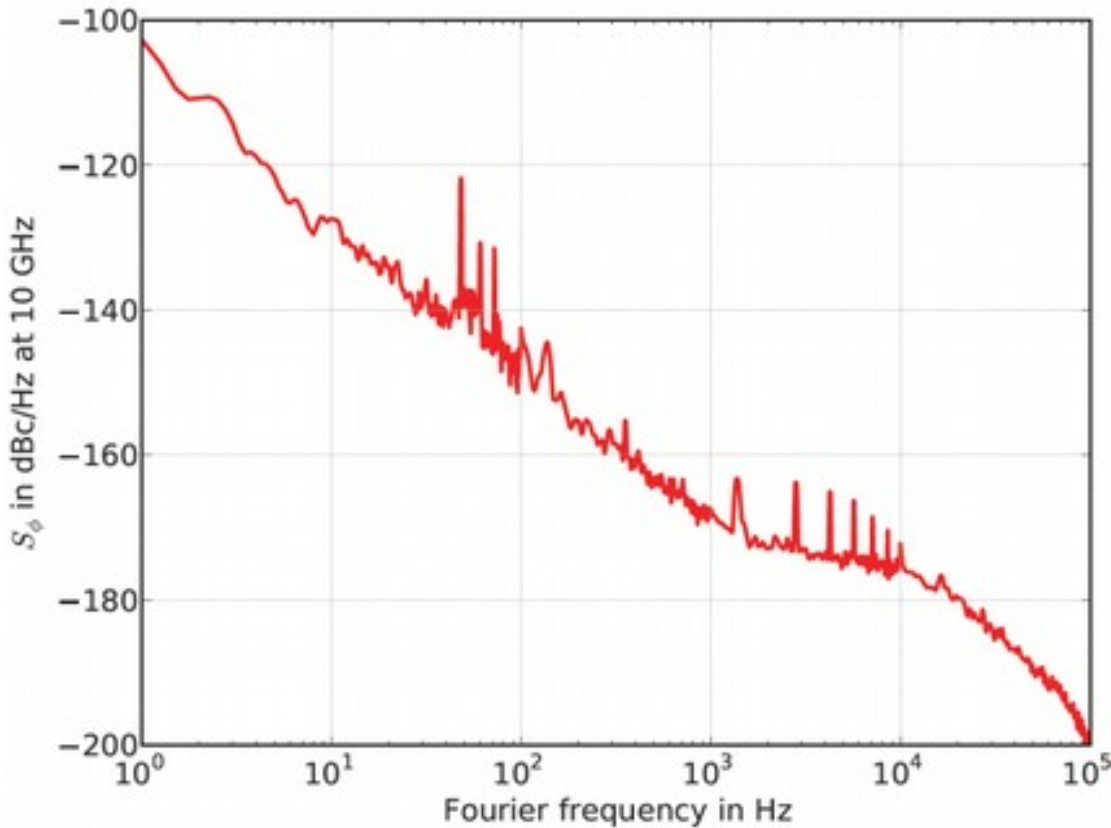
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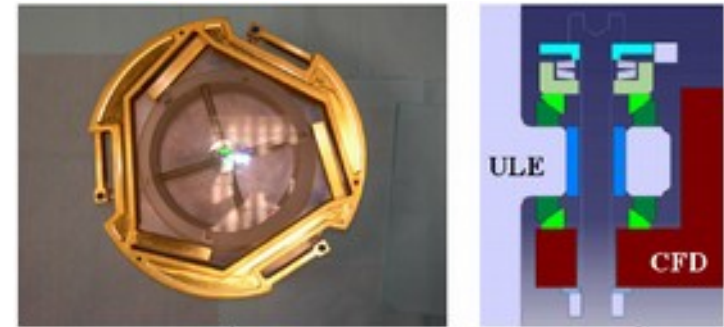
time delay  $\Delta t = \Delta \phi / (2\pi f_c)$  on  $f_c/2$   
 $\rightarrow$  dephasing  $\Delta \phi' = \Delta \phi / 2$  on  $f_c/2$

# USL transferred to $\mu$ -wave (projection)



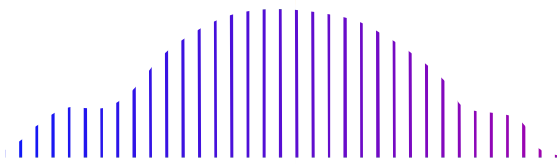
A robust  $4.5 \times 10^{-16}$  (@1s) level USL cavity (designed following space industry standards and methods)  
 $\rightarrow$  10cm long cavity with rings

Prototype designed for transport  $\pm 10g$  and operation at zero-2g  
 Currently existing lab prototype



$\Phi$ -noise of a 10 GHz carrier obtained by frequency division of the space-prototype USL at 200THz (SODERN/CNES/SYRTE), by a frequency comb, assuming perfect division

