

ANALYSE MULTI-TABLEAUX.  
FEATURING:  
PLAIN MULTI-TABLES PCA  
SUM-PCA, MULTIPLE FACTOR ANALYSIS, STATIS, ETC.

---

Hervé Abdi

The University of Texas at Dallas



# La Famille Multi-Tableaux

Biblio. Allez voir à [www.utdallas.edu/~herve](http://www.utdallas.edu/~herve)

A87: STATIS & DISTATIS

A71, A59: DISTATIS

C71: Rv Coefficient

C40: Multiple Factor Analysis

C33: STATIS

---

**CNAM: 7 NOVEMBRE 2011**

- Principal Component Analysis + Frills

---

**MAIN THEME: WHAT ARE MULTI-TABLE ANALYSIS?**

## Main ideas:

- Good pictures help.
- Project parts of a data table

Variation 1: Tables and sub-tables

Variation 2: Preprocessing tables (Z-scores)

Variation 3: sum-PCA, MFA

Variation 4: Optimal weights for tables: STATIS

Variation 5: Extensions of STATIS

---

**MUTI-TABLE ANALYSIS: TO STATIS AND BEYOND!**

- “I am reading in the brain ...”

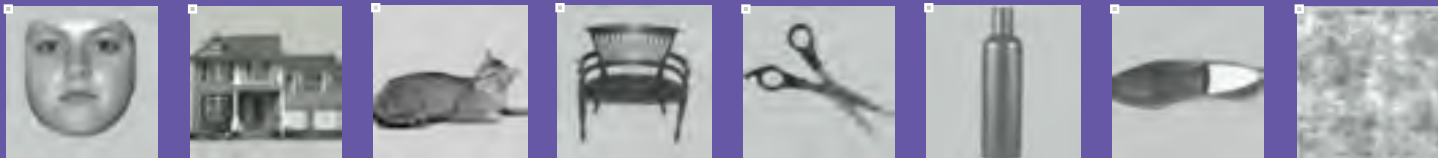
---

**START WITH AN EXAMPLE OF MULTI-TABLE ANALYSIS**

# OBJECT AND FACE PERCEPTION IN VT CORTEX

Haxby et al. (2001) *Science* 293, 2425-2429

- 8 categories of objects
  - faces, houses, cats, chairs, scissors, bottles, shoes, scrambled faces



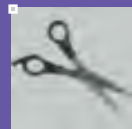
A scan =  $64 \times 64 \times 40 = 163,840$  voxels

Keep only the “sensitive voxels”  $\approx 500$  per subject  
(not critical for this story)

---

**AN EXAMPLE: LOOKING IN THE BRAIN**

- From Haxby *et al.* (2001)
  - small participant sample ( $N = 6$ )
  - simple 1-back memory task
  - 8 visual categories:



- 7 scans for each category per block; 8 blocks in 12 superblocks (672 scans total)
- Magnet parameters: gradient EPI on GE 3T scanner, TR = 2500ms, 40 3.5 mm sagittal images, FOV 24 cm, TE = 30 ms, flip angle 90°

---

**SOURCE DATA**

- A map with the categories

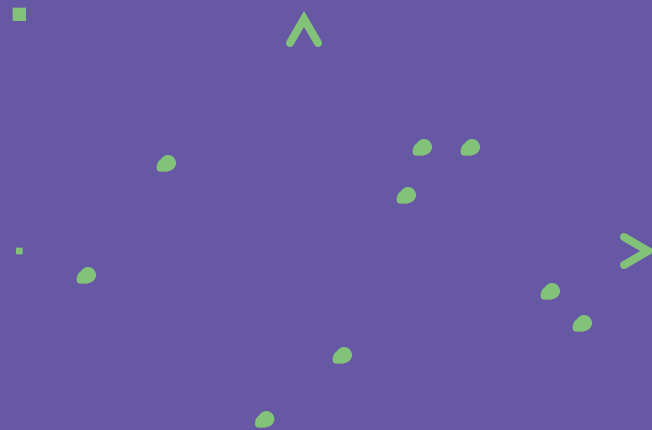
---

WHAT DO WE WANT?

General idea:  
things are points in a  
(Euclidean!) space

**DIMENSIONS**

**Euclidean Model**



---

**1,2,3 PCA**

---

WHY PCA?

# THE EUCLIDEAN WORLD IS BEAUTIFUL IT WORKS WITH THE PYTHAGOREAN THEOREM!

- Mean, variance, inertia are *natural* (cosines and contributions).
- We love to minimize sum of squares  
(and the eigen-world is *magic*).
- Good routines means very large data sets.
- Easy Duality (What does that mean ????)
- Generalizes beautifully (masses, weights, ...)
- And if it is multivariate normal we are *in Paradise!*

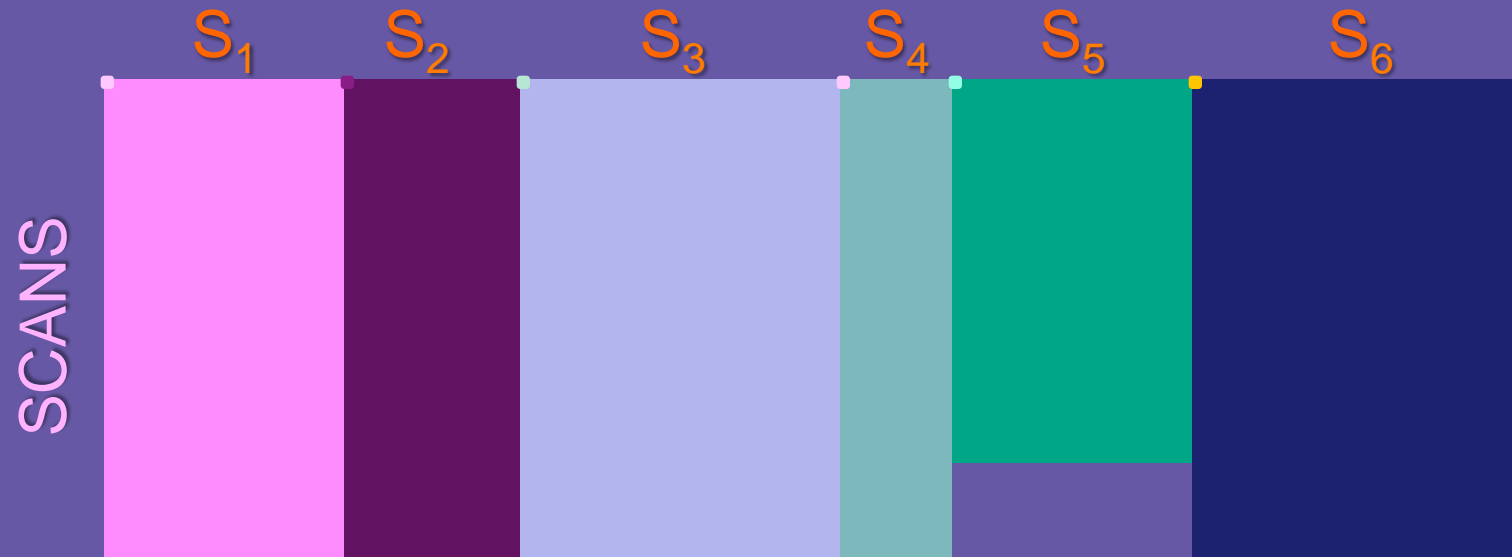
---

PCA: WHY EUCLIDEAN?

---

BACK TO THE DATA: *WHAT* IS THE STRUCTURE

- DATA MATRIX



---

6 PARTICIPANTS

WITH DIFFERENT # OF VARIABLES (VOXELS)

[577, 464, 307, 675, 422, 348]

- One participant = One block / subtable

One row = One scan

One column = one voxel of a participant

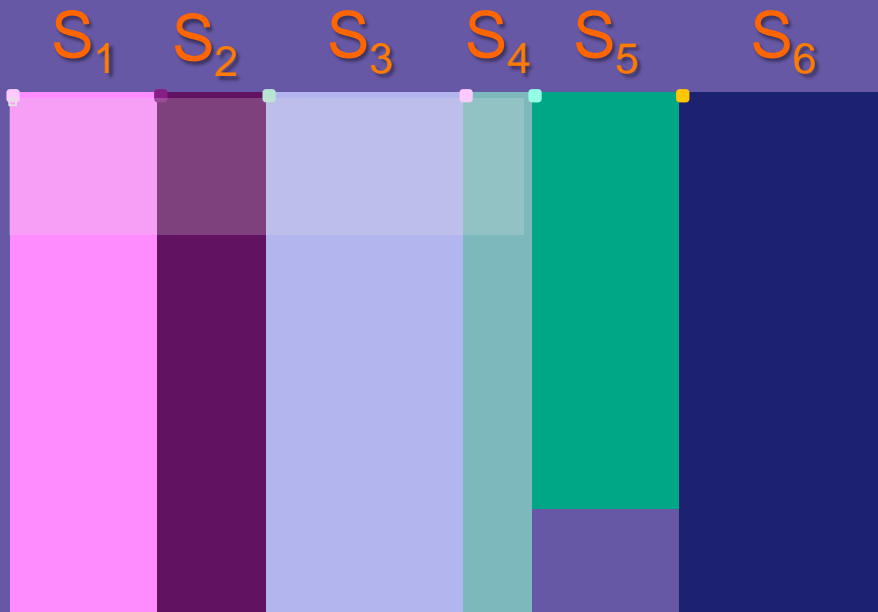
We want to look at everybody together  
but also at each subject alone

---

**STRUCTURES**

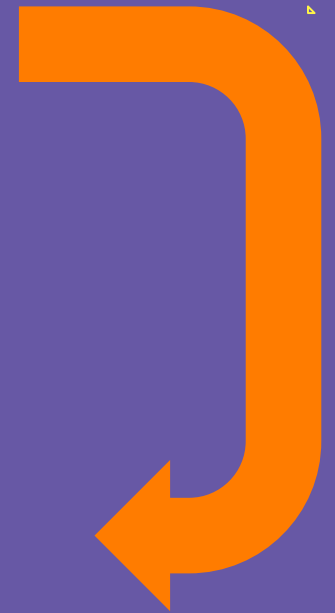
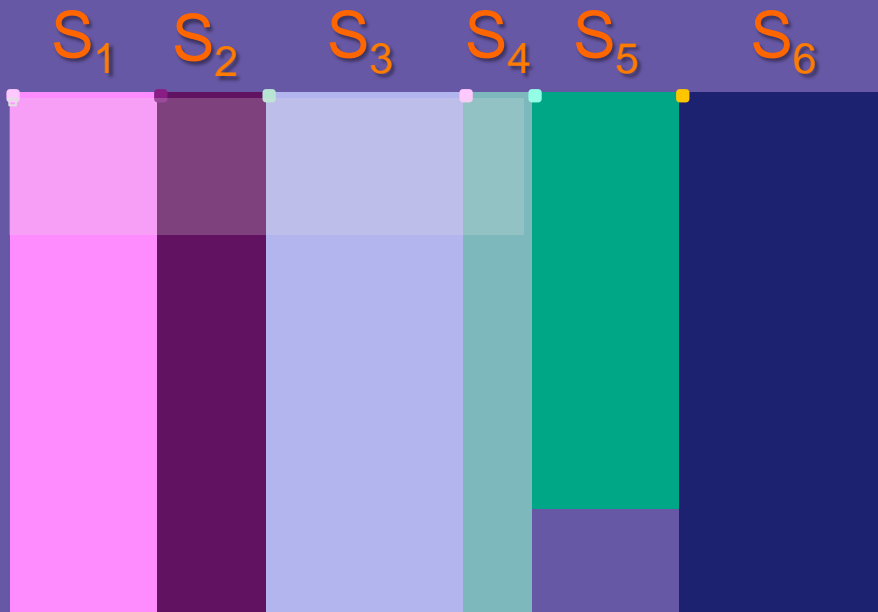
---

HOW TO ANALYZE THESE DATA



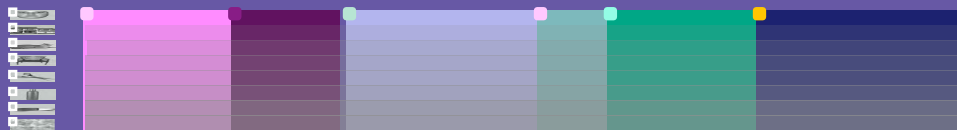
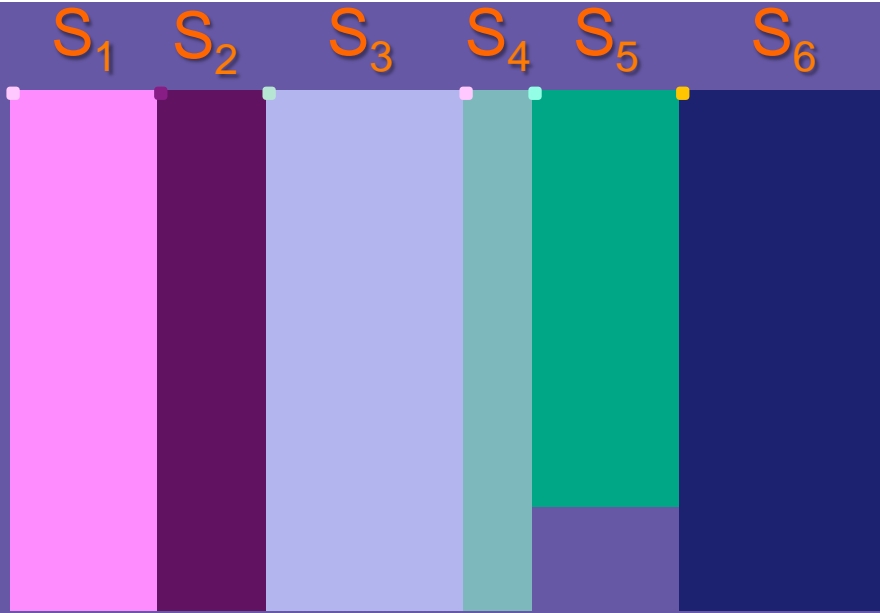
---