**200 THz ( $\lambda=1.5\mu\text{m}$ )**



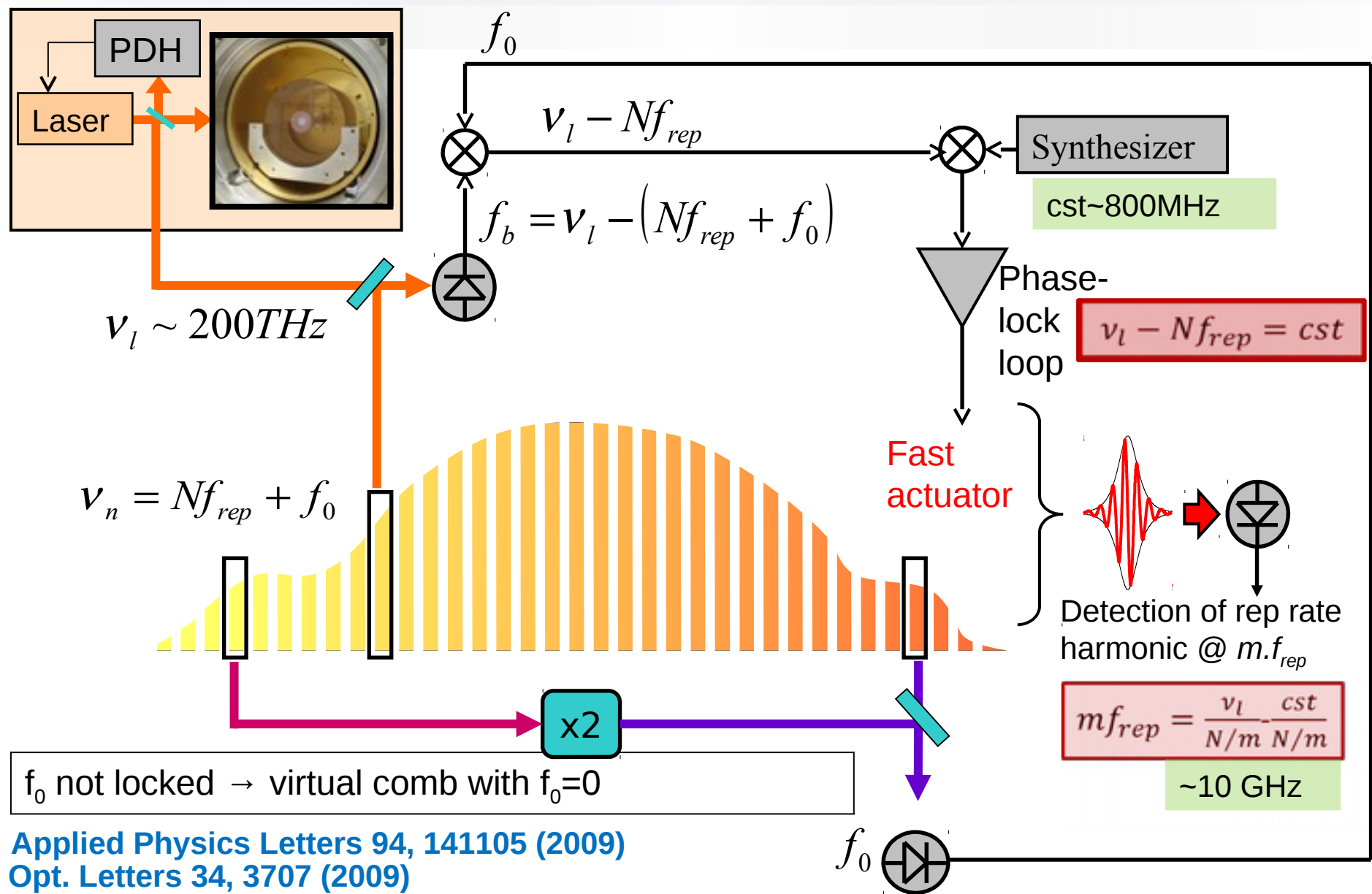
Opt. Freq. comb

$\Phi$ -noise

$$\rightarrow -20 \cdot \log(20000) = -86\text{dB} (!!!)$$

**10 GHz**

# Low noise $\mu$ -wave generation with comb (optical frequency divider scheme)



Applied Physics Letters 94, 141105 (2009)  
 Opt. Letters 34, 3707 (2009)



# Er-fibre comb with intra-cavity EOM

## WHY ?

large feed-back BW difficult for Er fs lasers

- pump diode current : rather low response,  $\sim 100\text{kHz}$  max BP (with good phase-advance electronics...)
- PZT : resonances  $\sim 40\text{kHz}$  BW

Free-running high Fourier frequency phase noise is hard to kill with phase-locking

## HOW ? (in coll. with MenloSystems)

-Add a fast actuator (EOM) in the fs laser cavity

-Used as a voltage-controlled group delay actuator

(index  $\langle n \rangle$  controlled by  $V$  ; linear polarization)

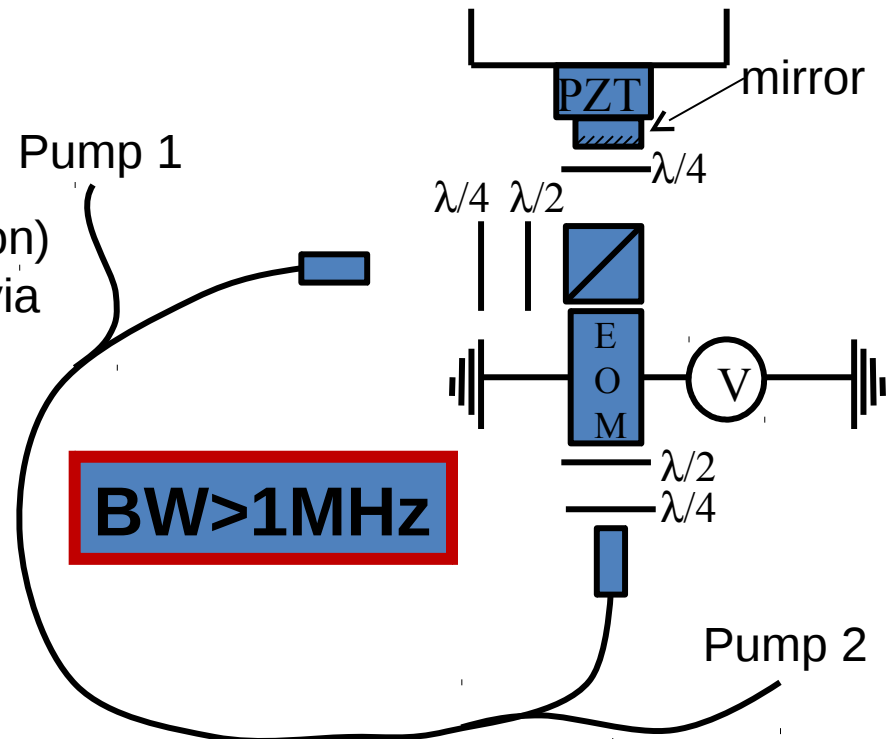
- Good alignment to decrease cross-talks (via polarization and amplitude)

IEEE UFFC 59, 432 (2012)

also Newbury et al. Opt.Lett. 34, 638 (NIST)

also Hong et al. Opt. Exp. 18, 1667 (NMIJ)

(Note : no output coupler represented here)





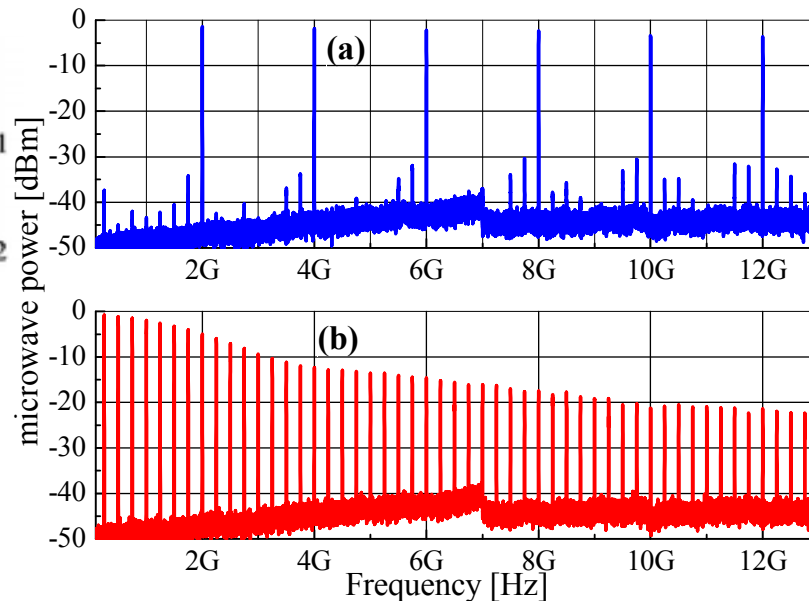
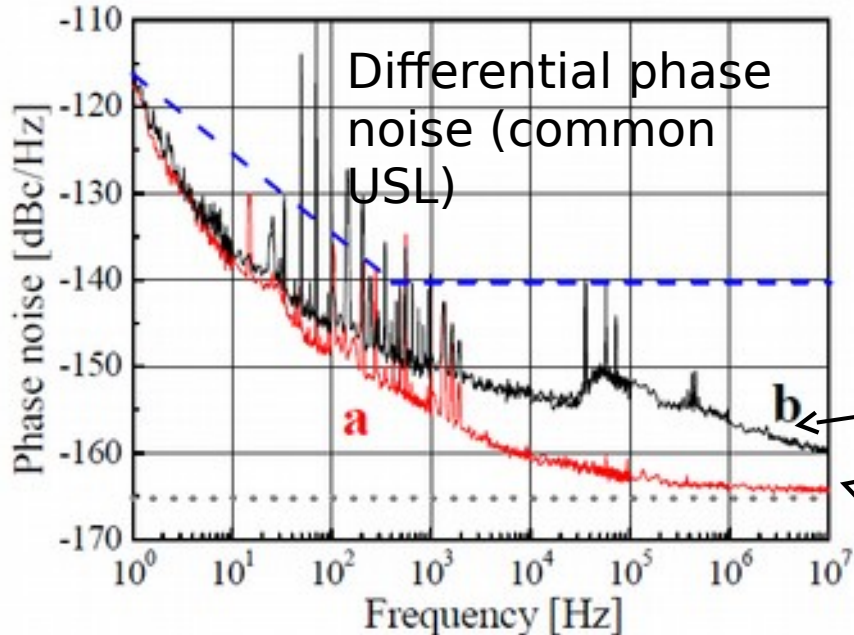
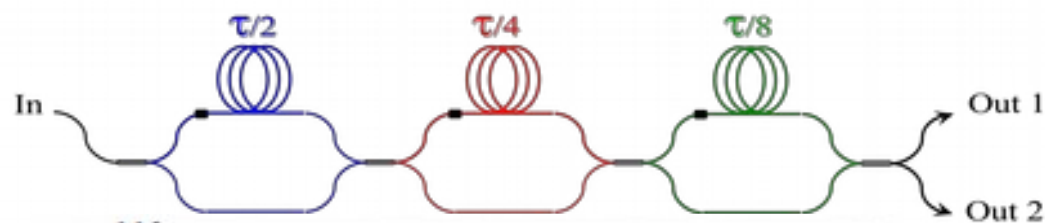
# Increase SNR for lower white phase noise floor