HOW TO ANALYZE? COMPUTE CATEGORY MEANS

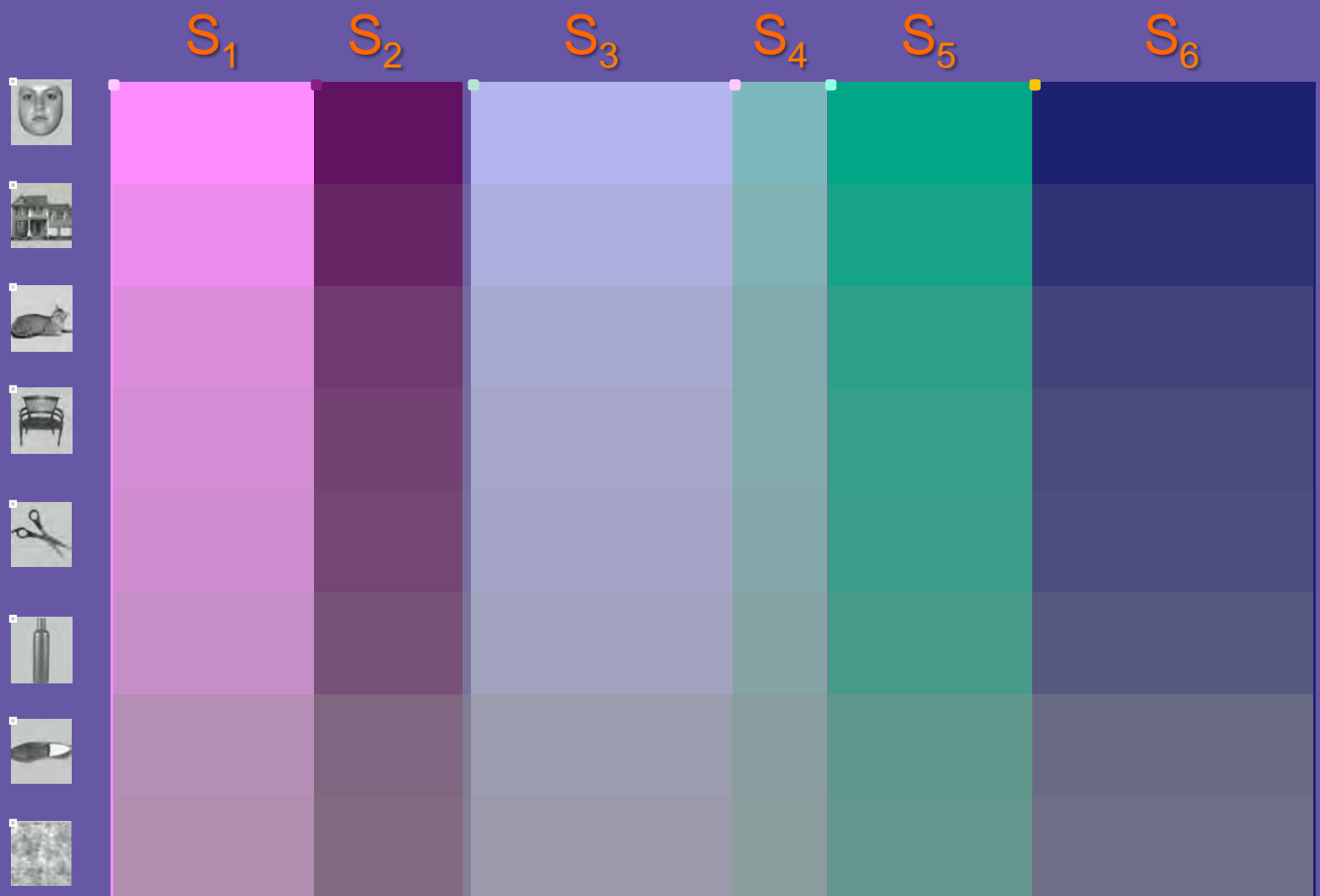


---

HOW TO ANALYZE? COMPUTE CATEGORY MEANS

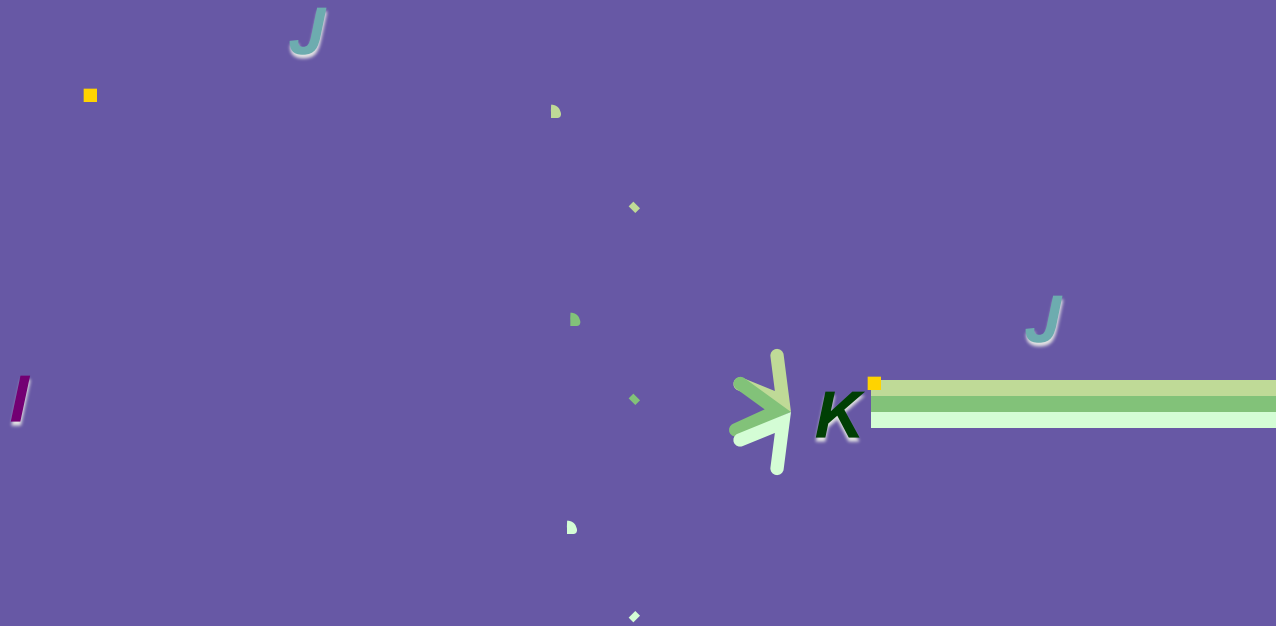


HOW TO ANALYZE? COMPUTE CATEGORY MEANS



DATA: 6 SUBJECTS BY 8 CATEGORIES:  
 AVERAGE ACTIVATION PER CATEGORY

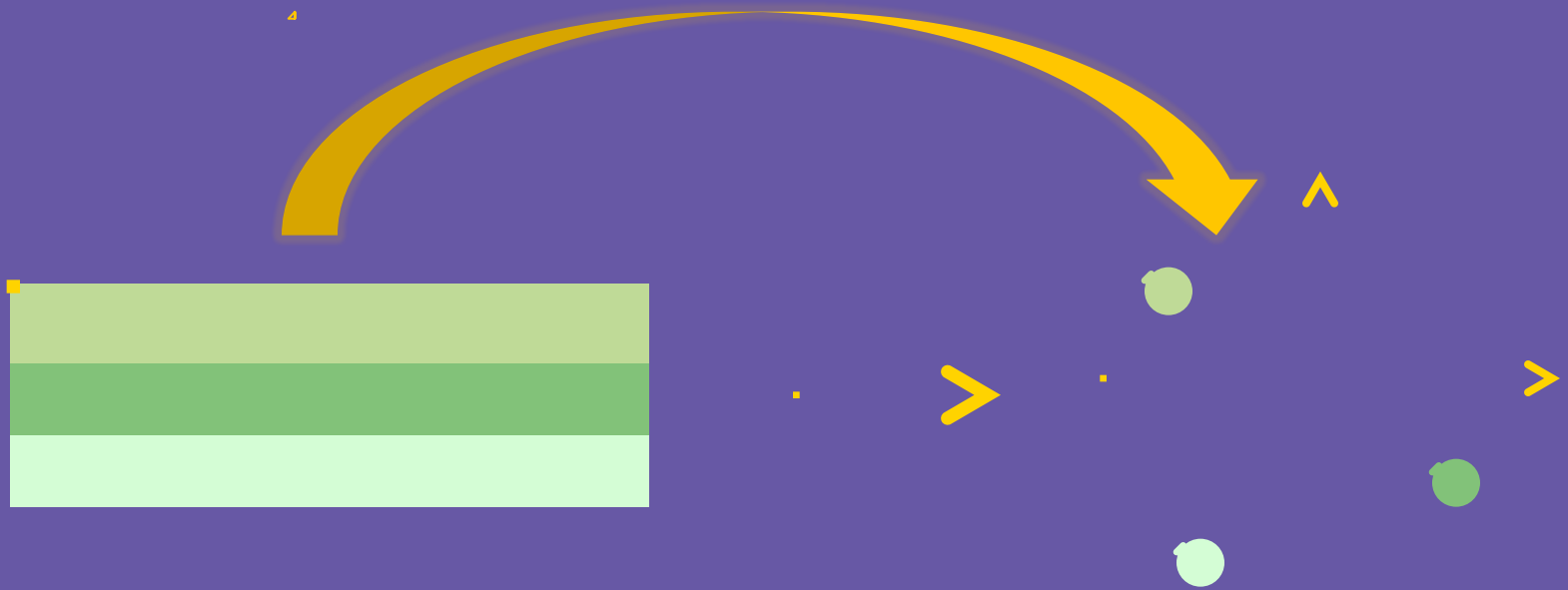
Step one: Compute barycenter.



---

THE BEAUTY OF EUCLID ...

Mix the variables to get “better variables”  
(separate the groups best and independent)  
Then plot the observations



---

PAUSE PRINCIPAL COMPONENT ANALYSIS (PCA)

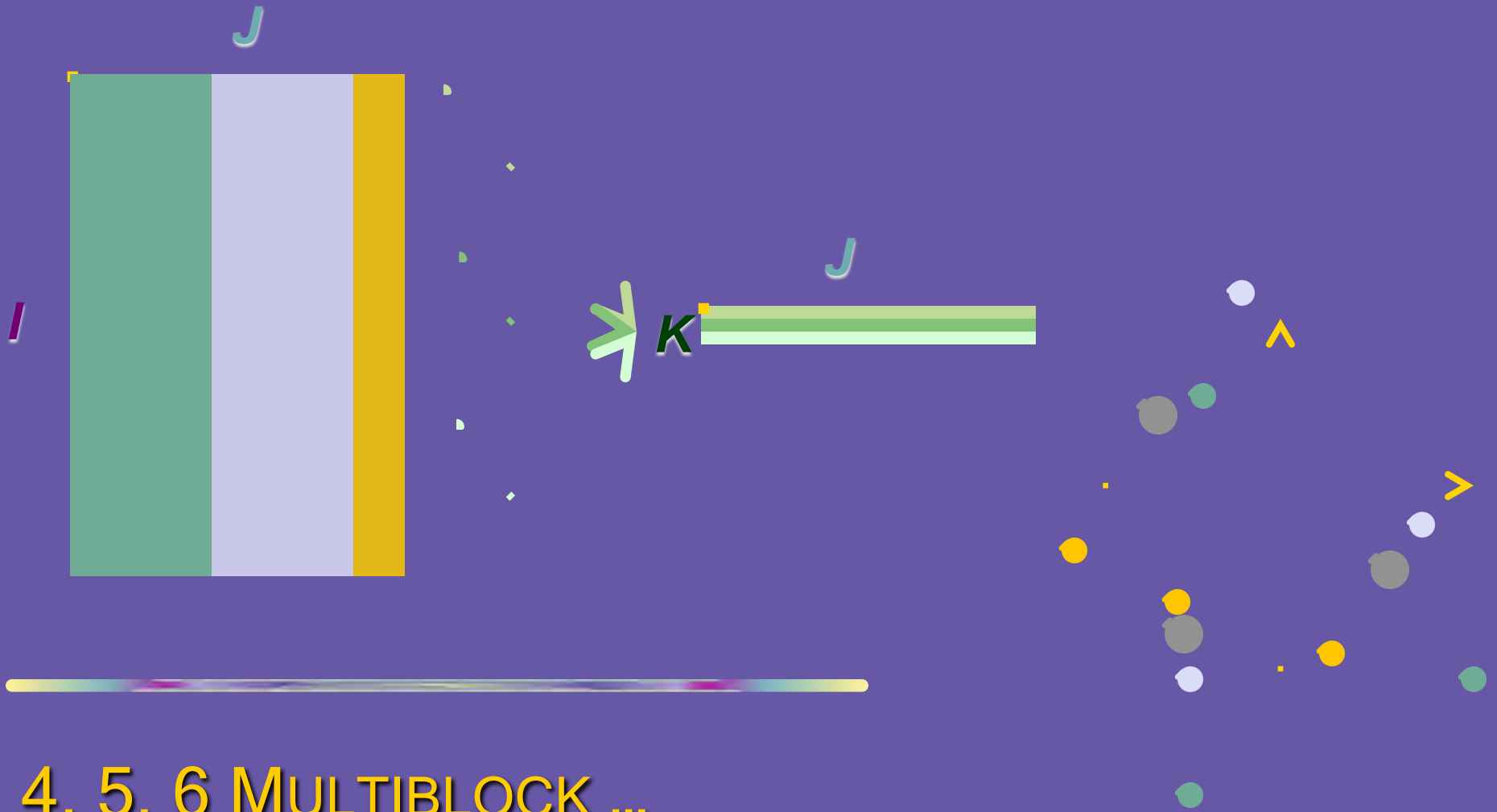
Step two project the observation (supplementary rows)



THE BEAUTY OF EUCLID ...

# Multi-Block Approach

## Project the blocks



4, 5, 6 MULTIBLOCK ...

Start with a  $I$  rows by  $J$  column data matrix:  $X$

---

TIME FOR SOME EQUATIONS

Start with a  $I$  rows by  $J$  columns data matrix:  $\mathbf{X}$

And  $\mathbf{X}$  is made of blocks (sub-tables):

$$\mathbf{X} = [\mathbf{X}_1, \dots, \mathbf{X}_k, \dots, \mathbf{X}_K]$$

with  $\mathbf{X}_k$  being an  $I$  by  $J_k$  matrix

---

TIME FOR SOME EQUATIONS

PCA (i.e., singular value decomposition) of  $\mathbf{X}$

$$\mathbf{X} = [\mathbf{X}_1, \dots, \mathbf{X}_k, \dots, \mathbf{X}_K]$$

gives

$$\mathbf{X} = \mathbf{P}\mathbf{\Delta}\mathbf{Q}^T \text{ with } \mathbf{P}^T\mathbf{P} = \mathbf{Q}^T\mathbf{Q} = \mathbf{I}$$

---

PCA: THE EQUATIONS

From

$$X = P\Delta Q^T \text{ with } P^T P = Q^T Q = I$$

---

PCA: THE EQUATIONS

From

$$X = P\Delta Q^T \text{ with } P^T P = Q^T Q = I$$

We got

---

PCA: THE EQUATIONS

From

$$X = P\Delta Q^T \text{ with } P^T P = Q^T Q = I$$

We got

1. Factor scores (rows):  $F = P\Delta = XQ$

---

PCA: THE EQUATIONS

From

$$X = P\Delta Q^T \text{ with } P^T P = Q^T Q = I$$

We got

1. Factor scores (rows):  $F = P\Delta = XQ$
2. Loadings (columns):  $Q$

---

PCA: THE EQUATIONS

From

$$\mathbf{X} = \mathbf{P}\mathbf{\Delta}\mathbf{Q}^T \text{ with } \mathbf{P}^T\mathbf{P} = \mathbf{Q}^T\mathbf{Q} = \mathbf{I}$$

We got (with  $L$  as rank of  $\mathbf{X}$ )

1. Factor scores (rows) is  $I$  by  $L$ :  $\mathbf{F} = \mathbf{P}\mathbf{\Delta} = \mathbf{X}\mathbf{Q}$
2. Loadings (columns) is  $J$  by  $L$ :  $\mathbf{Q}$   
with

$$\mathbf{Q} = [\mathbf{Q}_1, \dots, \mathbf{Q}_k, \dots, \mathbf{Q}_K]$$

with  $\mathbf{Q}_k$  being an  $L$  by  $J_k$  matrix (corresponds to  $\mathbf{X}_k$ )

---

PCA: THE EQUATIONS

## Getting to the “tables’ projection”

$$\text{So: } \mathbf{X} = \mathbf{P}\mathbf{\Delta}\mathbf{Q}^T = \mathbf{P}\mathbf{\Delta} [ \mathbf{Q}_1, \dots, \mathbf{Q}_k, \dots, \mathbf{Q}_K ]^T$$

1. Factor scores (rows):  $\mathbf{F} = \mathbf{P}\mathbf{\Delta} = \mathbf{X}\mathbf{Q}$
2. Loadings (columns):  $\mathbf{Q}$

---

MULTI-TABLES PROJECTIONS

Getting to the “tables’ projection”

$$\text{So: } \mathbf{X} = \mathbf{P}\mathbf{\Delta}\mathbf{Q}^T = \mathbf{P}\mathbf{\Delta} [\mathbf{Q}_1, \dots, \mathbf{Q}_k, \dots, \mathbf{Q}_K]^T$$

$$\text{and: } \mathbf{F} = \mathbf{P}\mathbf{\Delta} = \mathbf{X}\mathbf{Q}$$

---

MULTI-TABLES PROJECTIONS

Getting to the “tables’ projection”

$$\text{So: } \mathbf{X} = \mathbf{P}\mathbf{\Delta}\mathbf{Q}^T = \mathbf{P}\mathbf{\Delta} [\mathbf{Q}_1, \dots, \mathbf{Q}_k, \dots, \mathbf{Q}_K]^T$$

$$\text{and: } \mathbf{F} = \mathbf{P}\mathbf{\Delta} = \mathbf{X}\mathbf{Q}$$

Give

$$\mathbf{F} = \mathbf{X}\mathbf{Q} = \mathbf{X} [\mathbf{Q}_1, \dots, \mathbf{Q}_k, \dots, \mathbf{Q}_K]$$

---

MULTI-TABLES PROJECTIONS

## Getting to the “tables’ projection”

$$\text{So: } \mathbf{X} = \mathbf{P}\mathbf{\Delta}\mathbf{Q}^T = \mathbf{P}\mathbf{\Delta} [\mathbf{Q}_1, \dots, \mathbf{Q}_k, \dots, \mathbf{Q}_K]^T$$

$$\text{and: } \mathbf{F} = \mathbf{P}\mathbf{\Delta} = \mathbf{X}\mathbf{Q}$$

Give

$$\begin{aligned} \mathbf{F} &= \mathbf{X}\mathbf{Q} = \mathbf{X} [\mathbf{Q}_1, \dots, \mathbf{Q}_k, \dots, \mathbf{Q}_K] \\ &= [\mathbf{X}_1, \dots, \mathbf{X}_k, \dots, \mathbf{X}_K] \times [\mathbf{Q}_1, \dots, \mathbf{Q}_k, \dots, \mathbf{Q}_K] \end{aligned}$$

---

MULTI-TABLES PROJECTIONS

## Getting to the “tables’ projection”

$$\text{So: } \mathbf{X} = \mathbf{P}\mathbf{\Delta}\mathbf{Q}^T = \mathbf{P}\mathbf{\Delta} [\mathbf{Q}_1, \dots, \mathbf{Q}_k, \dots, \mathbf{Q}_K]^T$$

$$\text{and: } \mathbf{F} = \mathbf{P}\mathbf{\Delta} = \mathbf{X}\mathbf{Q}$$

Give

$$\mathbf{F} = \mathbf{X}\mathbf{Q} = \mathbf{X} [\mathbf{Q}_1, \dots, \mathbf{Q}_k, \dots, \mathbf{Q}_K]$$

$$= [\mathbf{X}_1, \dots, \mathbf{X}_k, \dots, \mathbf{X}_K] \times [\mathbf{Q}_1, \dots, \mathbf{Q}_k, \dots, \mathbf{Q}_K]$$

$$= \mathbf{X}_1 \mathbf{Q}_1 + \dots + \mathbf{X}_k \mathbf{Q}_k + \dots + \mathbf{X}_K \mathbf{Q}_K$$

---

MULTI-TABLES PROJECTIONS

## Getting to the “tables’ projection”

So from  $\mathbf{X} = \mathbf{P}\mathbf{\Delta}\mathbf{Q}^T = \mathbf{P}\mathbf{\Delta} [\mathbf{Q}_1, \dots, \mathbf{Q}_k, \dots, \mathbf{Q}_K]^T$

we got

$$\mathbf{F} = \mathbf{X}_1 \mathbf{Q}_1 + \dots + \mathbf{X}_k \mathbf{Q}_k + \dots + \mathbf{X}_K \mathbf{Q}_K$$

---

MULTI-TABLES PROJECTIONS

## Getting to the “tables’ projection”

So from  $\mathbf{X} = \mathbf{P}\mathbf{\Delta}\mathbf{Q}^T = \mathbf{P}\mathbf{\Delta} [\mathbf{Q}_1, \dots, \mathbf{Q}_k, \dots, \mathbf{Q}_K]^T$

we got

$$\mathbf{F} = \mathbf{X}_1 \mathbf{Q}_1 + \dots + \mathbf{X}_k \mathbf{Q}_k + \dots + \mathbf{X}_K \mathbf{Q}_K$$

I want the compromise factor score as mean of tables

$$\mathbf{F} = 1/K \sum \mathbf{F}_k$$

---

MULTI-TABLES PROJECTIONS

## Getting to the “tables’ projection”

So from  $\mathbf{X} = \mathbf{P}\mathbf{\Delta}\mathbf{Q}^T = \mathbf{P}\mathbf{\Delta} [\mathbf{Q}_1, \dots, \mathbf{Q}_k, \dots, \mathbf{Q}_K]^T$

we got

$$\mathbf{F} = \mathbf{X}_1 \mathbf{Q}_1 + \dots + \mathbf{X}_k \mathbf{Q}_k + \dots + \mathbf{X}_K \mathbf{Q}_K$$

I want the compromise factor score as mean of tables

$$\mathbf{F} = 1/K \sum \mathbf{F}_k$$

So:

$$\mathbf{F}_k = K \mathbf{X}_k \mathbf{Q}_k$$

---

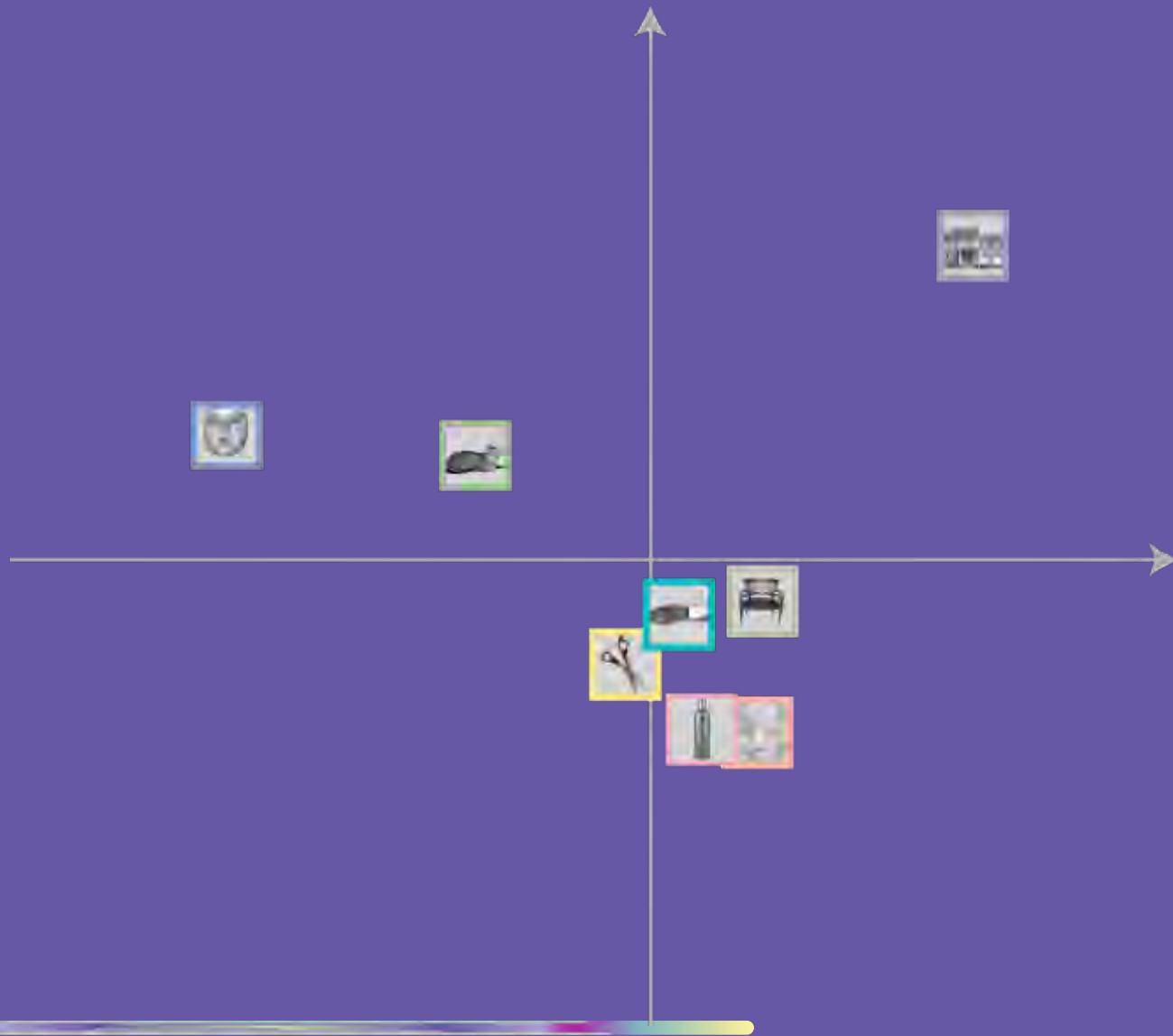
## MULTI-TABLES PROJECTIONS



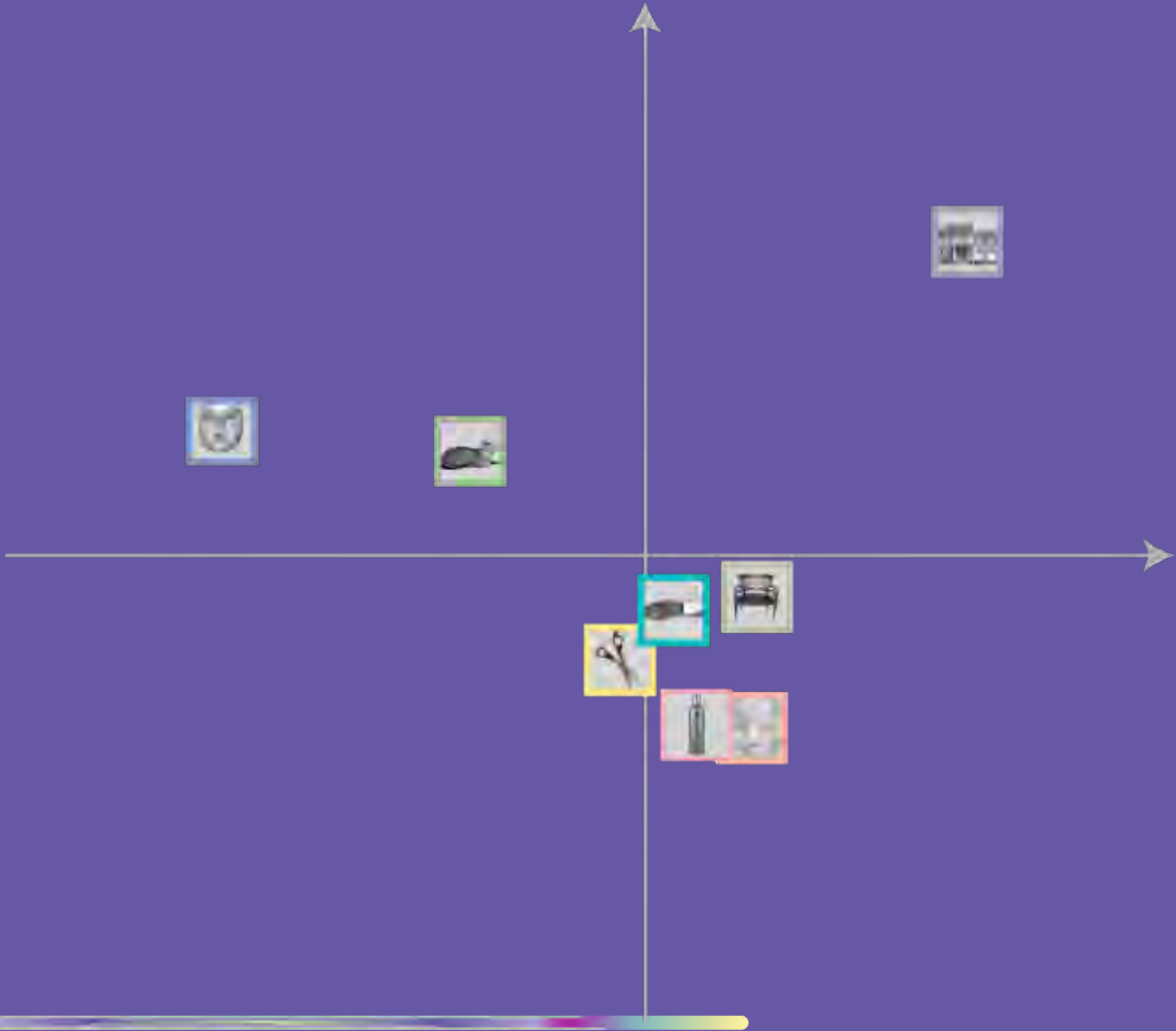
**READY FOR THE PICTURES?**

---

ALTOGETHER RESULTS



CATEGORIES



PRETTY



BUT, SO WHAT?

- Call for a test?
- Sampling distribution?

---

HOW STABLE IS THIS (IS  $P < .05$ ?)

REMEMBER COHEN'S THE EARTH IS ROUND  $P < .05$

- Get confidence Intervals

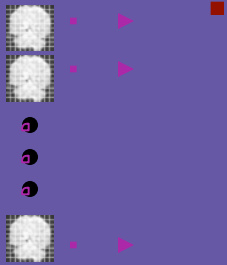
---

USE BOOTSTRAP

# Bootstrap

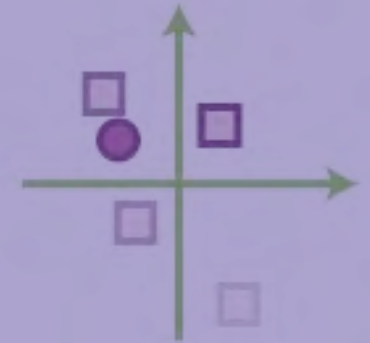
---

**THE SAMPLE *IS* THE  
POPULATION**

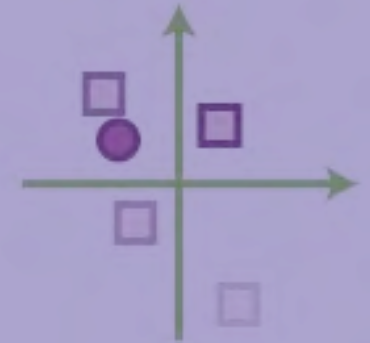


---

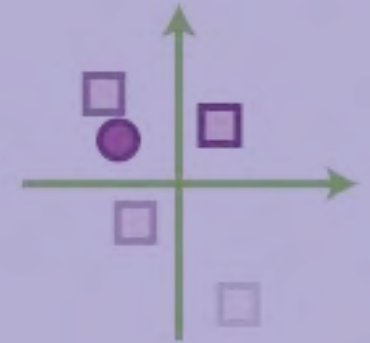
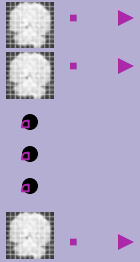
BOOTSTRAP: START WITH A DATA TABLE



BOOTSTRAP: DO THE ANALYSIS

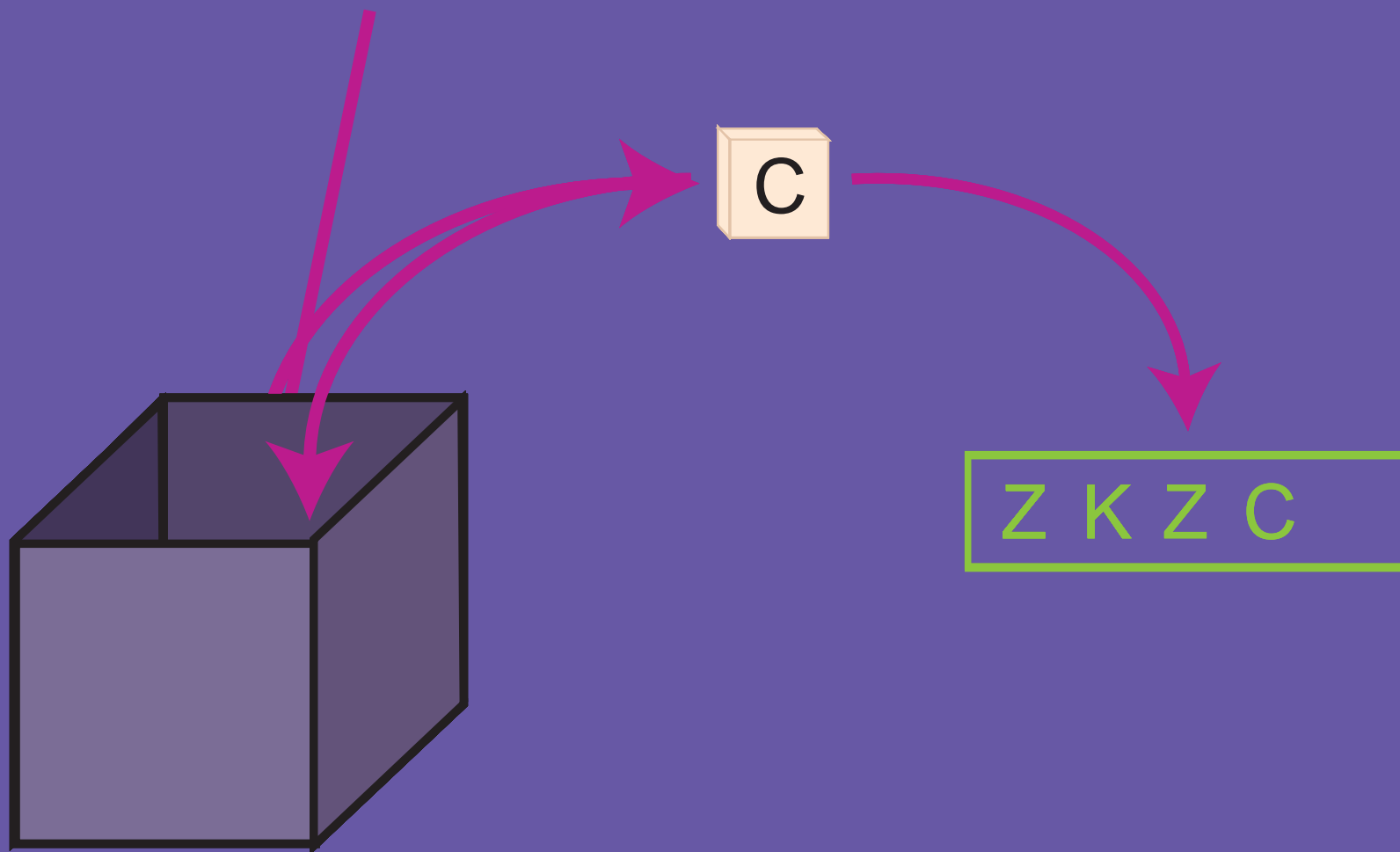


**BOOTSTRAP: DO THE ANALYSIS**

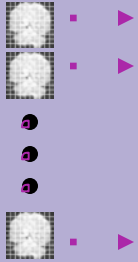


BOOTSTRAP: GENERATE BOOTSTRAP SAMPLE

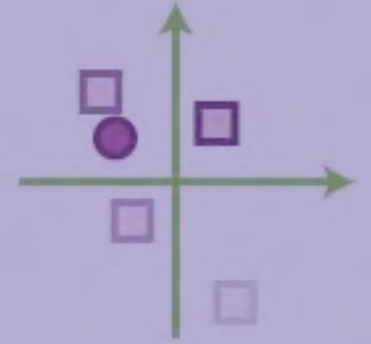
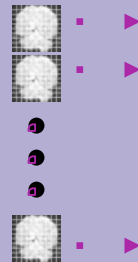
V C H Z K



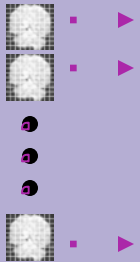
DRAWING WITH REPLACEMENT



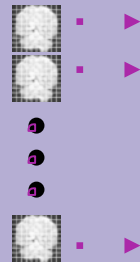
Brains



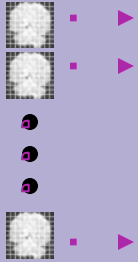
SO GET BOOTSTRAP SAMPLE



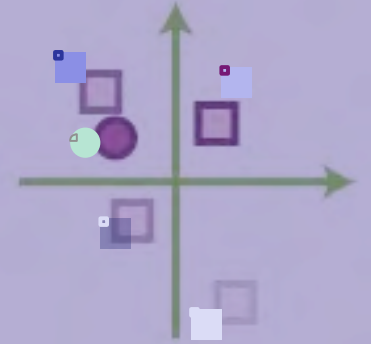
Brains



PROJECT BOOTSTRAP SAMPLE ONTO ORIGINAL

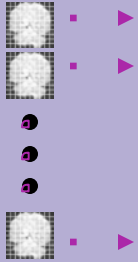


Brains



---

KEEP ON WITH MORE BOOTSTRAP SAMPLES

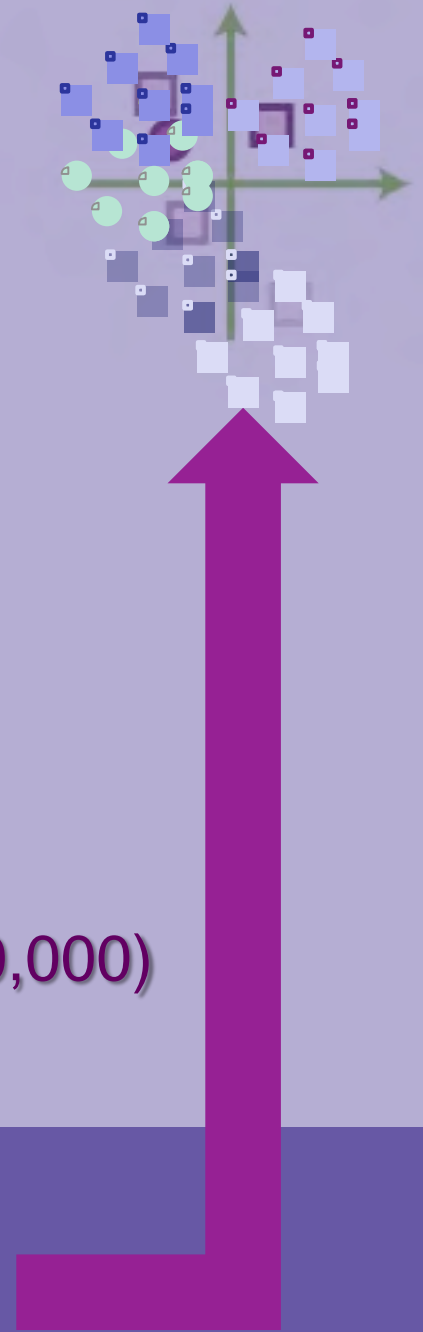


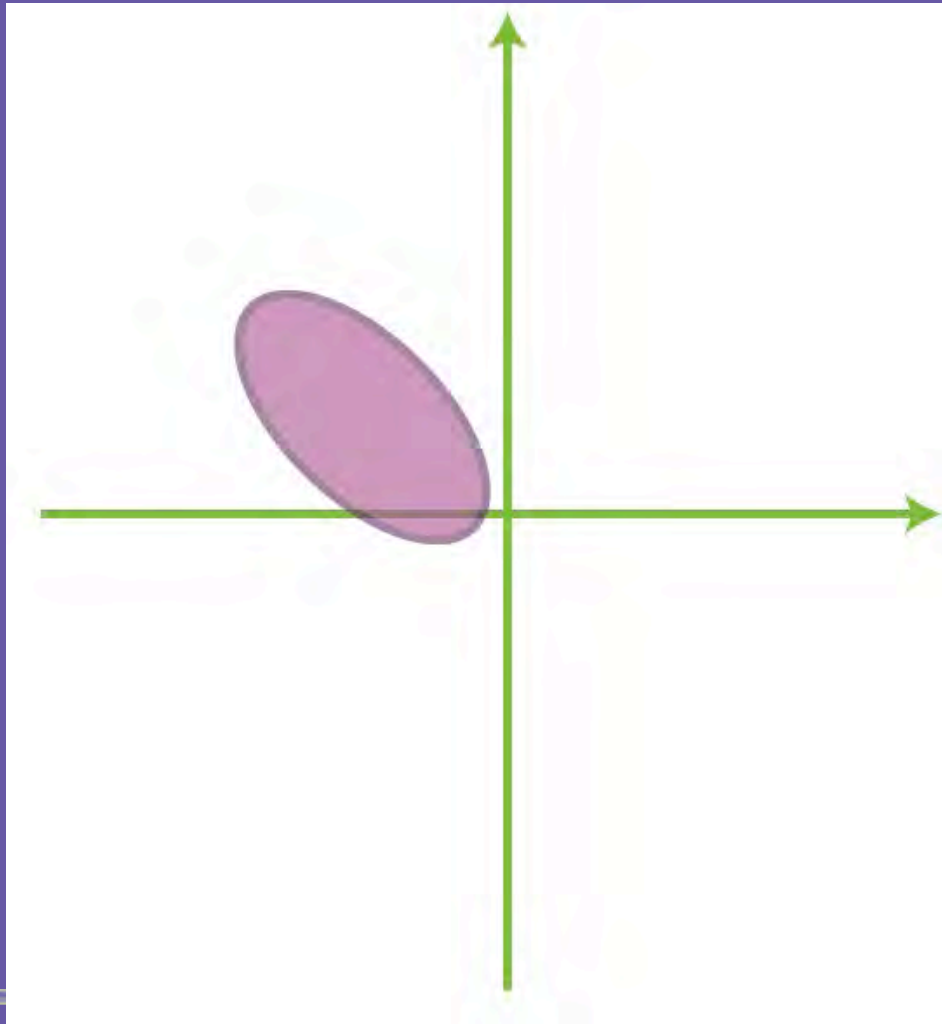
Brains



- 
- 
- 

A lot o' times (e.g., 10,000)



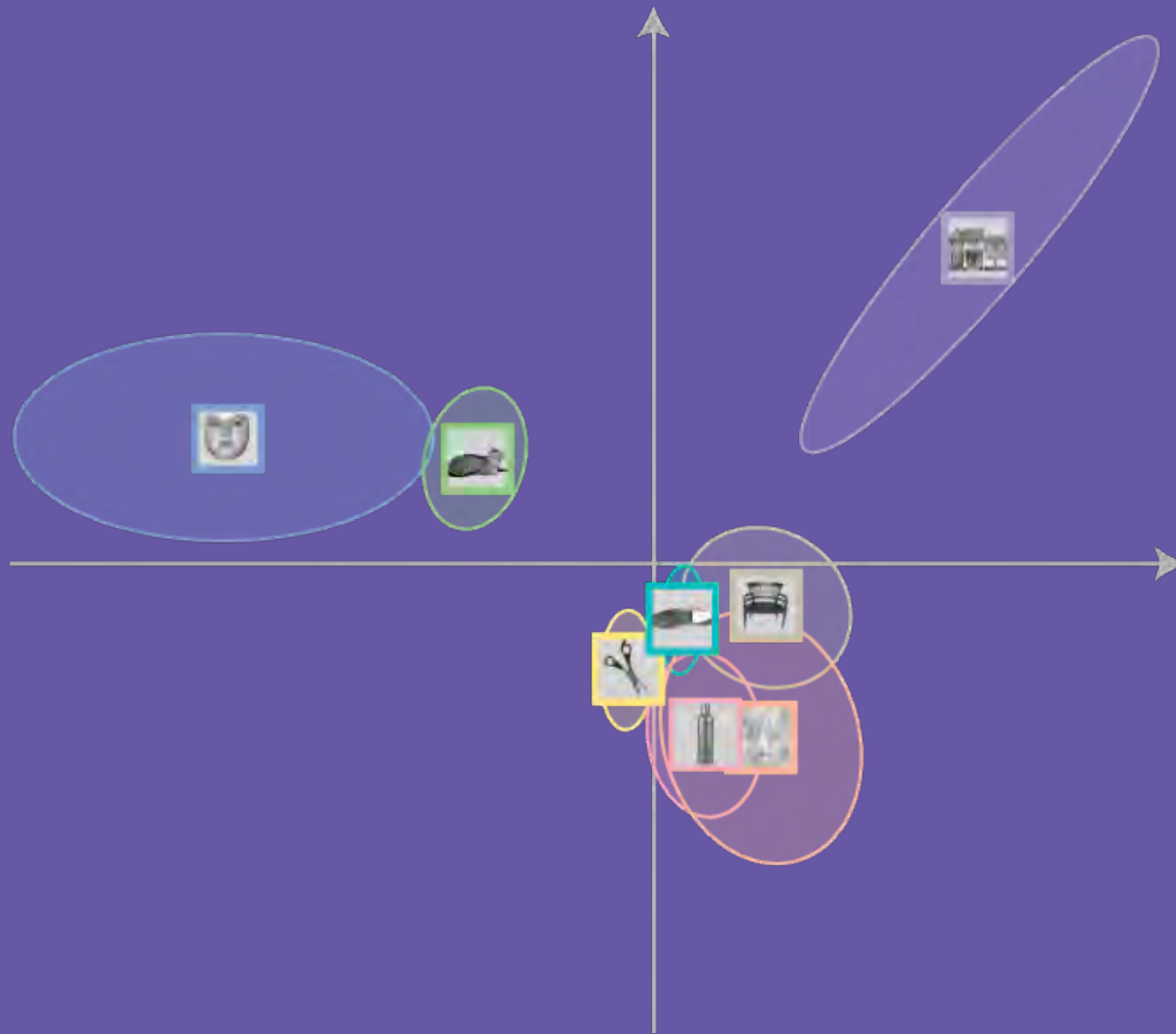


**FIT A 95% ELLIPSOID: CONFIDENCE INTERVAL**

- 1. Bootstrap the participants
- 2. Bootstrap the scans
- 3. put all that together.
- 4. Project in the common space