## Thermal noise (Johnson-Nyquist) :

A 0 dBm  $\mu$ -wave signal cannot have a white phase noise limit better than -177dBc/Hz

Solution : increase  $\mu$ -wave power

- higher optical power+more linear PD  
**(in coll. with Discovery semiconductor)**
- high rep rate fs laser / external rep rate multiplication  
→ less power in undesired harmonics,  
more in the harmonic of interest



2 combs 2 MZM 2 PD  
(excess phase noise to investigate)

1 combs 2 MZM 2 PD

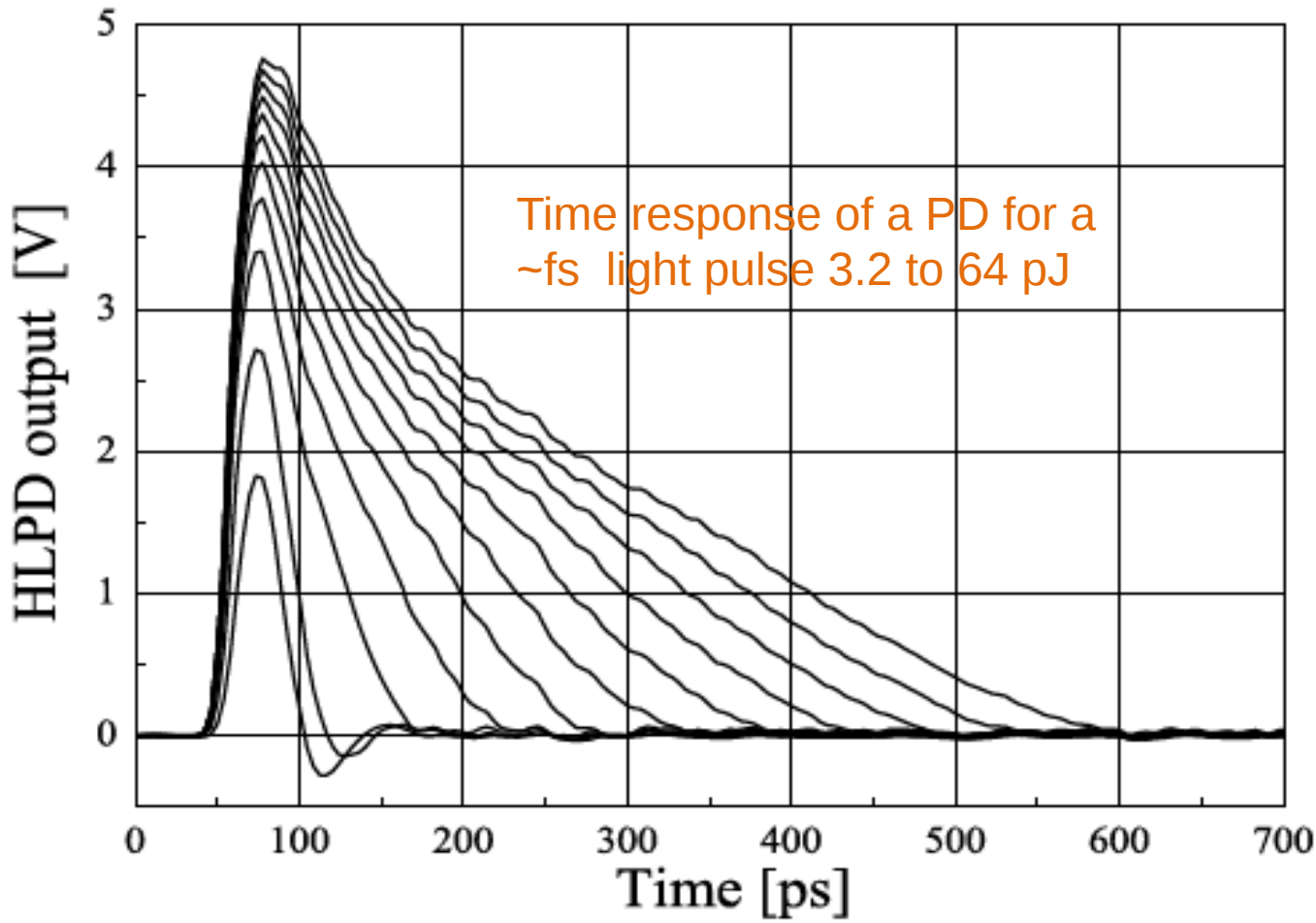
# AMPM conv. in $f_{\text{rep}}$ and harmonics photodetection

amplitude fluctuations of the fs laser induce fluctuations of phase of  $f_{\text{rep}}$   
(and its harmonics)

→ possible to lock amplitude (but only at low Fourier frequencies)  
 $1.2 \times 10^{-16}$  @ 1s generated  $\mu\text{wave}$  / 100as synchro

→ or analyze carefully the physics...

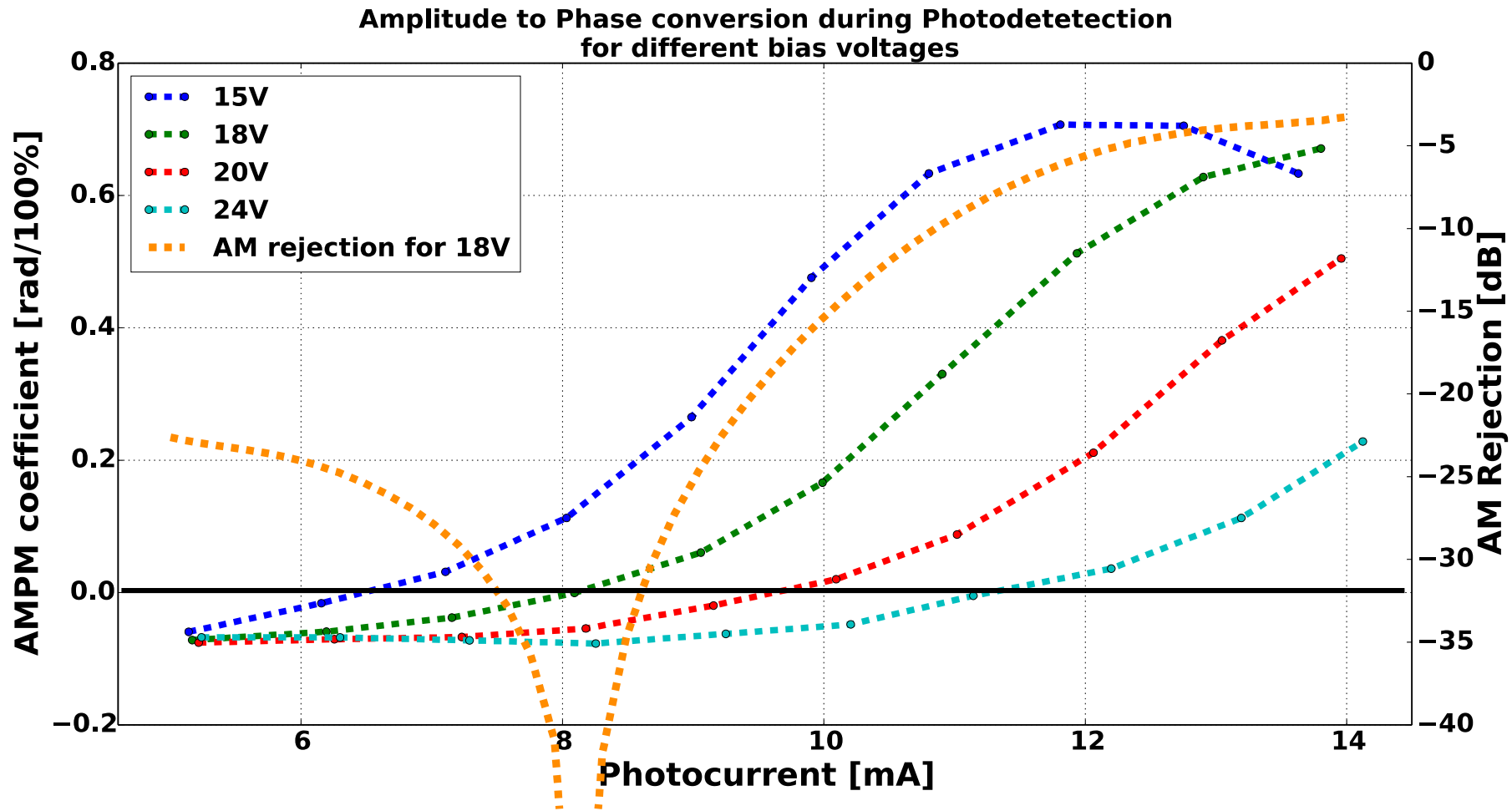
**App. Phys. Lett. 96, 211105 (2010)**



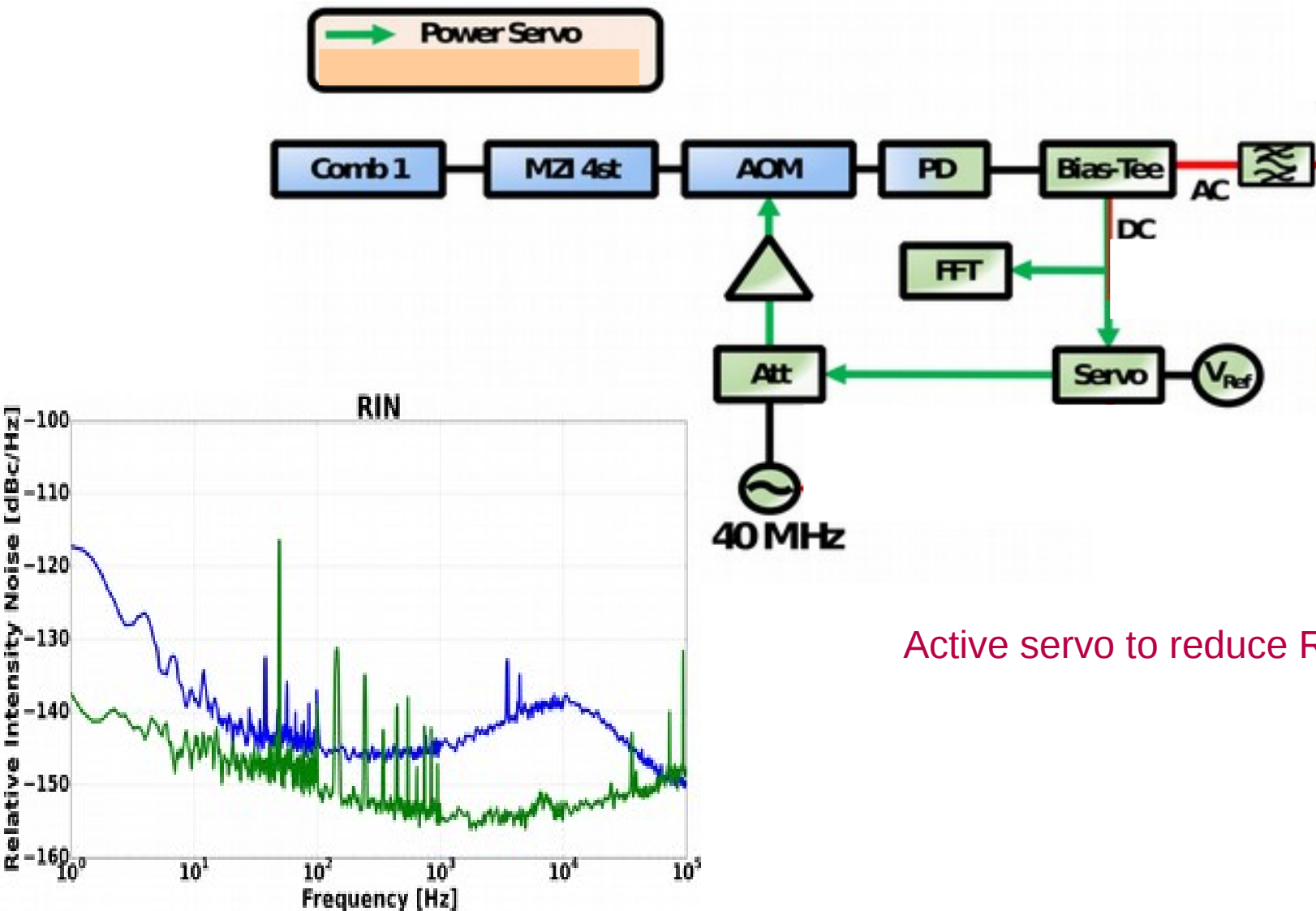
By **space-charge screening effect**, close to saturation, the PD response is **asymmetric**  
→ AM noise produces PM noise

For harmonic order  $> 1$  there are special situations...