---

**DOUBLE BOOTSTRAP**



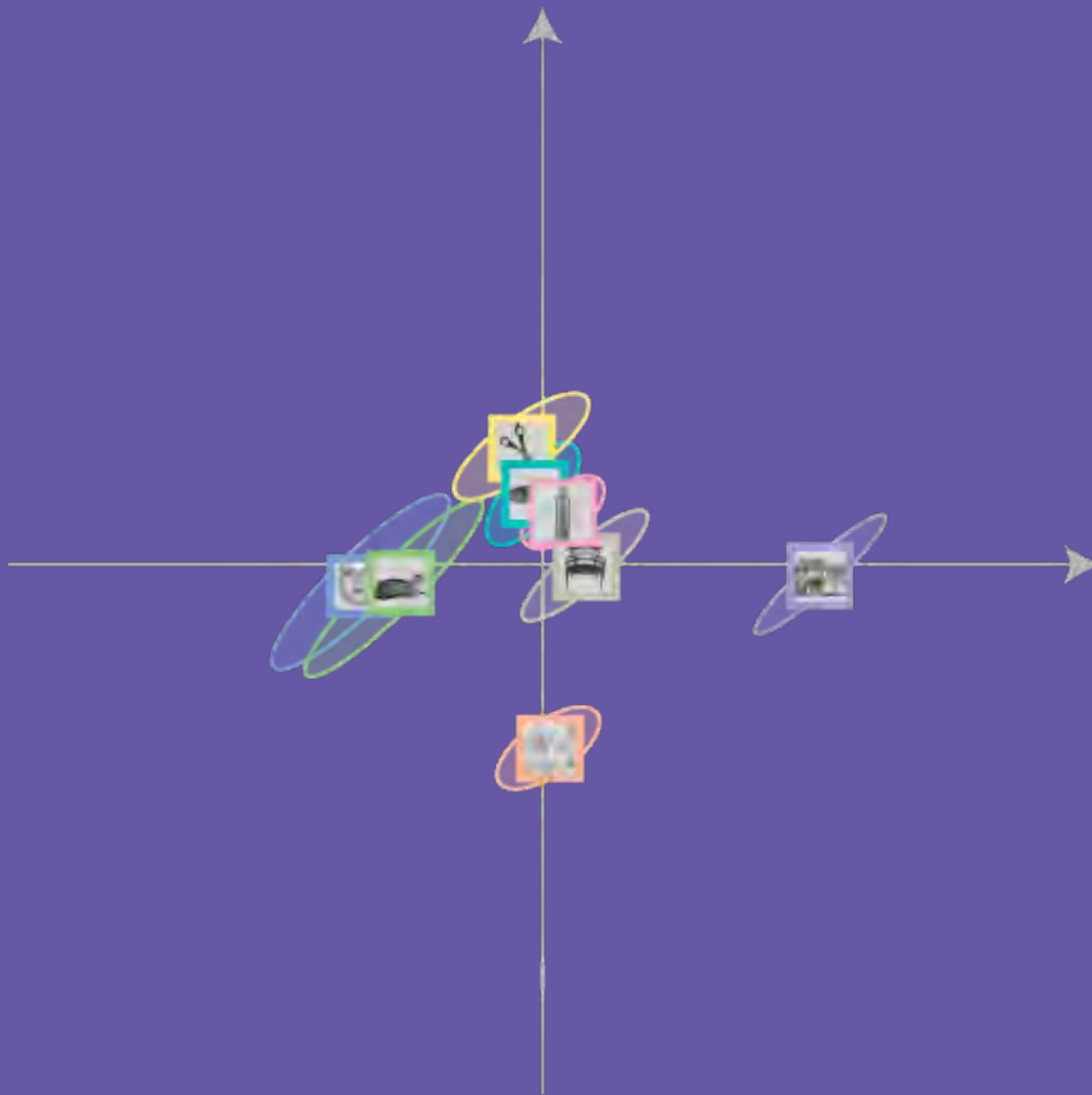
**BETWEEN CATEGORY CONFIDENCE INTERVALS  
THE EARTH IS ROUND!**

- Look at one participant (#3)

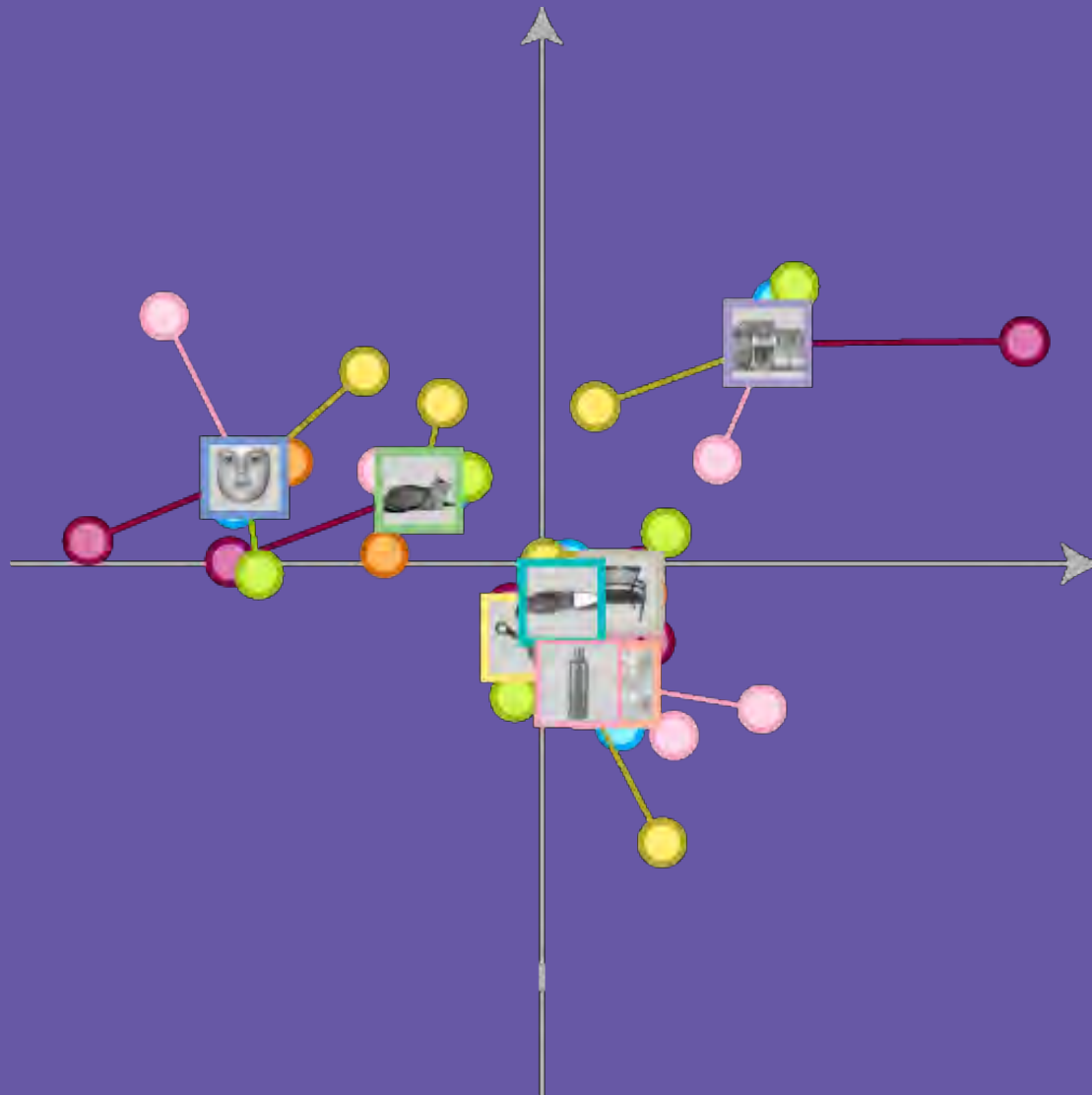
Use Block projection

---

**BACK TO THE PRESENT!**



S3 CONFIDENCE INTERVAL



CATEGORIES AS BARYCENTER OF SUBJECT TABLES

- Brain or Image?

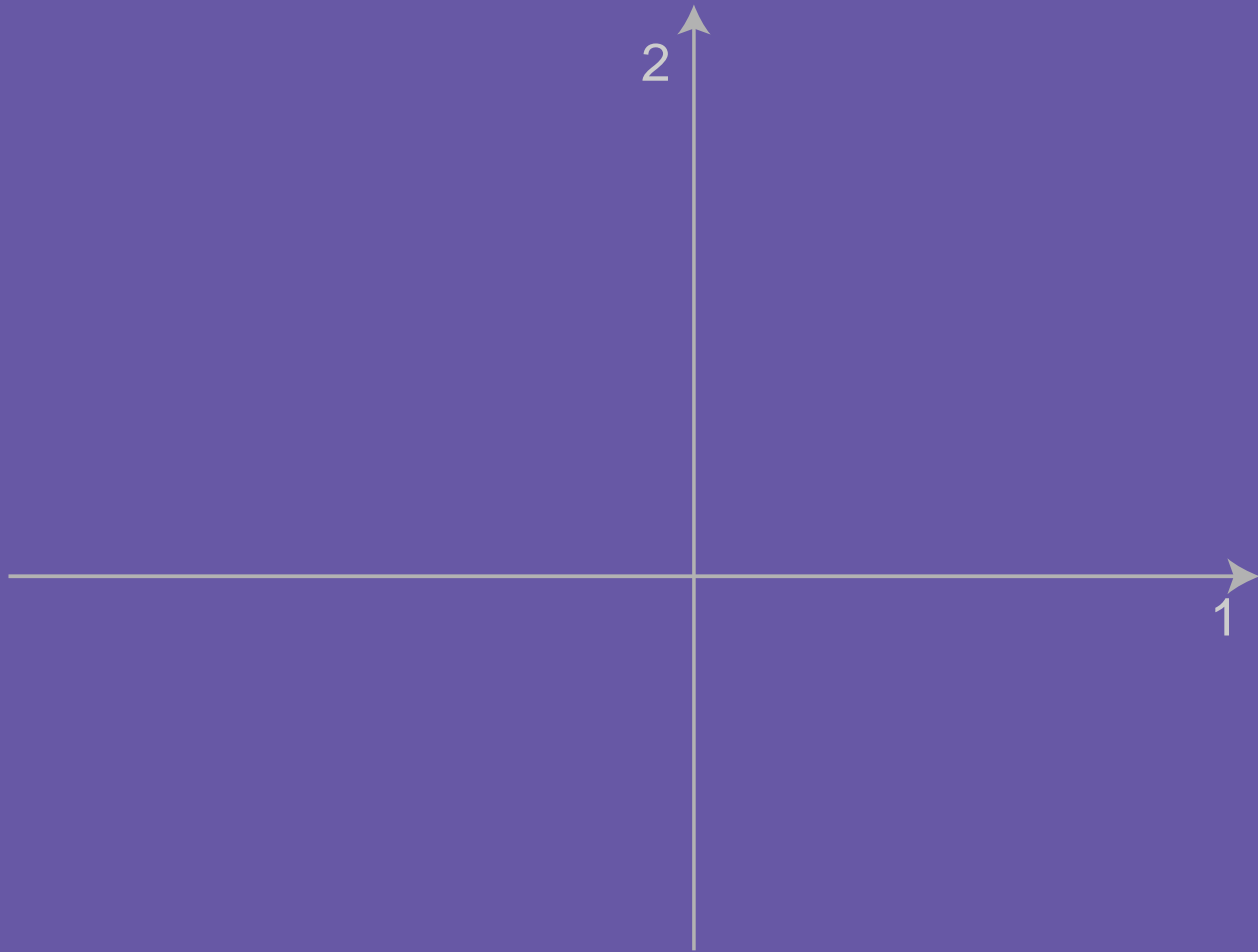
---

WHERE DOES THE CATEGORIZATION COME FROM?

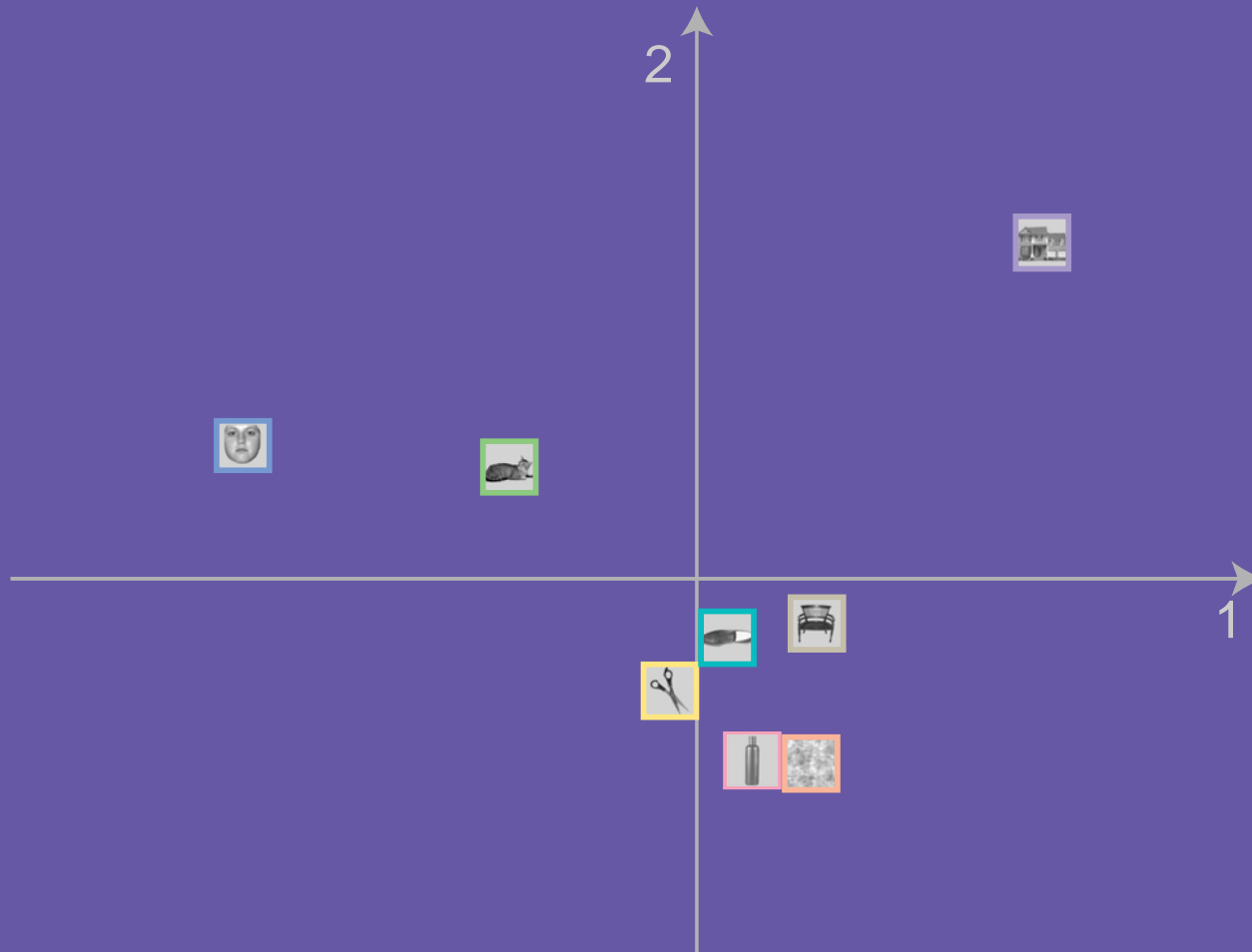
- Project the images onto the brain space