# Suppression of AMPM conversion

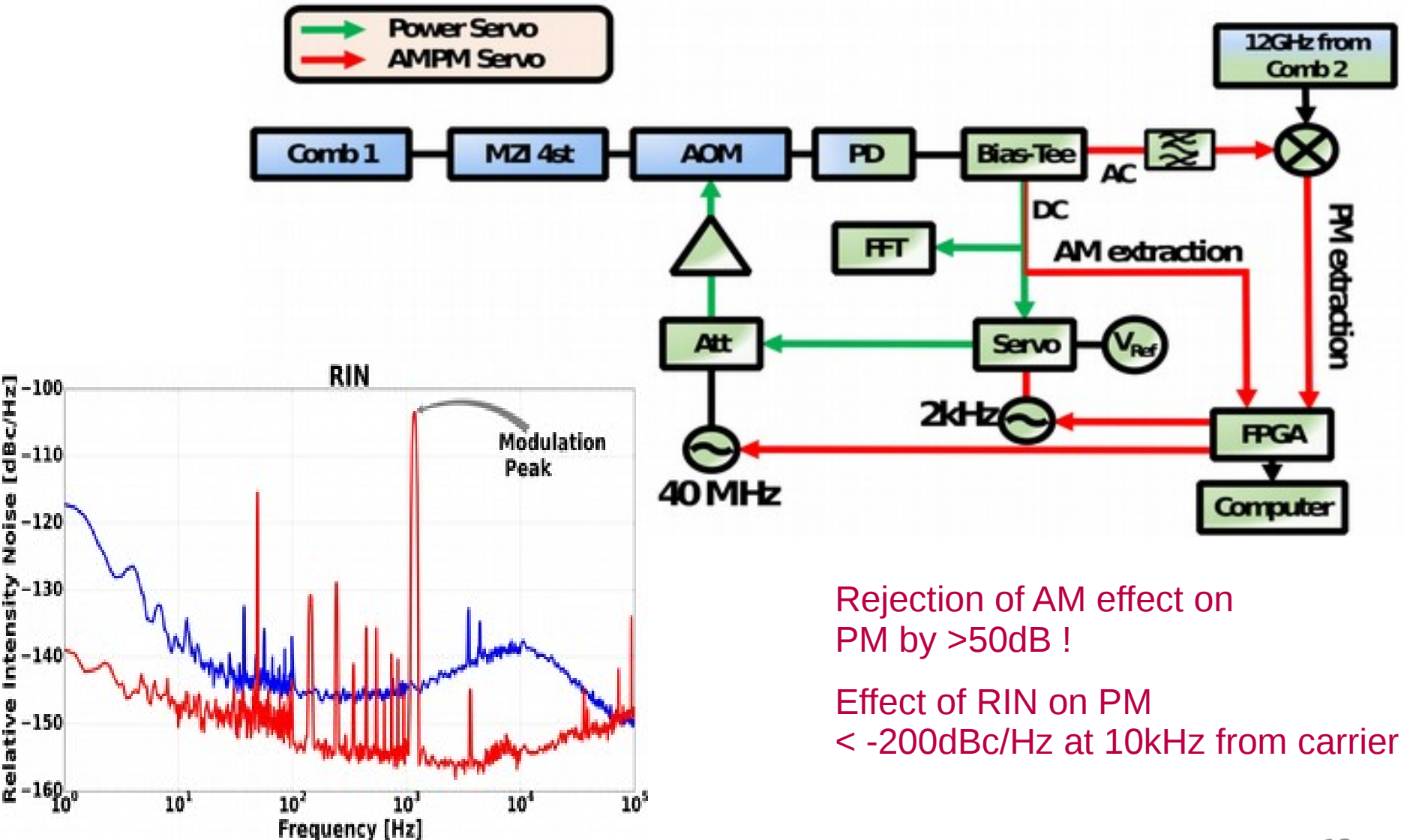


# Suppression of RIN



Active servo to reduce RIN

# Suppression of RIN

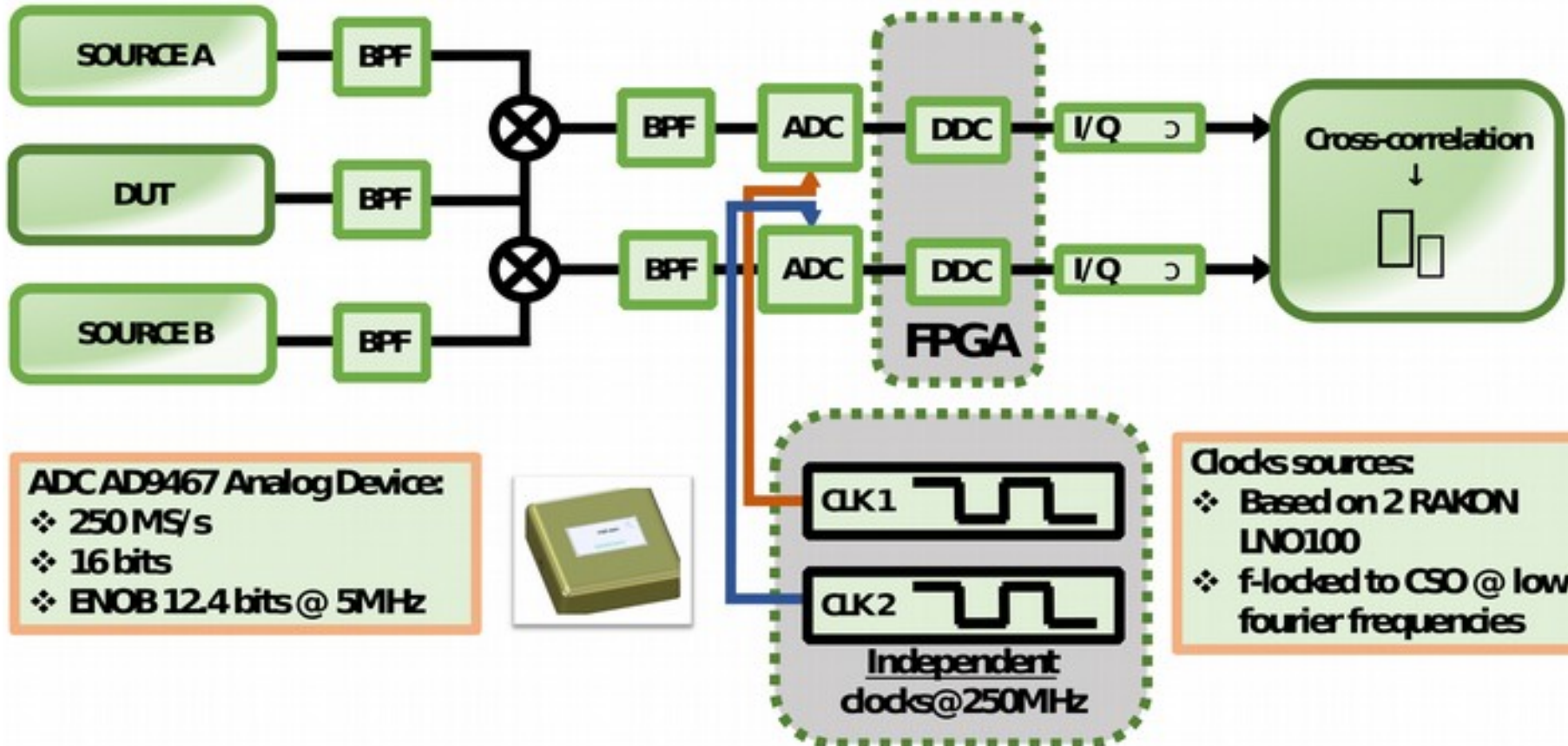




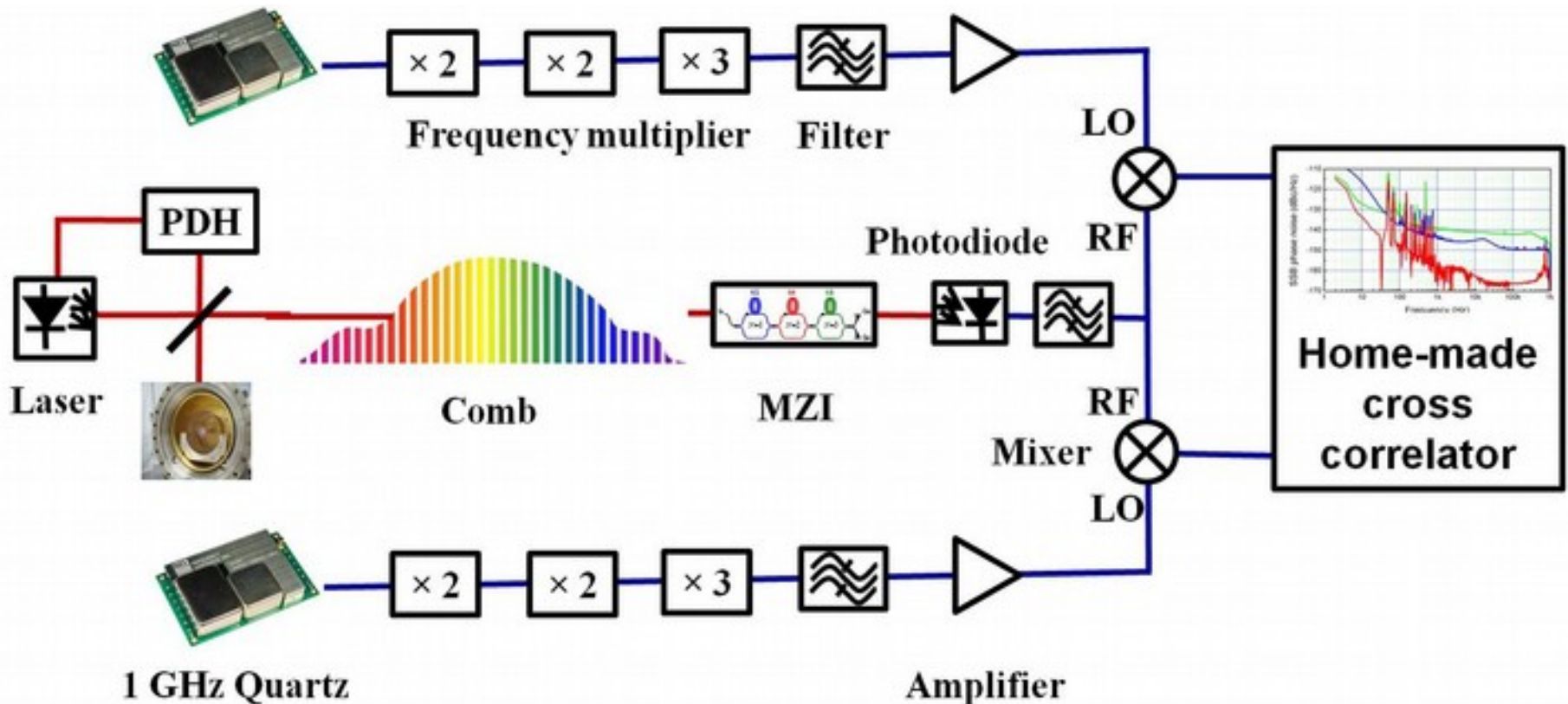
# $\Phi$ -noise Measurement method

At very low phase noise, cross-correlation is the technique of choice BUT tricky  
Most commercial systems are homodyne → relatively high sensitivity to AM  
→ We developed our own heterodyne system

## Heterodyne Cross-correlation for *absolute* phase noise measurement



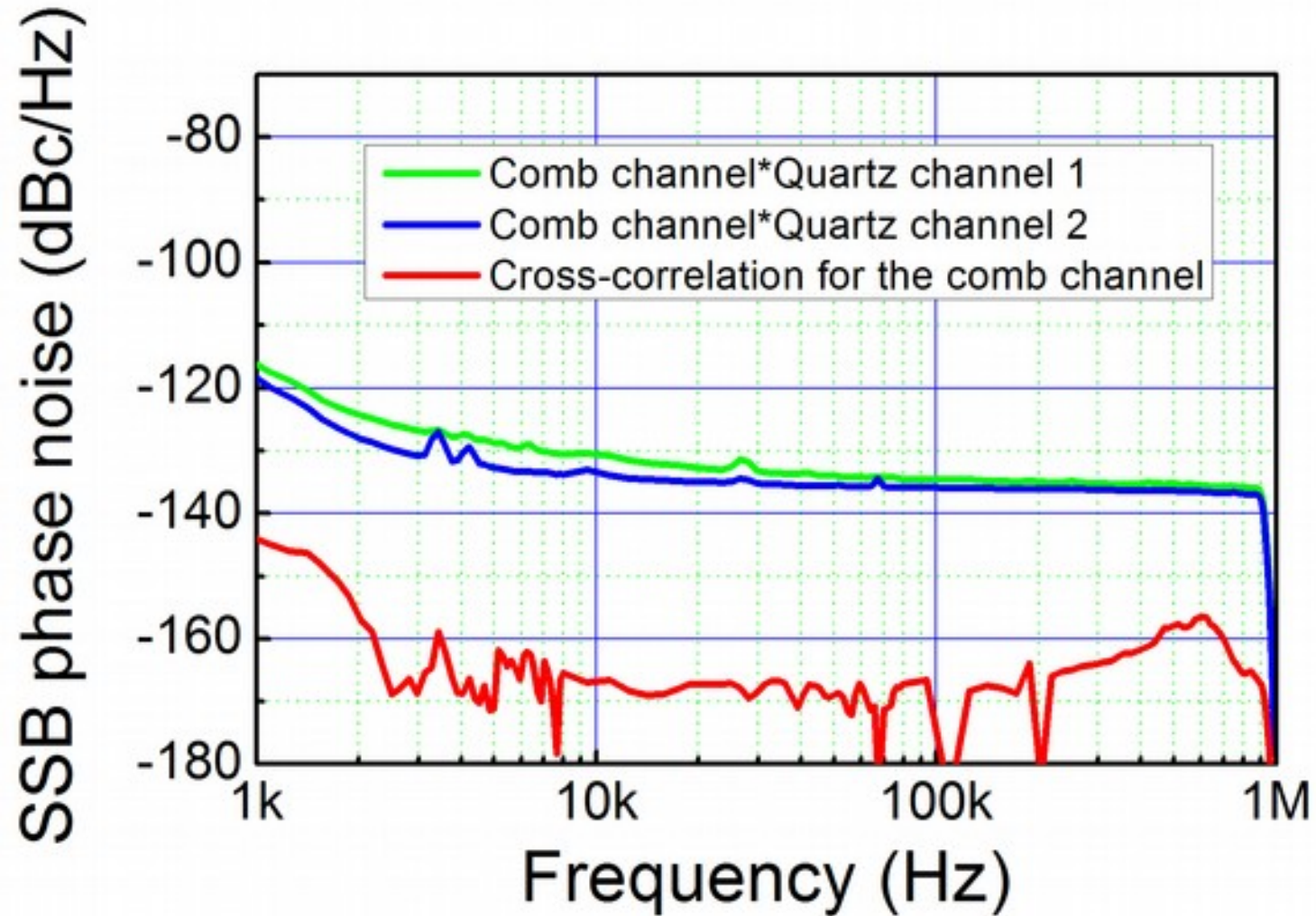
# $\Phi$ -noise Measurement method (development setup)