---

**REDO THE ANALYSIS WITH THE IMAGES**

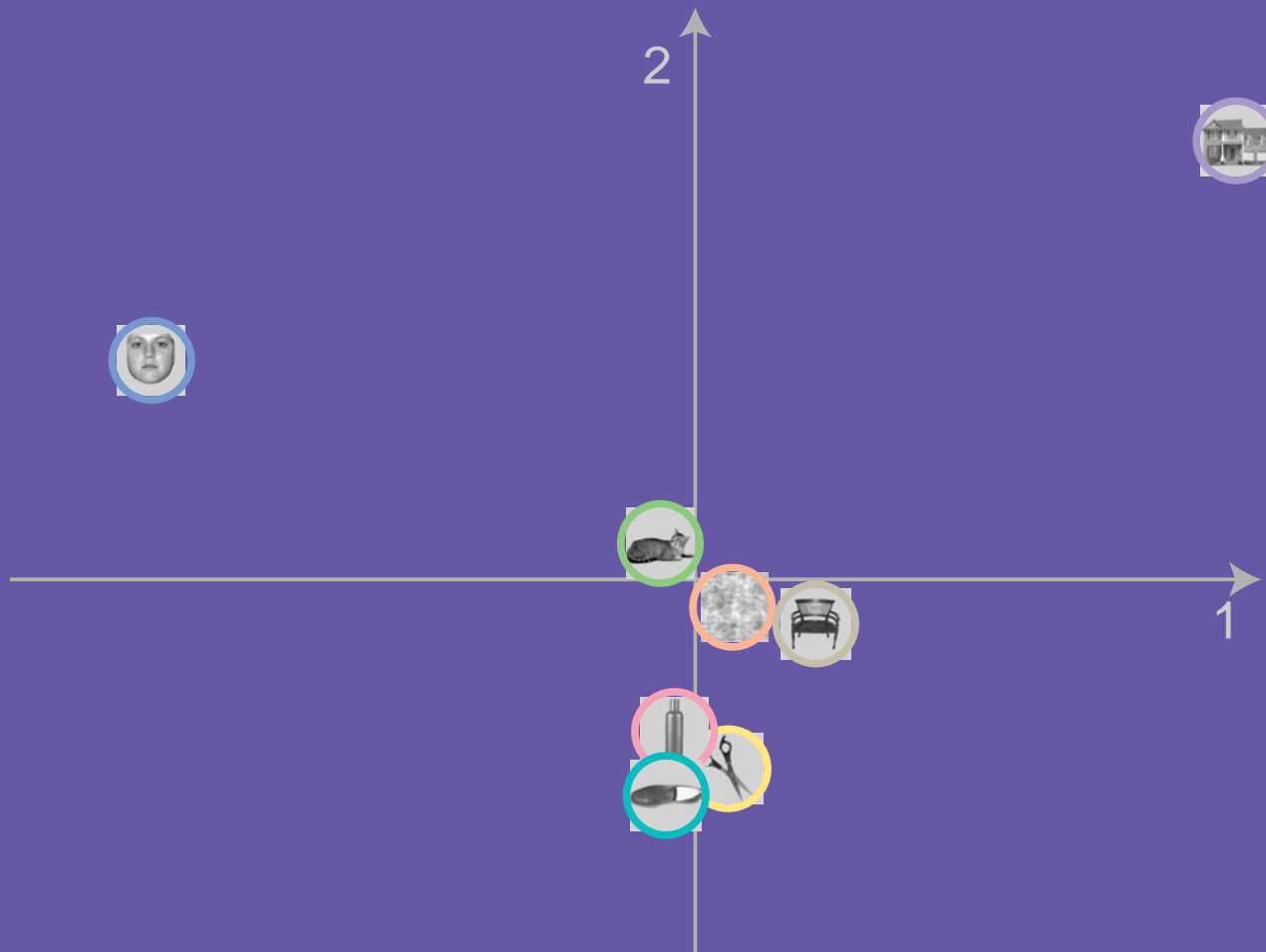


HAXBY 1

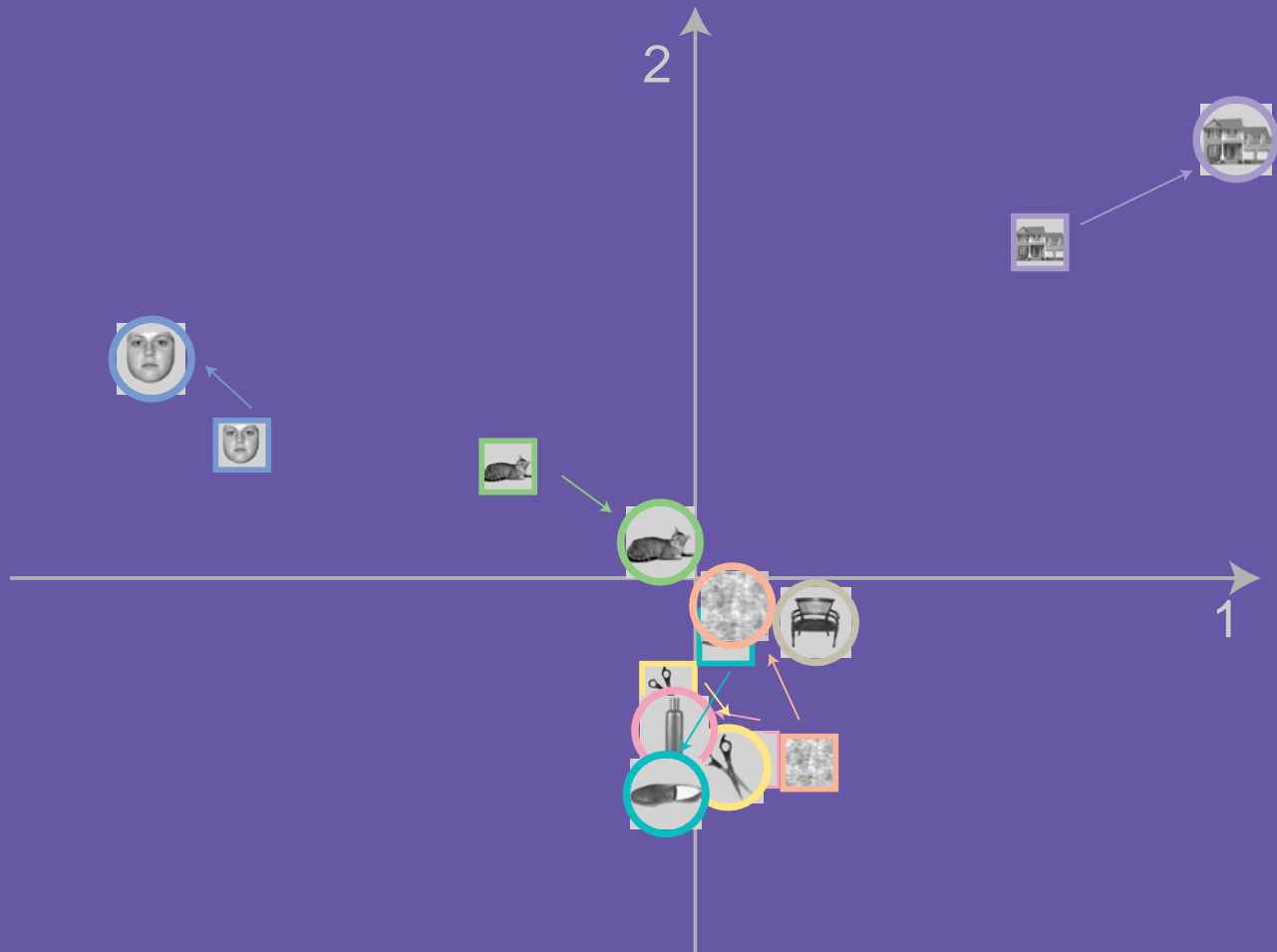


---

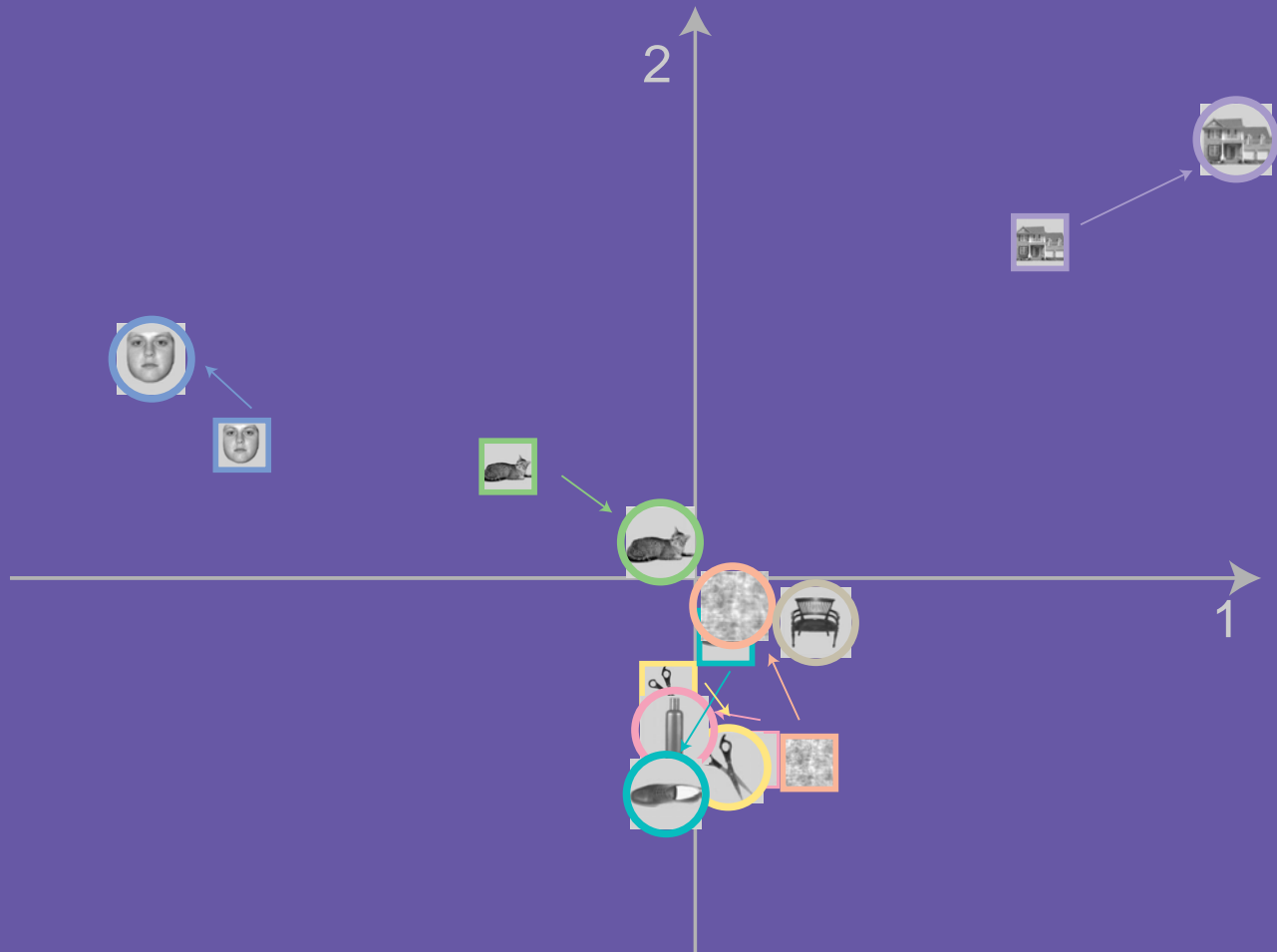
# THE BRAIN SPACE



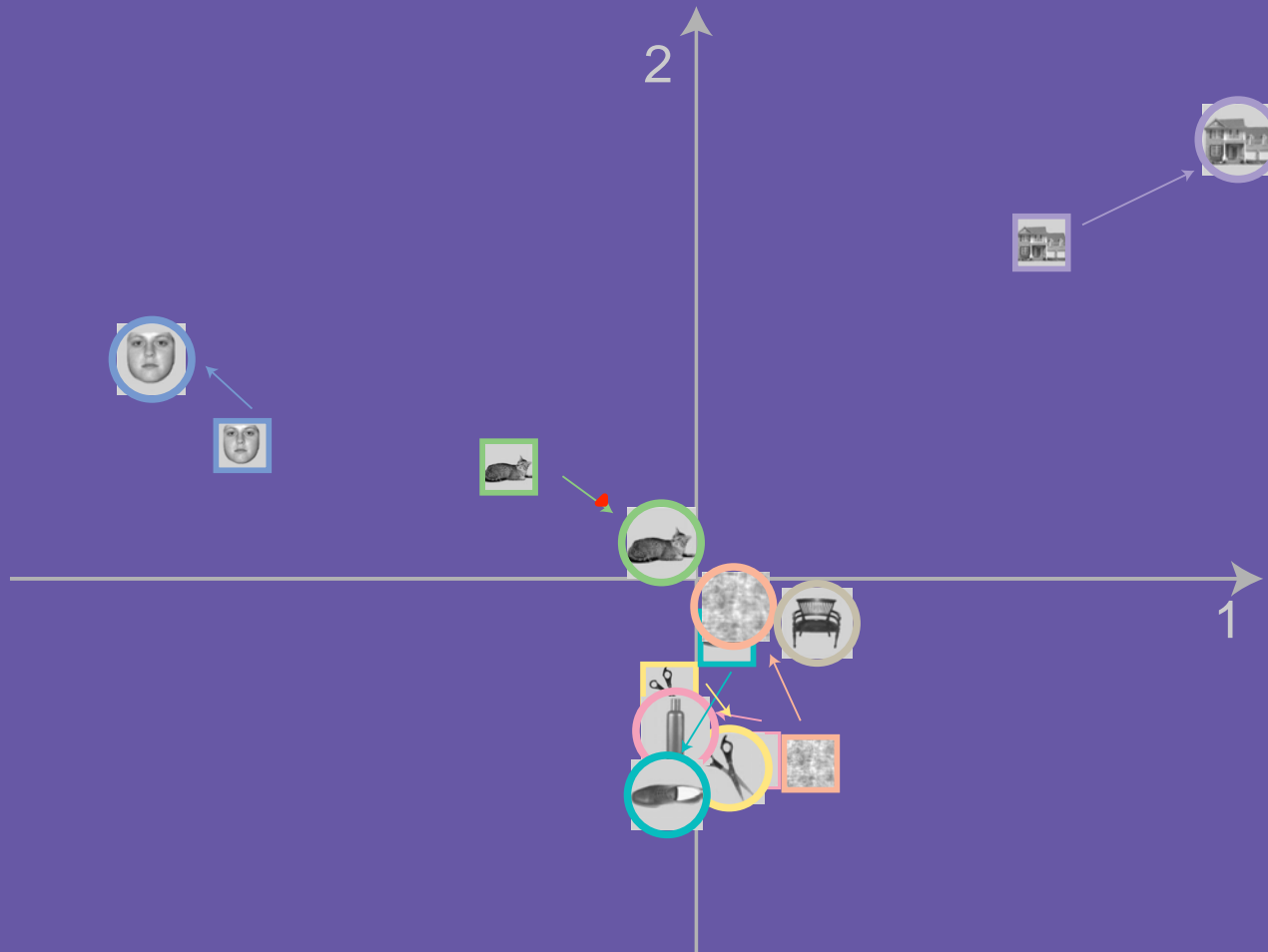
THE IMAGE PROJECTED ONTO THE BRAIN SPACE



**BRAIN AND IMAGES IN BRAIN SPACE**



# IMAGES IN THE BRAIN SPACE



FOR THE BRAIN CATS LOOK LIKE HUMANS  
CATS HAVE FACES!

- Cats have faces!

---

FINALE: VARIATION 1

## VARIATION 2

---

Dogs and monkeys have faces  
too?

- Try other types of faces
- Same design as in 2001
- But: Use anatomical definitions
- Use 3 Regions of Interest (ROIs)

---

**DOGS AND MONKEYS HAVE FACES**

- 10 Participants
- 7 categories
- Block design (8 runs × 7 blocks)
- Task: one back
- 3T scanner/TR=2s/



---

## FACES AND OBJECTS

- 1. Medial occipital (MO) includes:  
calcarine cortex
- 2. Inferior occipital (IO) includes:  
lateral object sensitive regions
- 3. Ventro Temporal (VT) includes:  
inferior temporal, fusiform, parahippocampal gyri

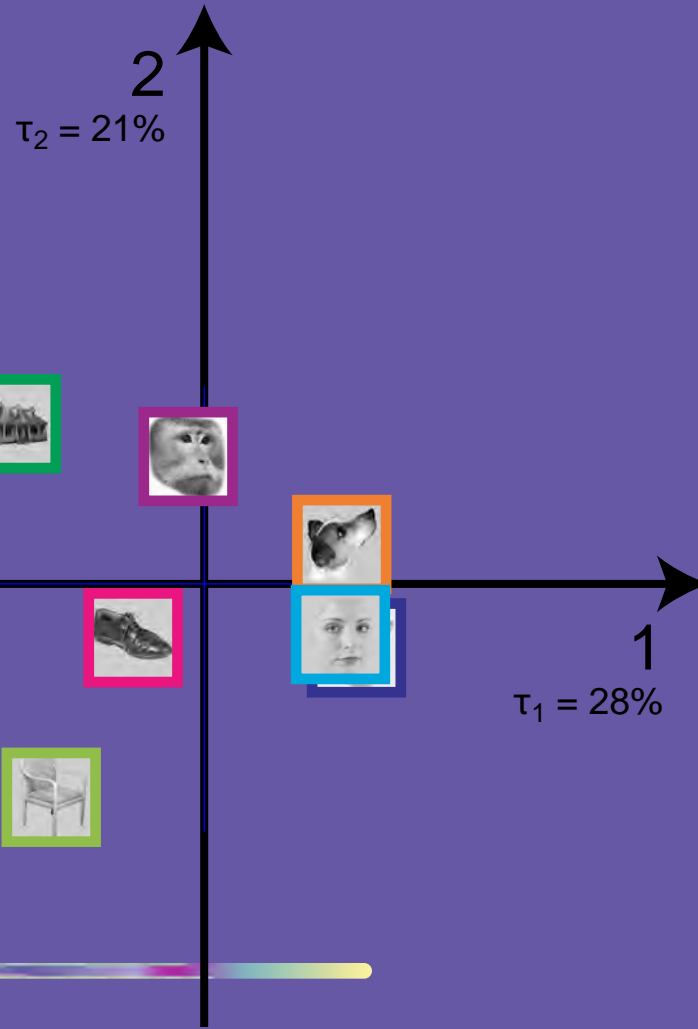
---

**THREE ANATOMICAL ROIs:  
FROM LOW LEVEL TO HIGH LEVEL VISION**

- **Implies different # of voxels per subjects**
- **Medial Occipital (MO): 435 to 1261 voxels**
- **Inferior Occipital (IO) : 688 to 1859 voxels**
- **Ventro-Temporal (VT): 2791 to 4815 voxels**

---

**ANATOMICAL ROIs**



All Rois

---

WHAT ARE THE DIMENSIONS?

- Dimension 1: Faces vs. non faces (semantic?)

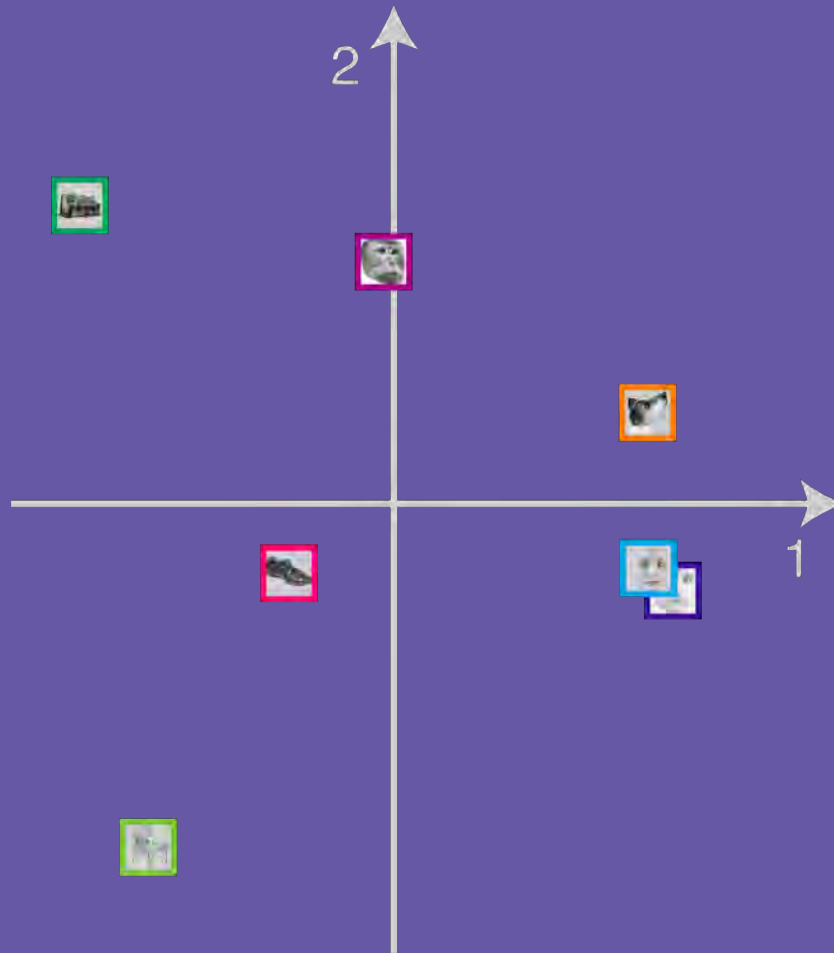
---

WHAT ARE THE DIMENSIONS?