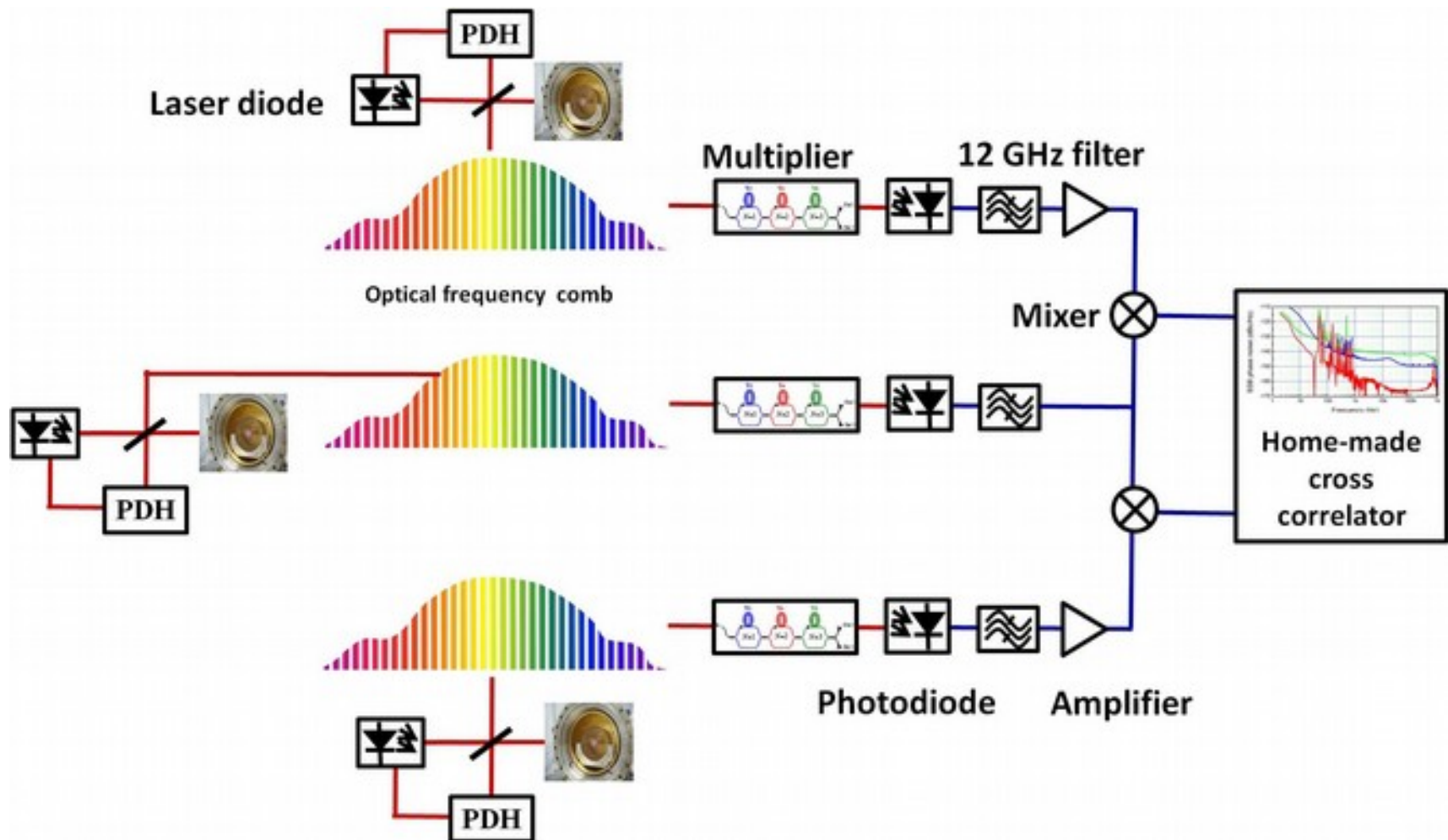
- Auxiliary sources are ~ good enough at high Fourier frequency and trivial to operate
- Cross-correlating away their noise takes time, and ways too much time for low Fourier frequencies  $\rightarrow$  not useful for characterizing noise frequencies  $< 1\text{kHz}$



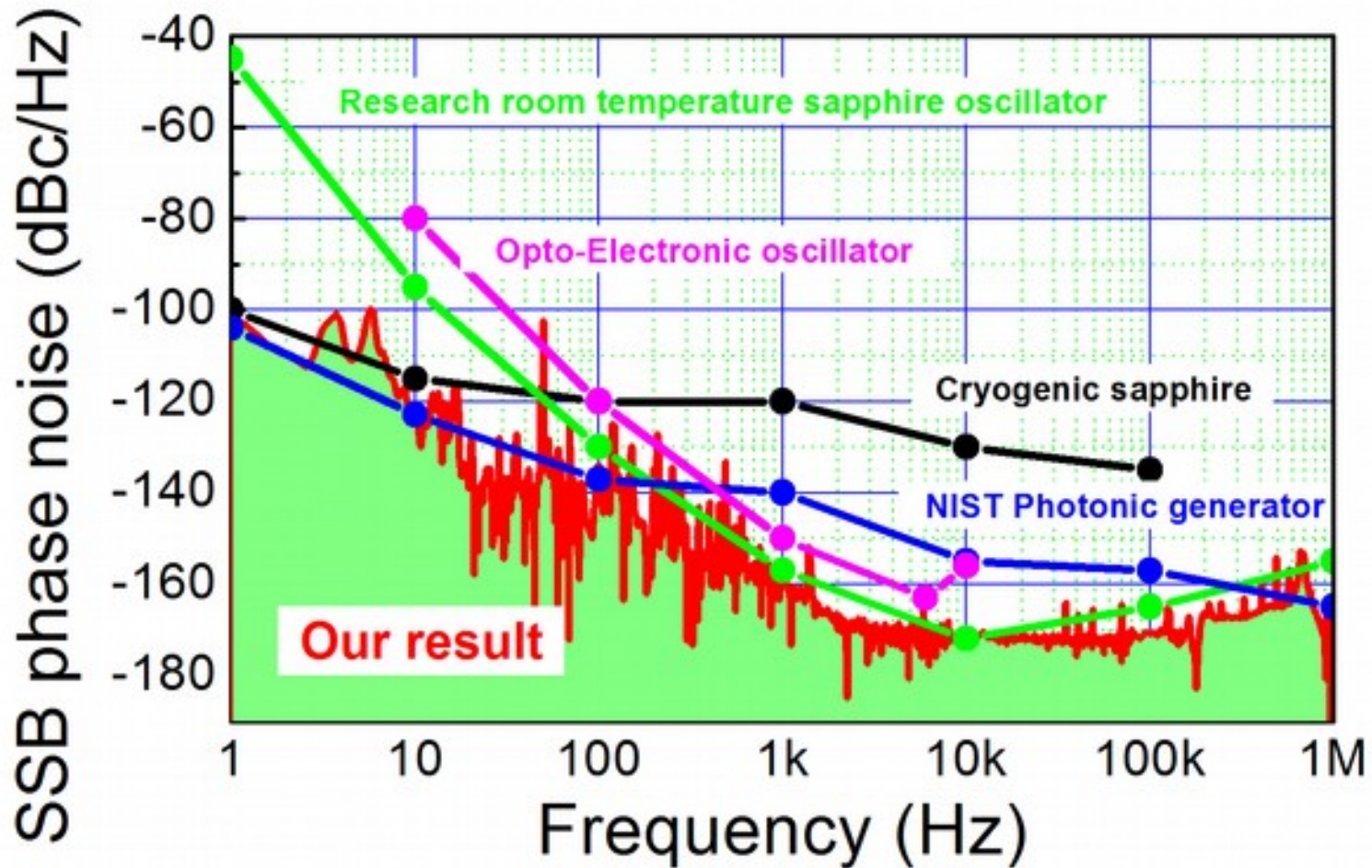
# $\Phi$ -noise Measurement method (development setup)