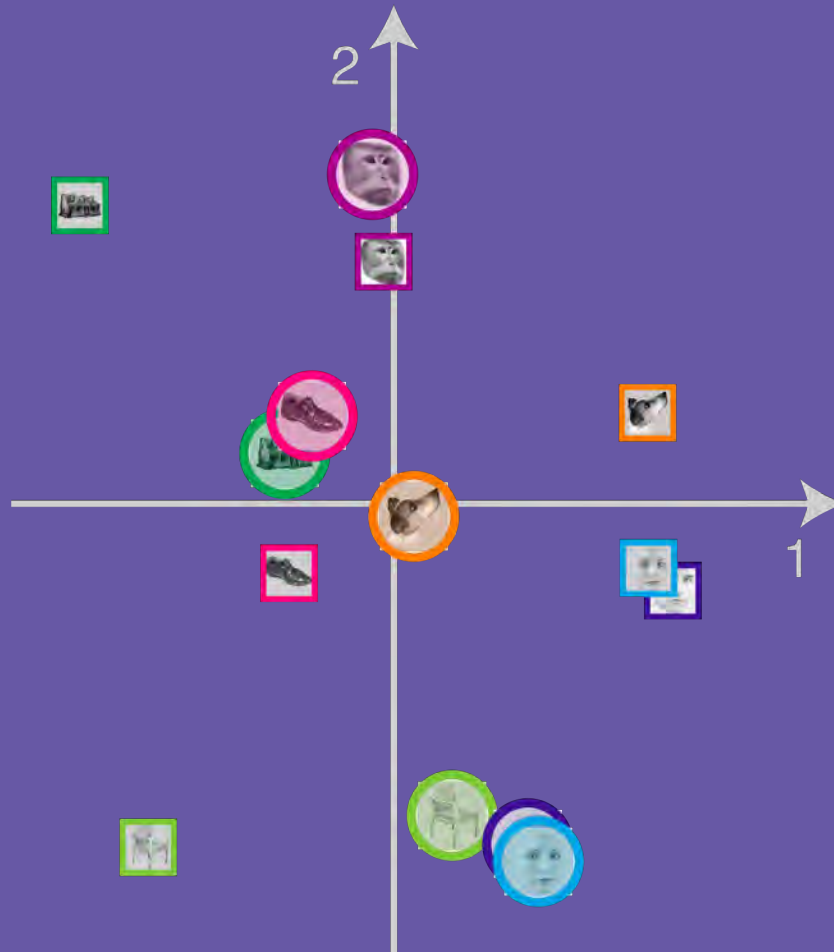
- Dimension 1: Faces vs non faces (semantic?)
- Dimension 2: Low level again?

---

**WHAT ARE THE DIMENSIONS?**



## MONKEY-DOG: BRAIN CATEGORIES



MONKEY-DOG: WITH THE PICTURES

- Dimension 1: Semantic
- Dimension 2: Low Level

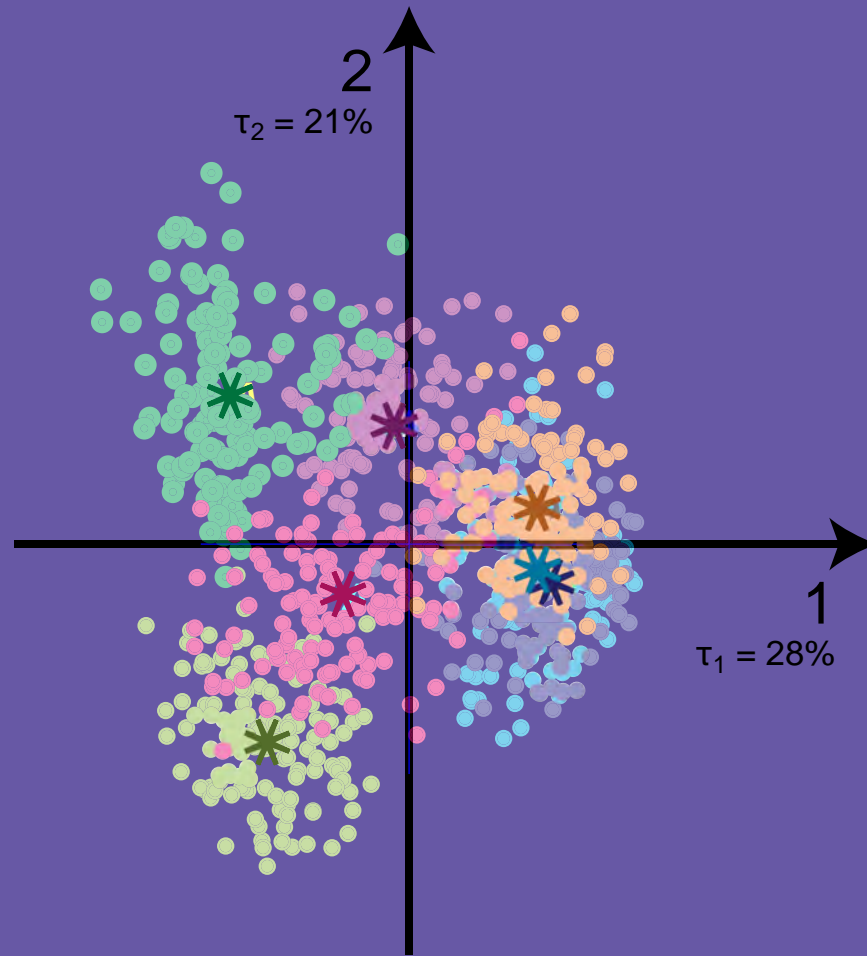
---

**DIMENSIONS**

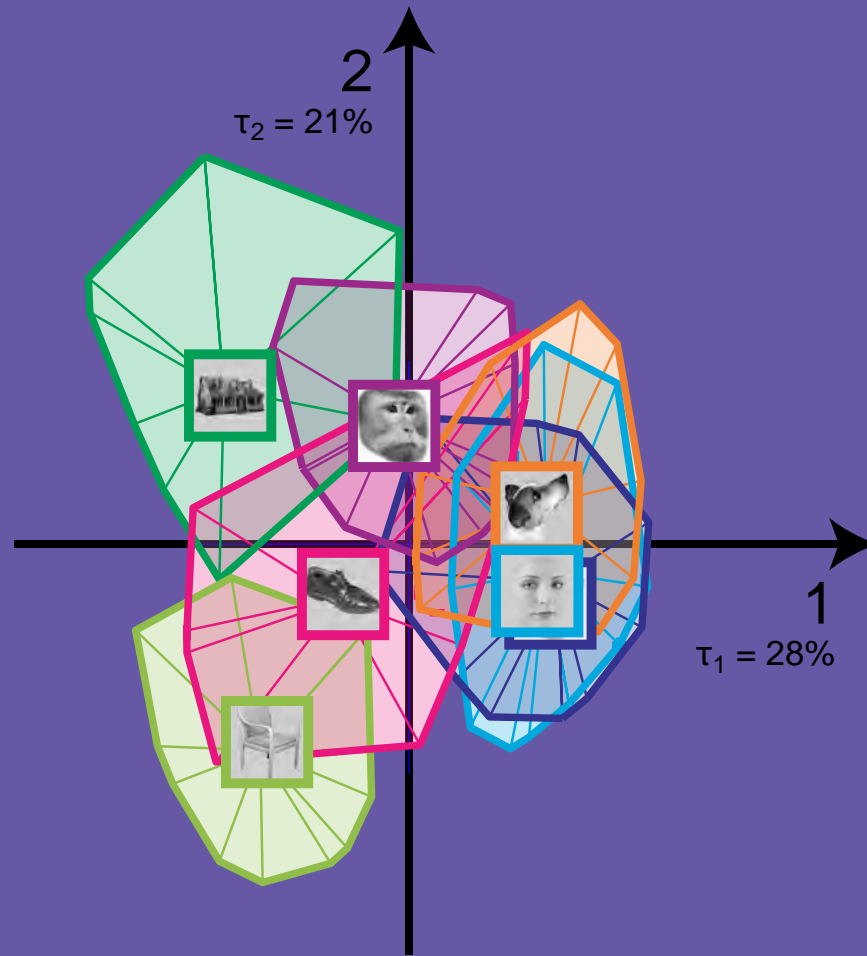
- One scan is one point.
- Look at the scans

---

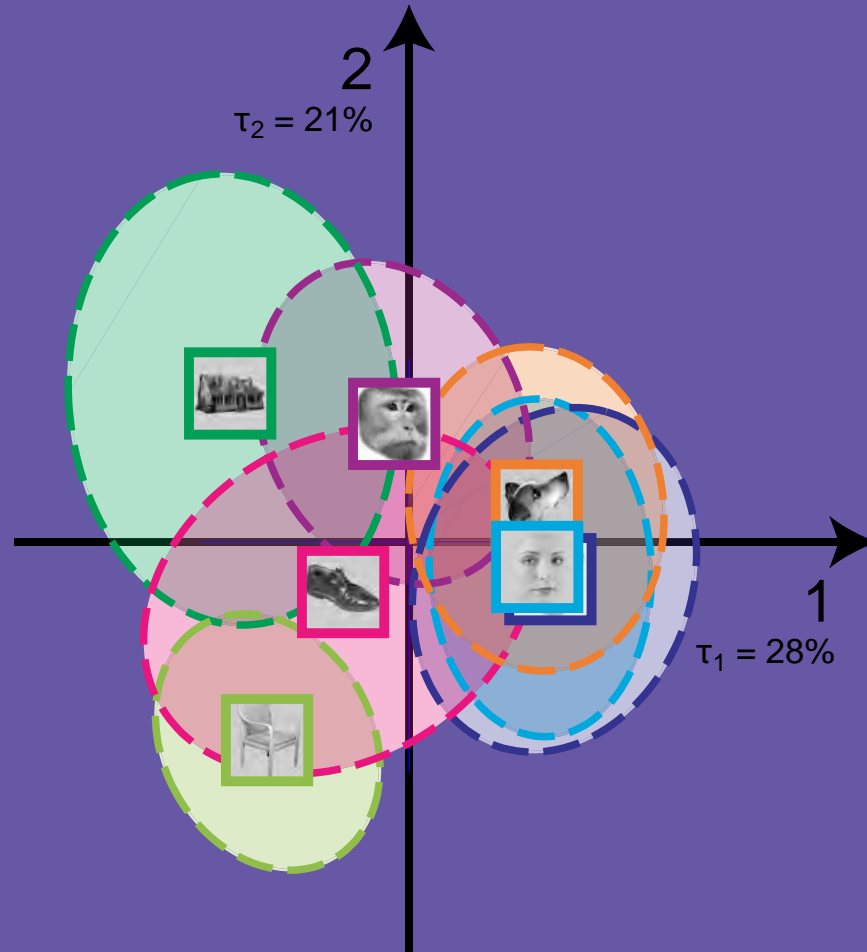
HOW GOOD IS THE MODEL?



All Rois. Observations



All Rois Convex Hulls

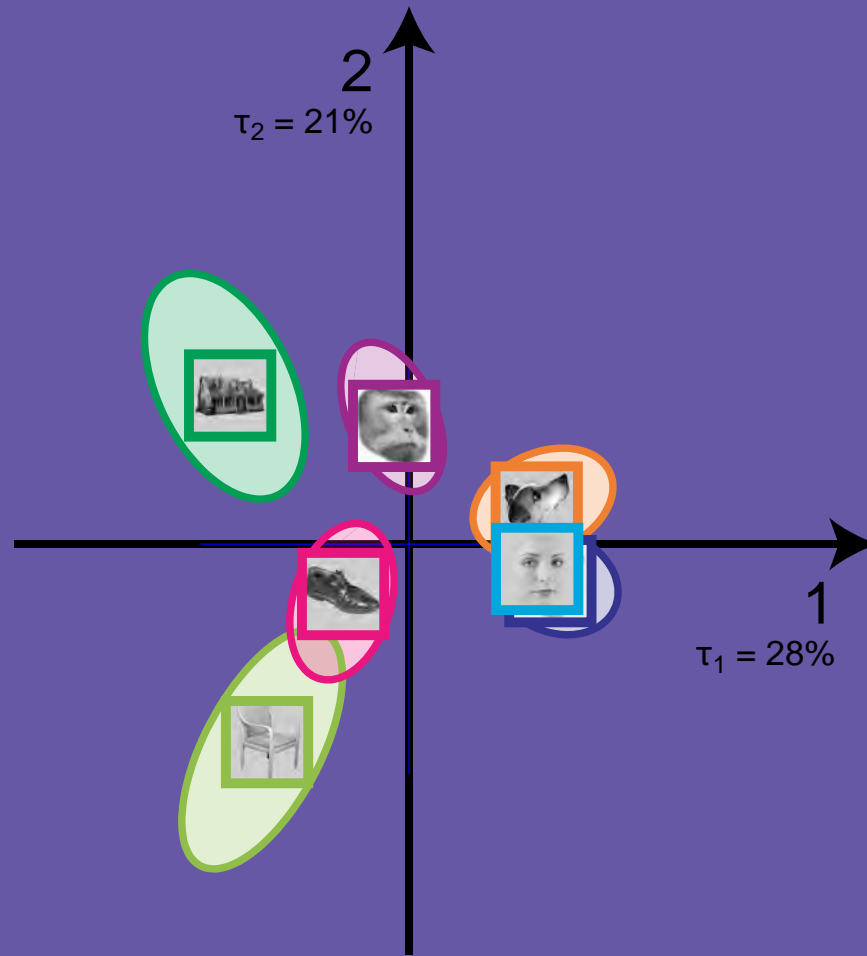


All Rois Tolerance Intervals

---

IS THE EARTH ROUND?

BOOTSTRAP AGAIN FOR CONFIDENCE INTERVALS



All Rois Confidence Intervals

---

HOW GOOD IS THE PREDICTION FOR NEW SCANS

J

■

▶

▶

▶

1-1

---

BADA: JACKKNIFE TAKE ROW OR BLOCK 1 ...

J

■

■

■

■

1-1

---

BADA: JACKKNIFE TAKE ROW OR BLOCK 1 ...

1-1



K



J



?



BADA: JACKKNIFE ...

I-1



K



J



?



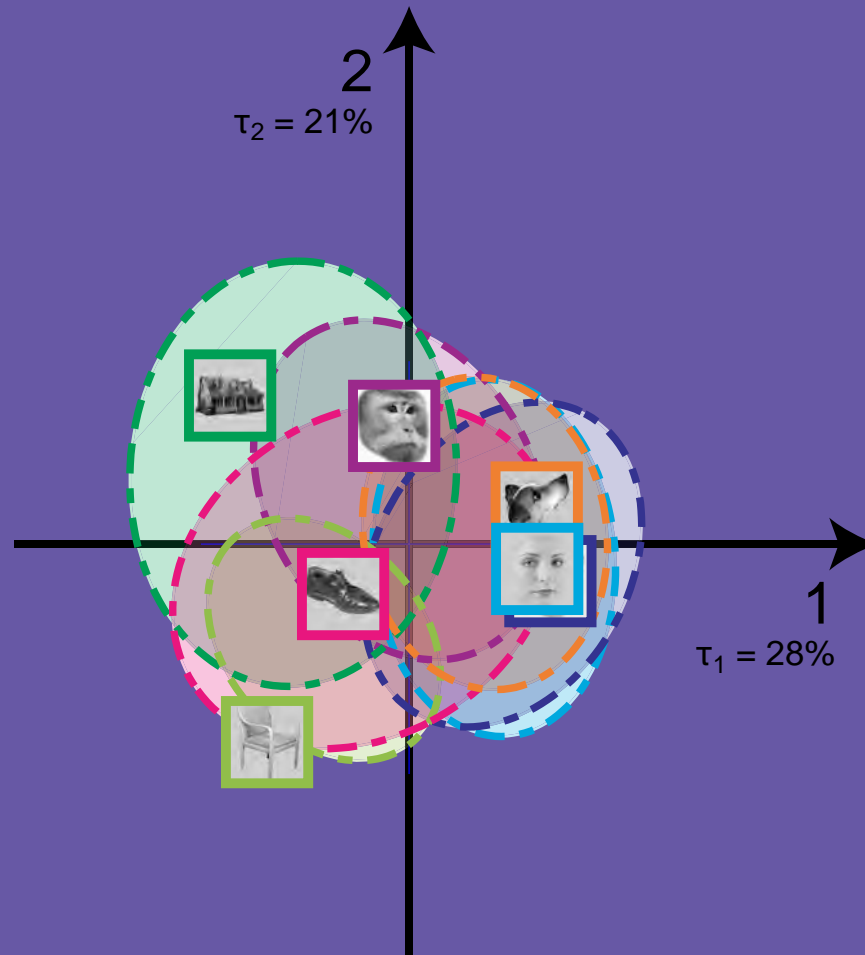
MULTI-TABLE: JACKKNIFE ...

PREDICTION: Do not use scans from the same block!

→ Jackknife the whole block

---

**THE DANGERS OF TIME CORRELATION**



All Rois: Prediction Intervals

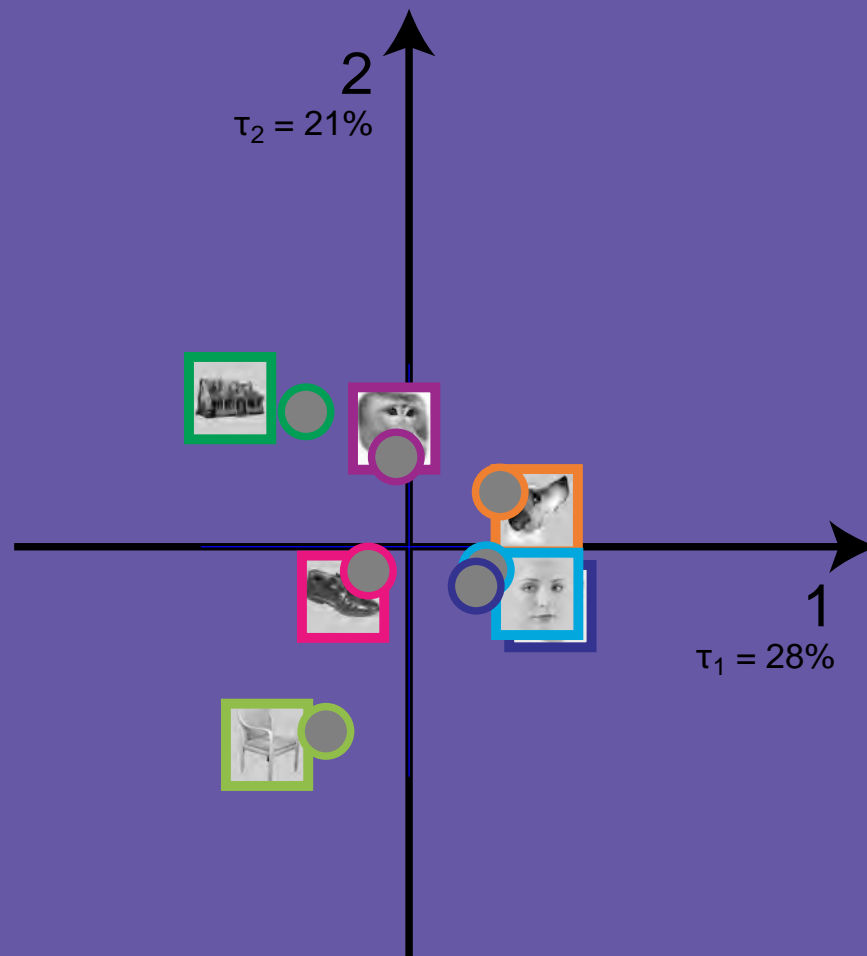
---

WHAT ABOUT THE ROIS?

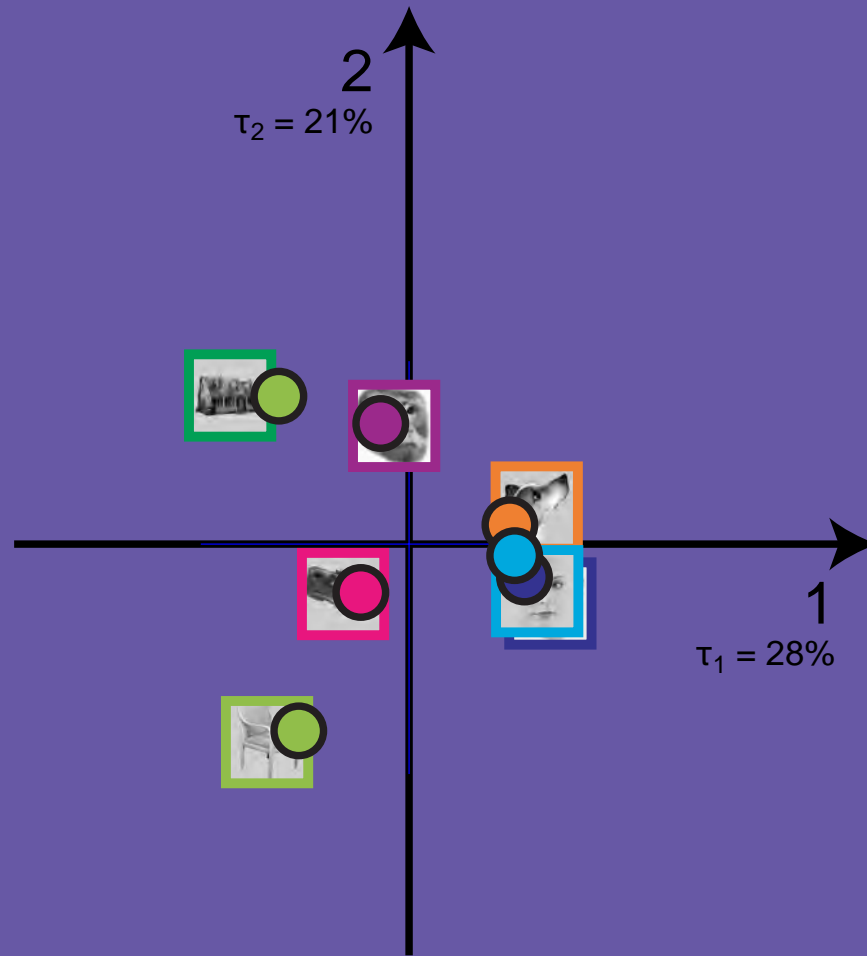
3 ROIS

---

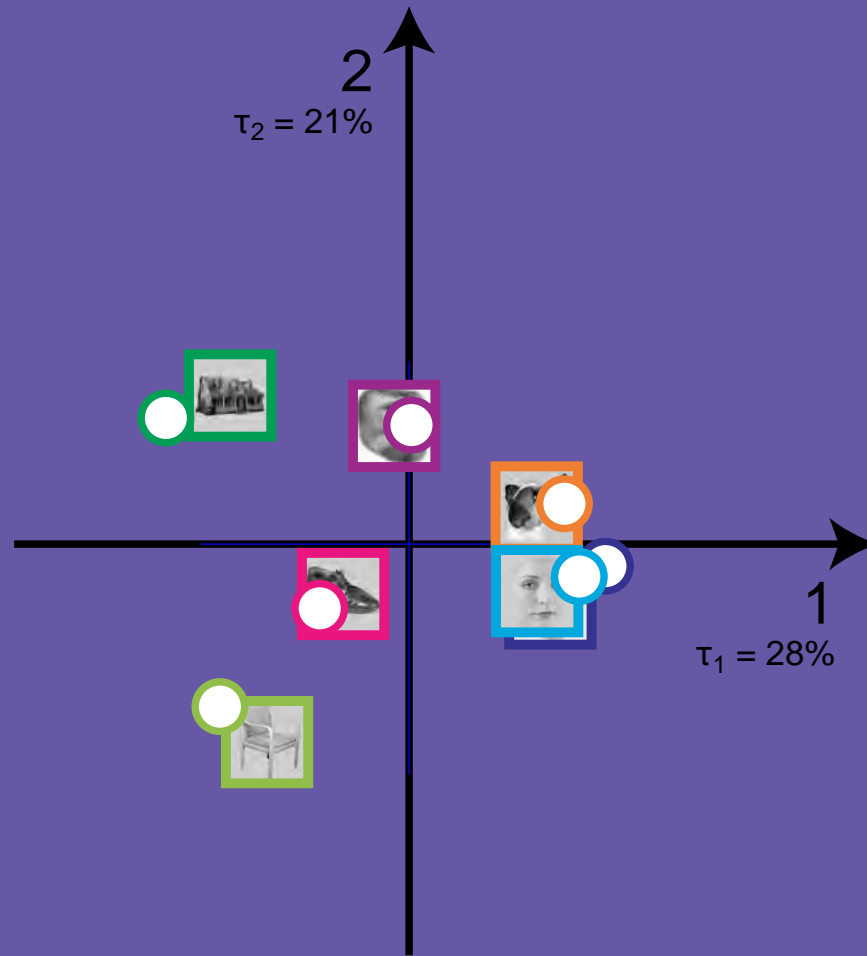
MO → IO → VT



Roi: Medio-Occipital (MO)



Roi: Inferior Occipital (IO)



Roi: Ventro Temporal (VT)

**THE BRAIN BECOMES  
MORE “SEMANTIC” AS WE GO  
DEEPER IN THE VENTRAL STREAM**

---

**FINALE VARIATION 2:  
BRAIN AND IMAGES:**

- Data from Denise Park

---

**VARIATION 3: CATEGORIZATION, BRAIN AND AGE**

## VARIATION 3:

---

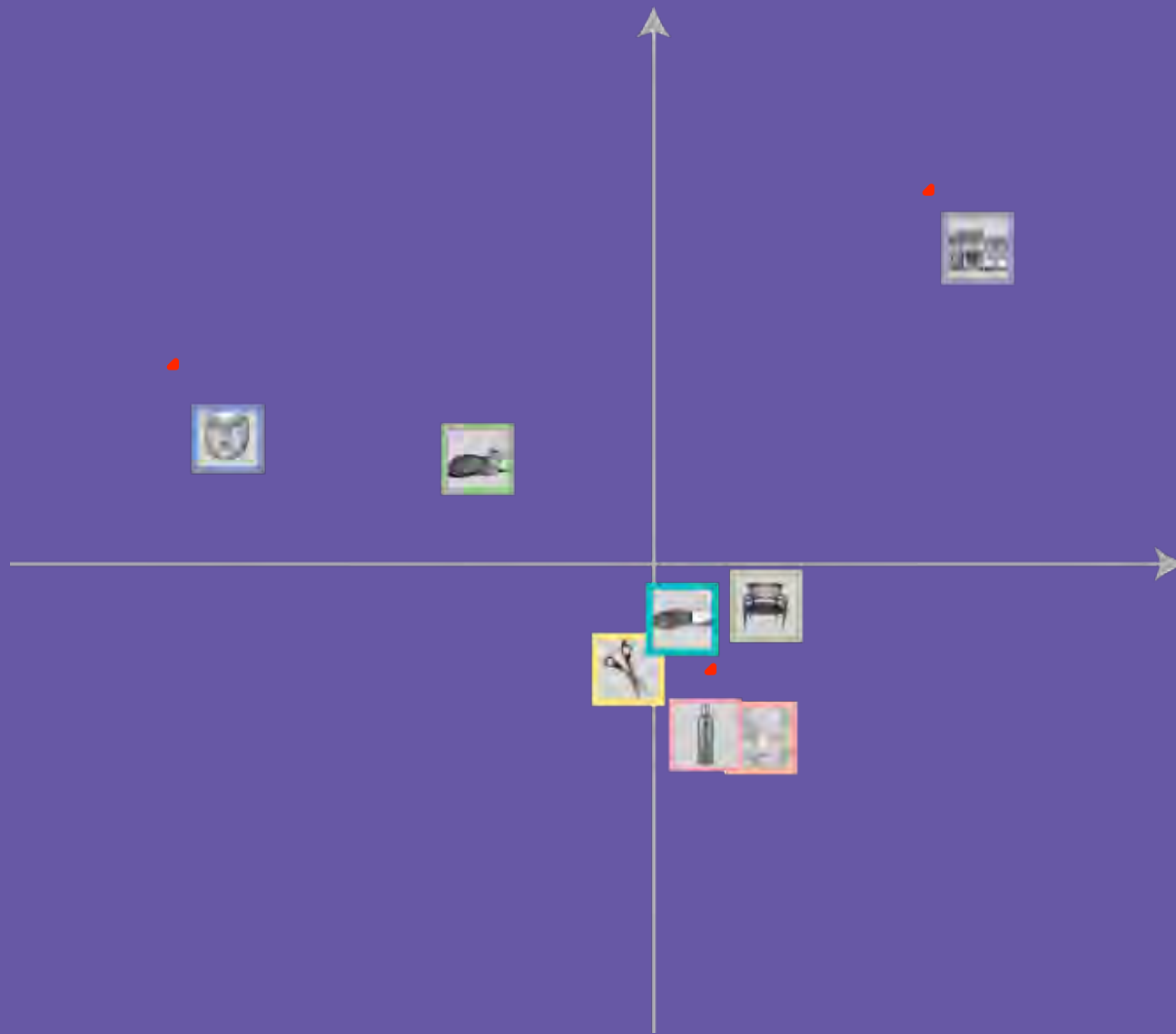
Flatter brain space as we mature?

QUESTION: DOES THE BRAIN CHANGES ITS  
CATEGORIZATION STRATEGY WITH AGE

---

Main idea:

Replicate Haxby (2001)  
with old and young participants



BACK TO HAXBY 2001, ABDI ET AL. (2009)  
PICK UP THREE CATEGORIES

- *f*MRI Brain Reading Experiment:
- GOAL:  
evaluate age effects on brain reading

---

DESIGN

- Passive viewing of Pictures

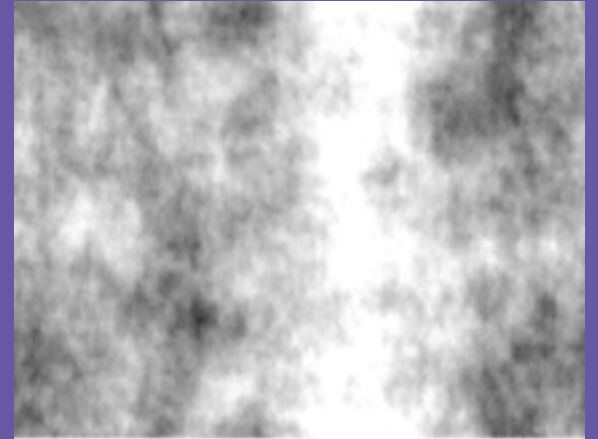
60 FACES : 30 Female & 30 Male

60 HOUSES : 30 Residential & 30 Apartment

60 SCRAMBLE

---

DESIGN: STIMULI



---

STIMULI

- One Run
- 4 blocks  $\times$  3 Categories = 12 Blocks
- Order of Pictures  
*randomized* for each participant

---

DESIGN

- 3.0T Siemens Allegra scanner

---

DESIGN: MATERIAL

# PARTICIPANTS

---

YOUNG

OLD

---

Male

Female

---

Male

Female

---



Young

Old

Men

50

41

91

Women

47

53

100

97

94

191

---

DESIGN: PARTICIPANTS

- 180 Pictures into  $2+2+1 = 5$  categories
  - **60 Faces**
    - 30 male & 30 female faces
  - **60 Houses**
    - 30 multiple & single houses
  - **60 Scramble pictures**
- 191 Participants into  $2 \times 2 = 4$  categories
  - Young and Old participants
  - Male and Female participants

---

**DESIGN: RECAP**

- **Anatomical ROIs.**

ventral visual cortex including (usual suspects):  
fusiform, inferior temporal,  
lingual, parahippocampal,  
and occipital regions

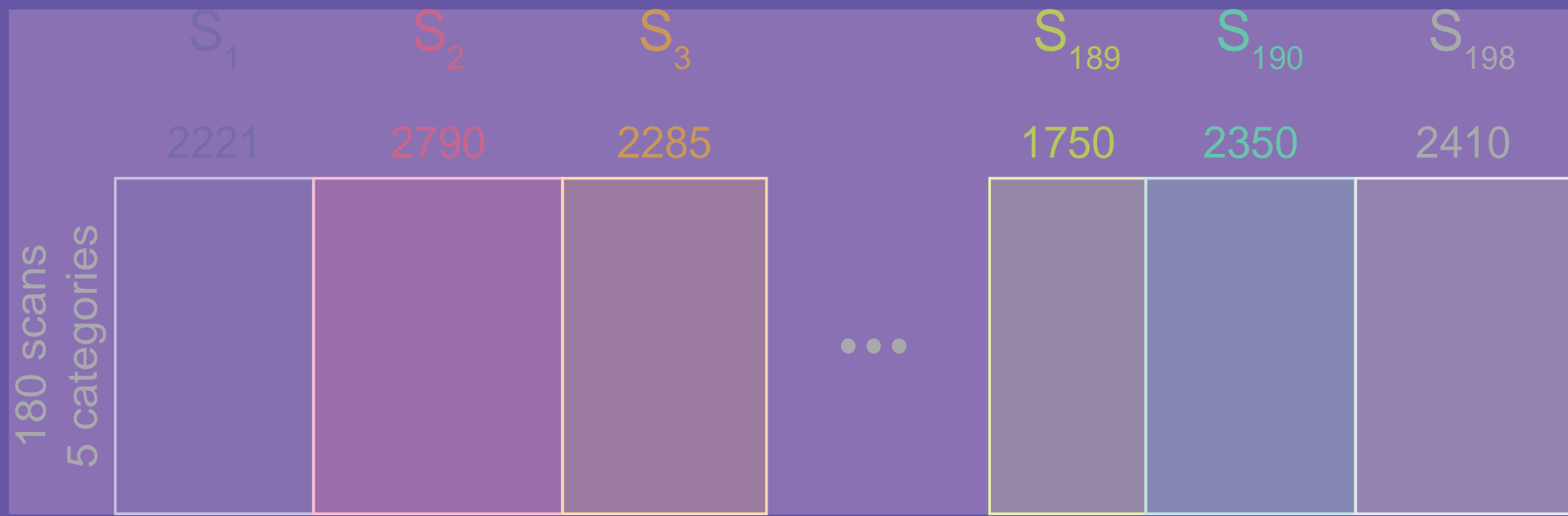
---

**USUAL PREPROCESSING +**

- 180 rows
- 191 Blocks: One Block = One Participant  
anatomical ROIs  
implies different # of voxels per participant
- Total number of voxels = 264,395

---

**METHOD: MUBADA**  
**(MULTIBLOCK BARYCENTRIC DISCRIMINANT ANALYSIS)**

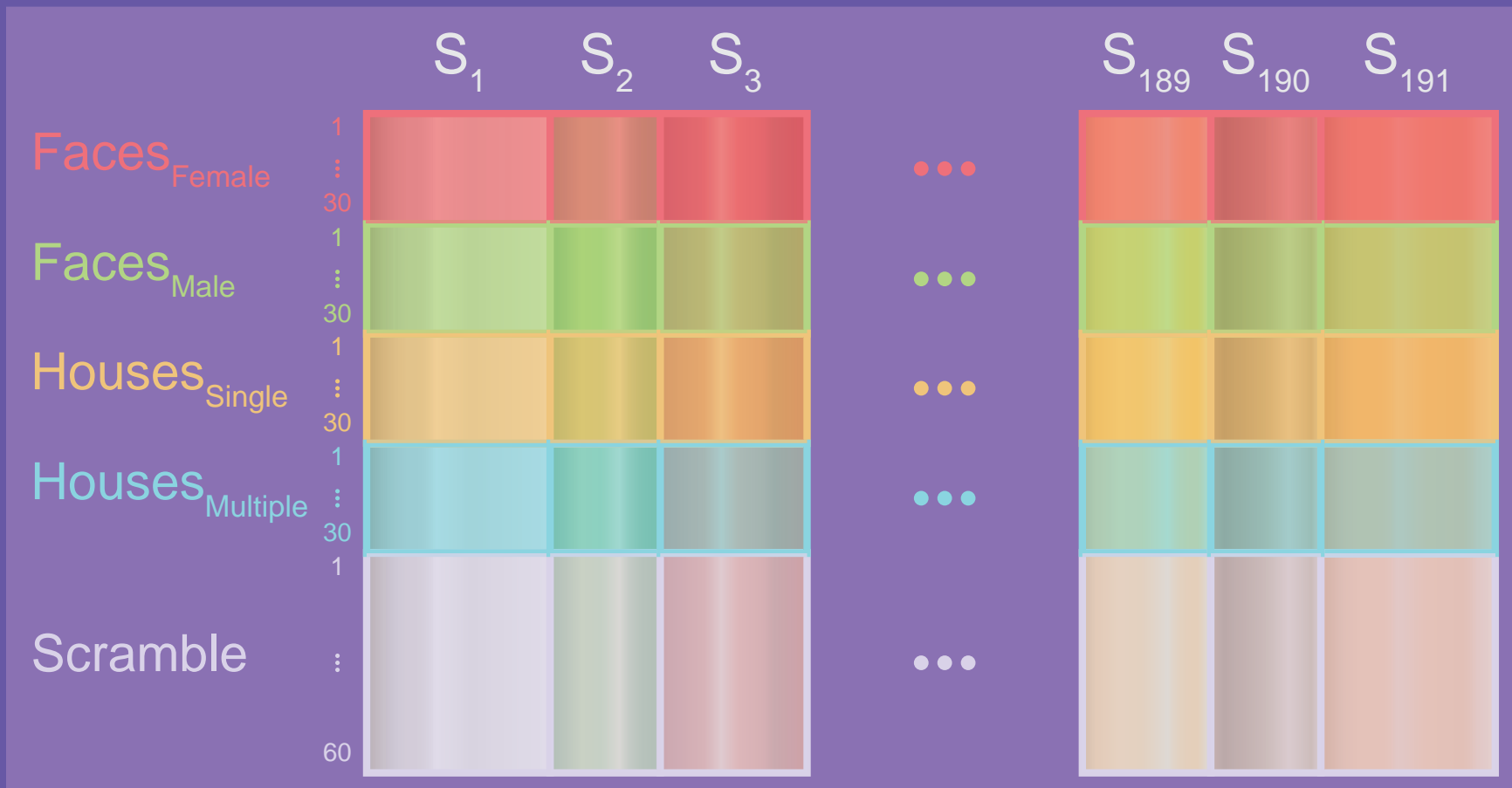


Total # of Voxels

$$2221 + 2790 + \dots + 2350 + 2410 = 506,375$$

---

180 SCANS FROM 5 CATEGORIES  
191 PARTICIPANTS (97 YOUNG, 94 OLDS)



# DATA STRUCTURE

- Block normalization:  
Do a PCA of each block  
equalize the first component  
(singular value normalization, kind of Z-score)