# $\Phi$ -noise Measurement method (Full setup)



# $\Phi$ -noise Measurement method (Full setup result)



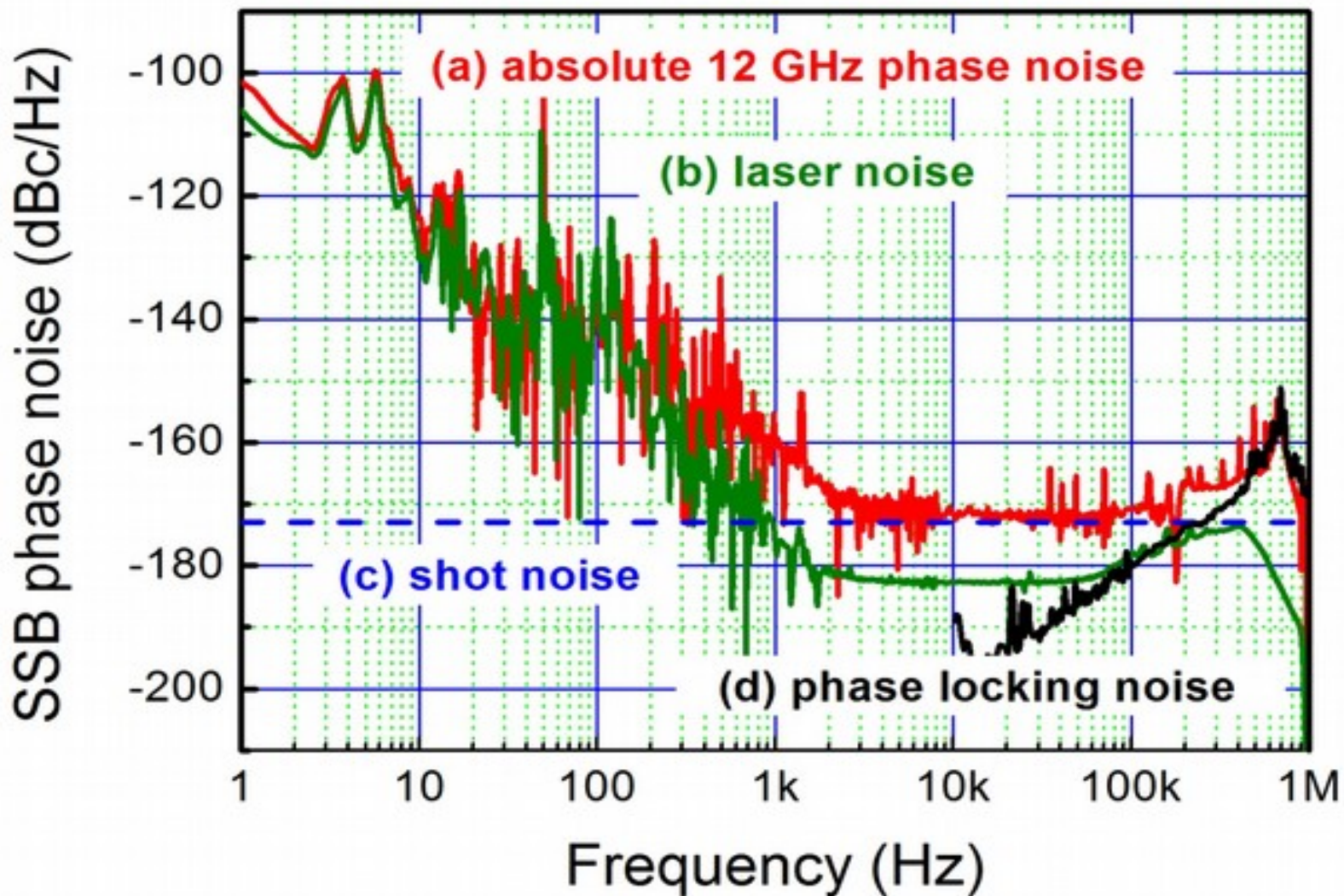
**-104 dBc/Hz @ 1Hz**

**-172 dBc/Hz @ 10kHz and beyond**

From a 12 GHz carrier

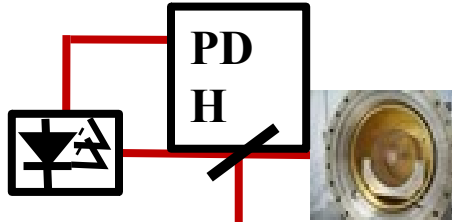


# $\Phi$ -noise result analysis



# Conclusion

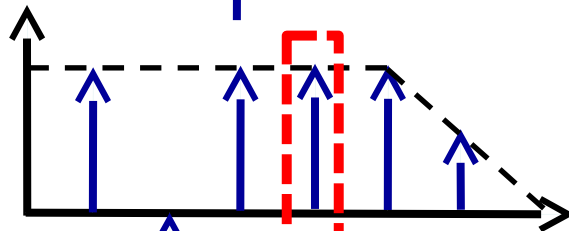
CW laser



Comb



HLPD



Electrical spectrum

Record ultra-low phase noise 12 GHz  
signal generation

**-104 dBc/Hz at 1 Hz**  
**-172 dBc/Hz at 10 kHz**

Phase noise characterization by a  
heterodyne FPGA-based cross-correlation  
scheme

**Noise floor below:**  
**-180 dBc/Hz**

A comb is 3U 19" rack-size (and plane/ space qualified...), USL is larger (size of a H-maser, typically) and "only"  $\sim 10^{-15}$  (ie  $\sim -100$ dBc/Hz)

→ we are seeking **better and/or more compact cw lasers** for referencing the comb

→ we are seeking **in-field applications** ...