---

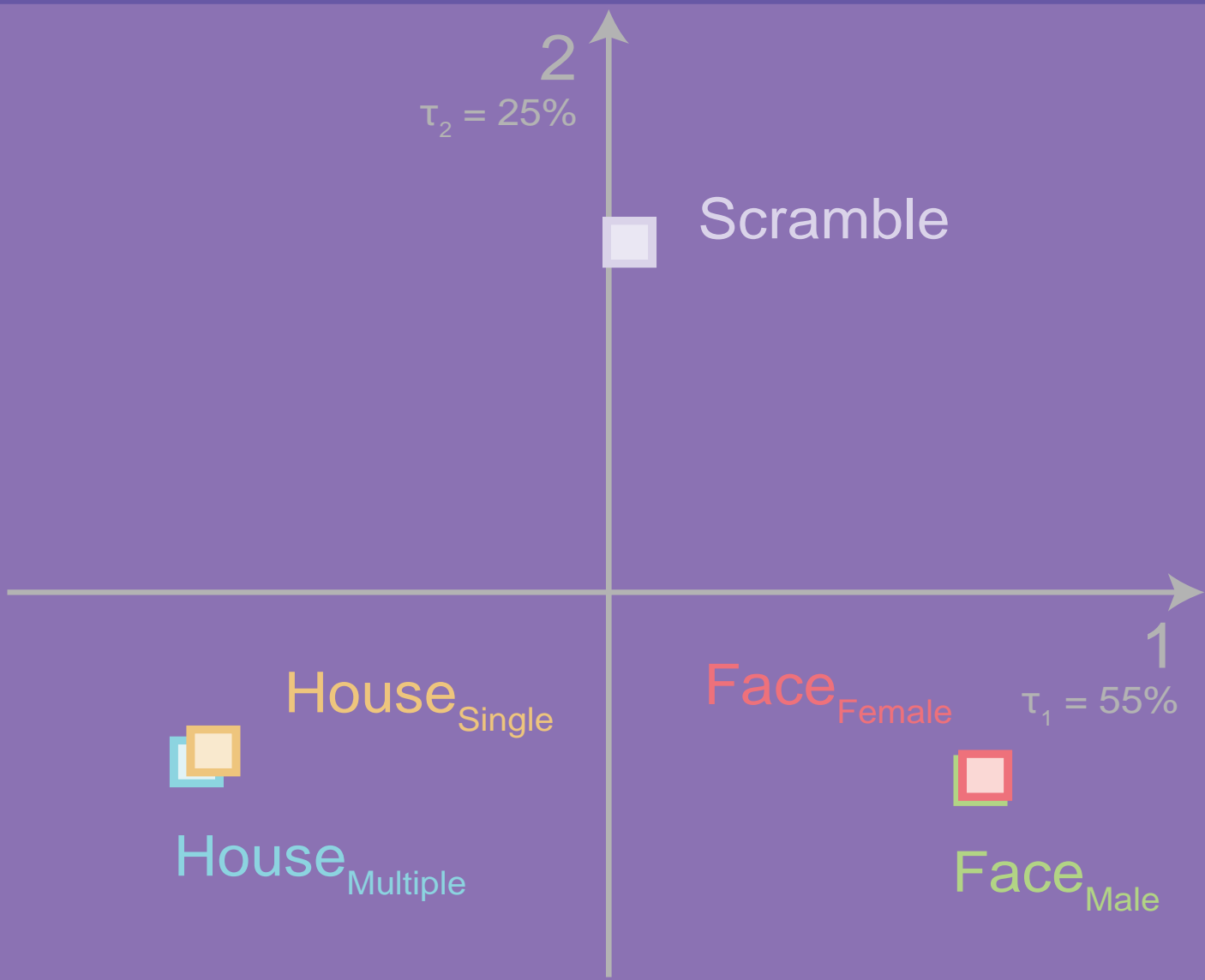
**PROBLEM OF DIFFERENT VARIANCE PER SUBJECT**

---

**RUN A BARYCENTRIC DISCRIMINANT ANALYSIS  
(BADA)**

---

RESULTS FROM MULTI-TABLE



# FIXED EFFECT MODEL

CONFUSION MATRICE  
TOLERANCE ELLIPSOIDS

# RANDOM EFFECT MODEL

CONFUSION MATRICE  
PREDICTION ELLIPSOIDS  
CONFIDENCE ELLIPSOIDS

---

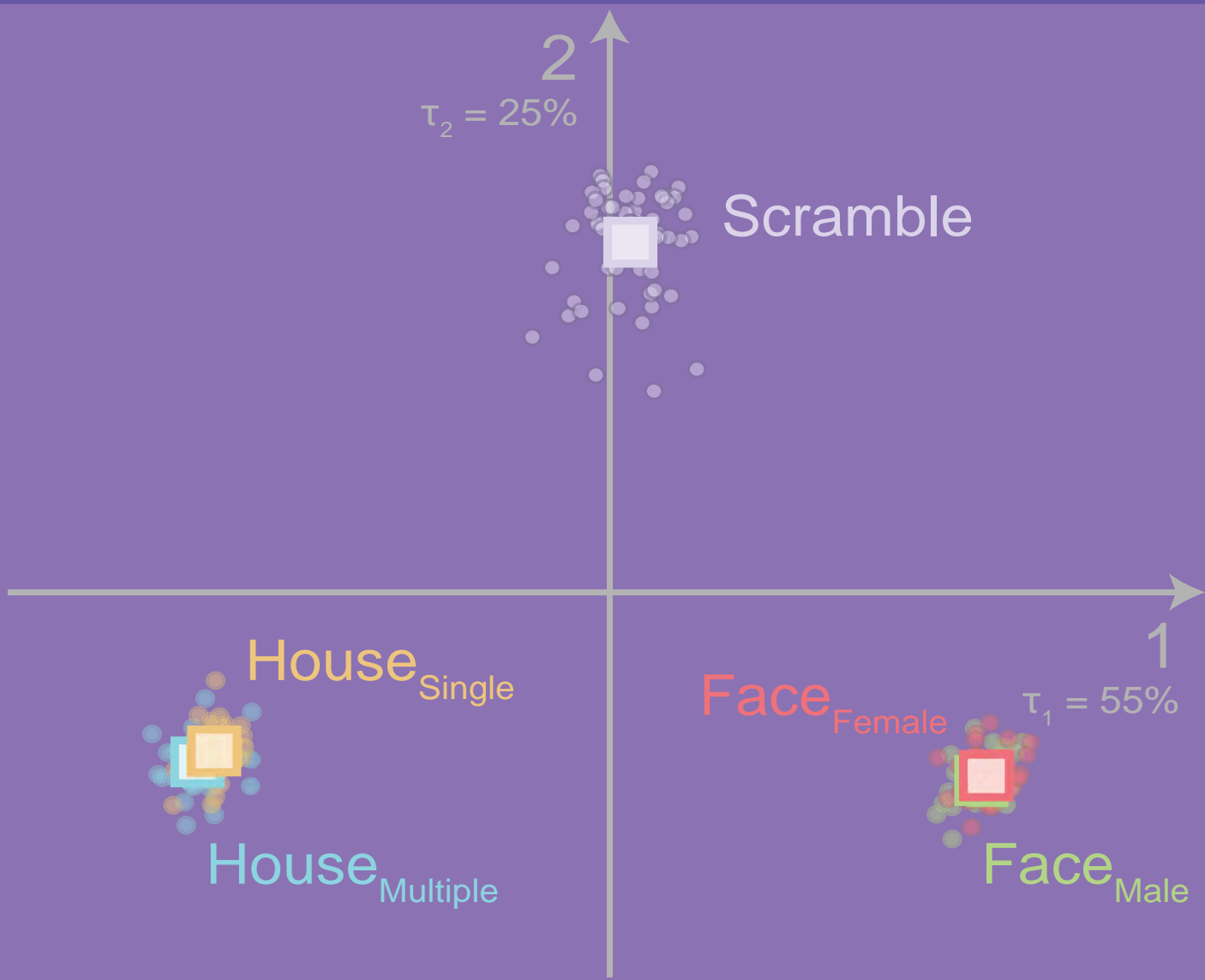
RESULTS: HOW GOOD IS THE MODEL?

# FIXED EFFECT MODEL

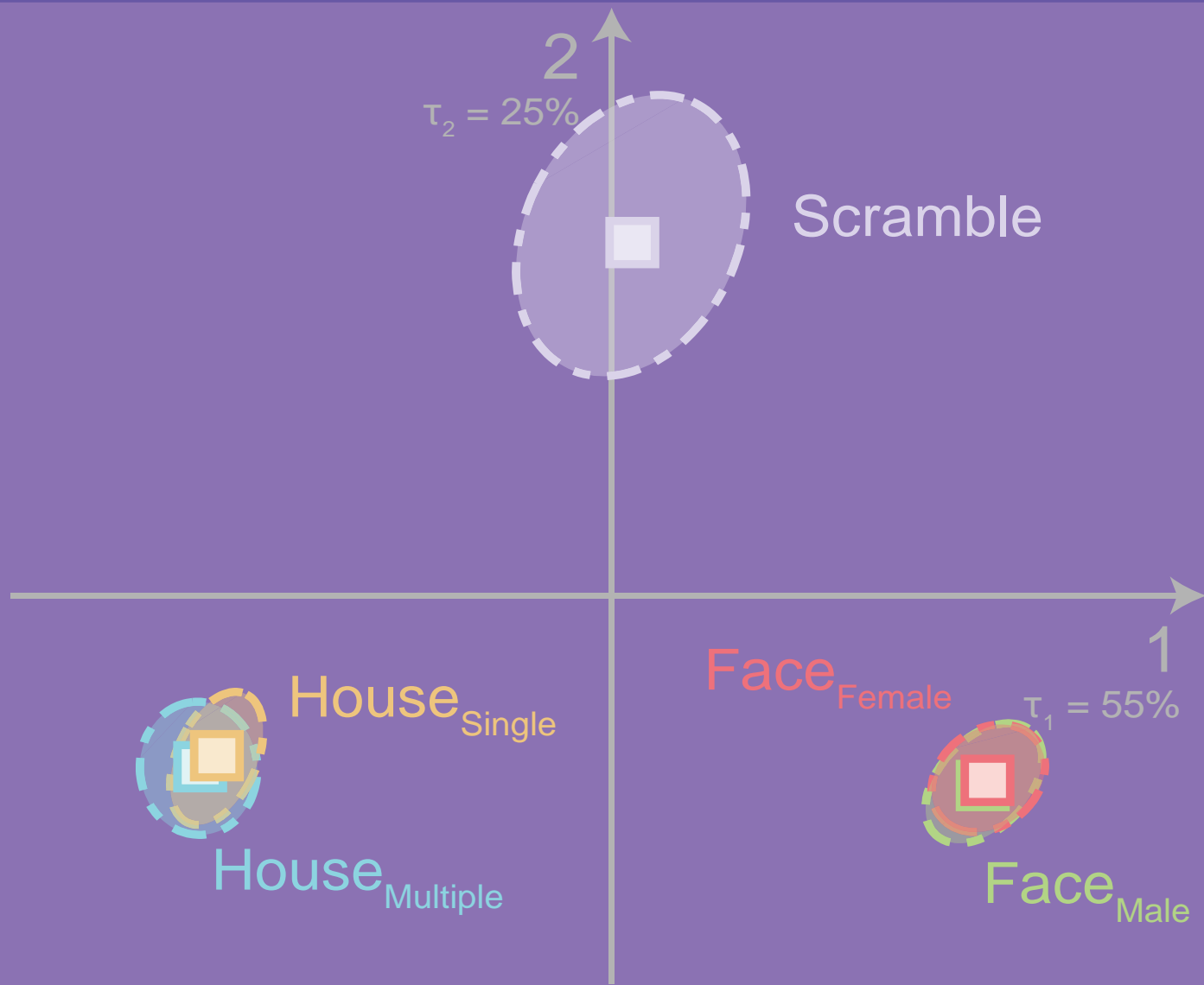
CONFUSION MATRICE  
TOLERANCE ELLIPSOIDS

---

RESULTS: HOW GOOD IS THE MODEL?



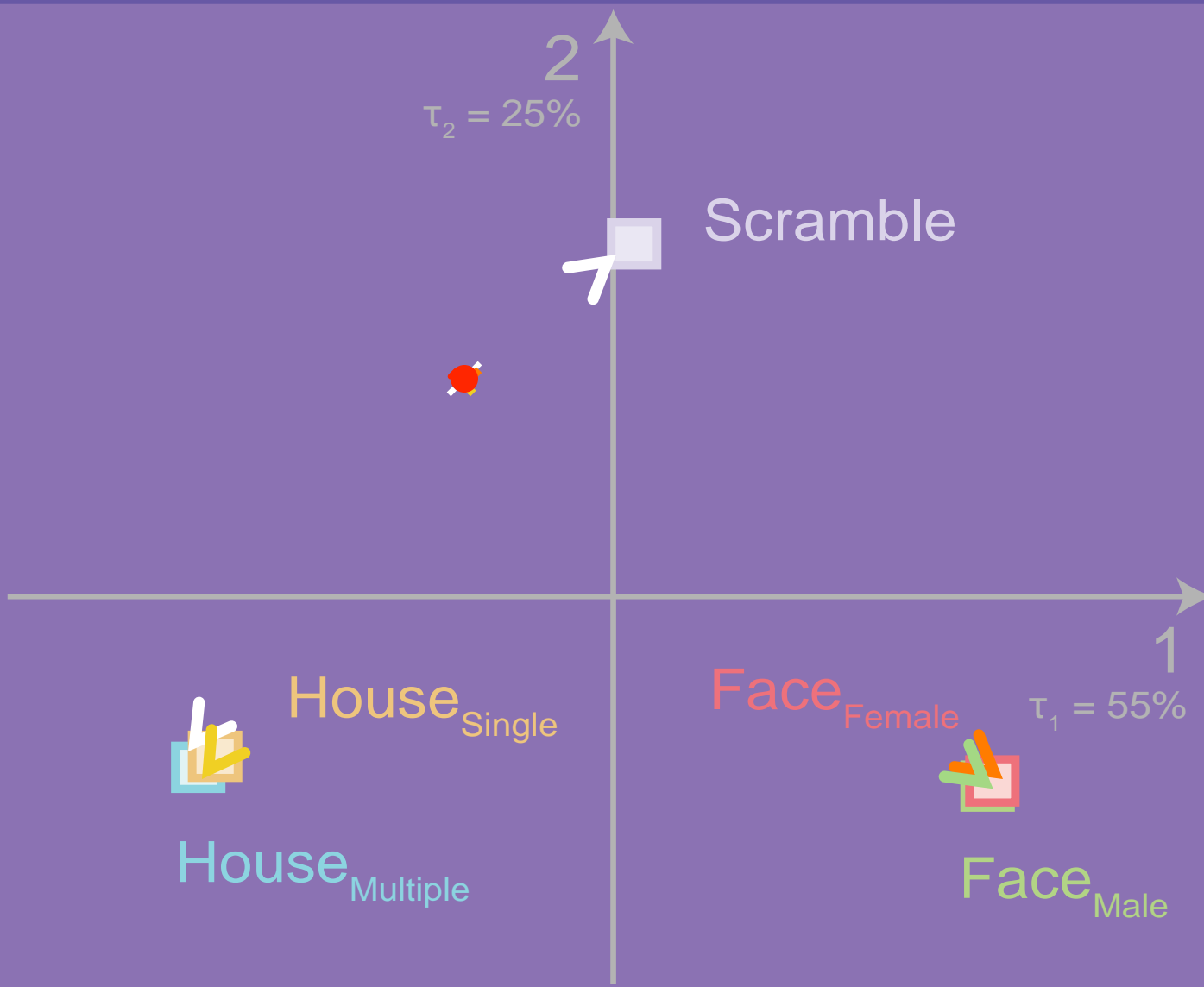
ONE DOT = ONE PICTURE



**95% TOLERANCE ELLIPSES**  
**(95% OF THE SCANS ARE IN THE ELLIPSE)**

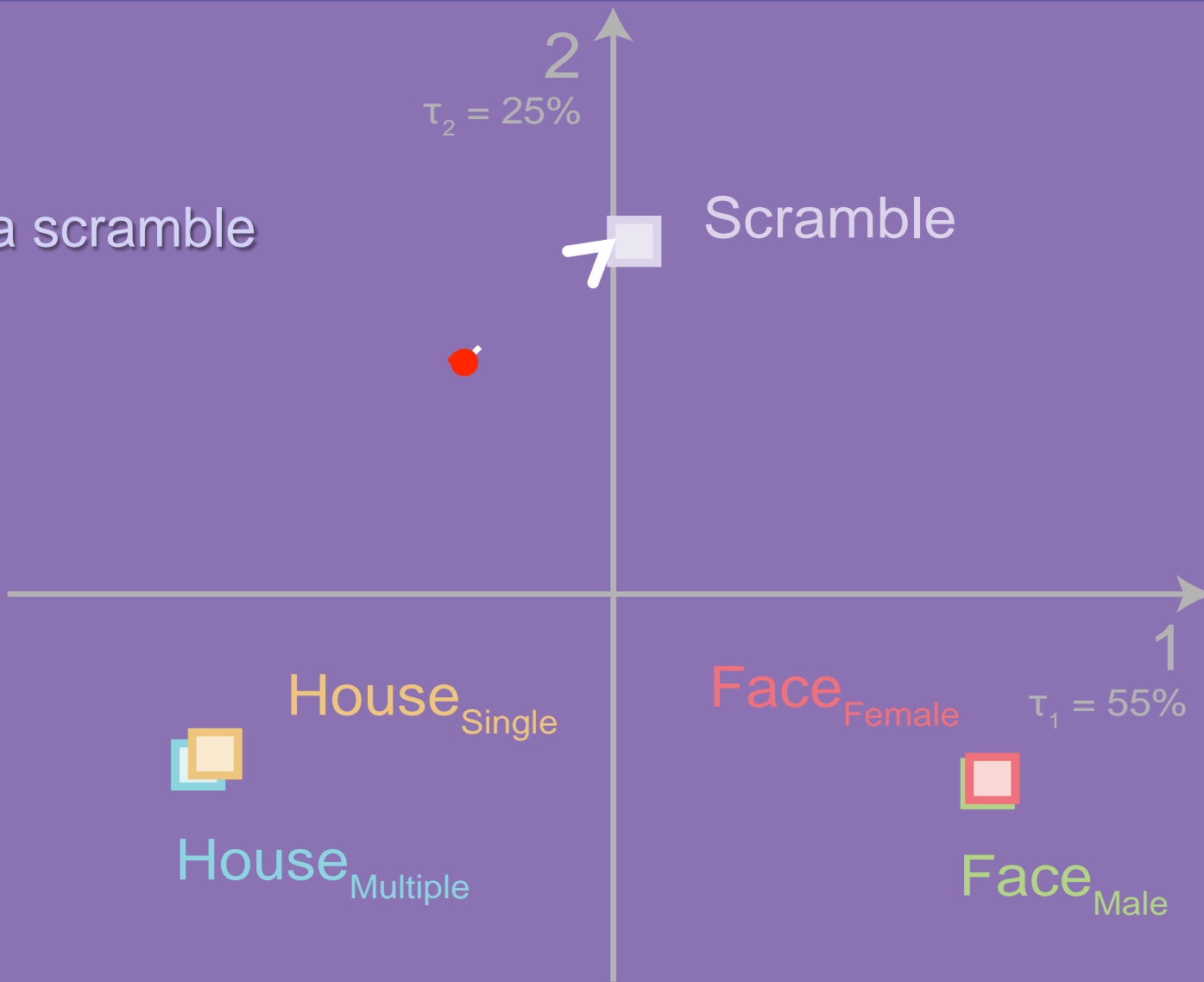
---

# HOW TO CLASSIFY OBSERVATIONS (WHAT CATEGORY OF PICTURE WAS WATCHED)



# ASSIGNING SCANS TO CATEGORIES

● Is a scramble



## ASSIGNING SCANS TO CATEGORIES

## Fixed Effect Model

### Actual Classification

		F-m	F-f	H-b	H-s	Scr
Predicted Classification	F-m					
	F-f					
	H-b					
	H-s					
	Scr					

---

**BARYCENTRIC DISCRIMINANT ANALYSIS**

## Fixed Effect Model

### Actual Classification

Predicted Classification		Actual Classification				
		F-m	F-f	H-b	H-s	Scr
F-m	30	0	0	0	0	
F-f	0	30	0	0	0	
H-b	0	0	30	0	0	
H-s	0	0	0	30	5	
Scr	0	0	0	0	60	

180 = 100%

# BARYCENTRIC DISCRIMINANT ANALYSIS

# RANDOM EFFECT MODEL

## Use Jackknife + Bootstrap

CONFUSION MATRICE  
PREDICTION ELLIPSOIDS  
CONFIDENCE ELLIPSOIDS

---

RESULTS: HOW GOOD IS THE MODEL?

---

JACKKNIFE (LEAVE ONE OUT: LOO)

I-1



K



J



?



BADA: JACKKNIFE... ONE ROW AT A TIME

## Random Effect Model Actual Classification

Predicted Classification		Actual Classification				
		F-m	F-f	H-b	H-s	Scr
F-m	<i>13</i>	14	0	0	0	
F-f	17	<i>16</i>	0	0	0	
H-b	0	0	<i>13</i>	17	0	
H-s	0	0	17	<i>13</i>	0	
Scr	0	0	0	0	<i>60</i>	

115 = 64%

# BARYCENTRIC DISCRIMINANT ANALYSIS

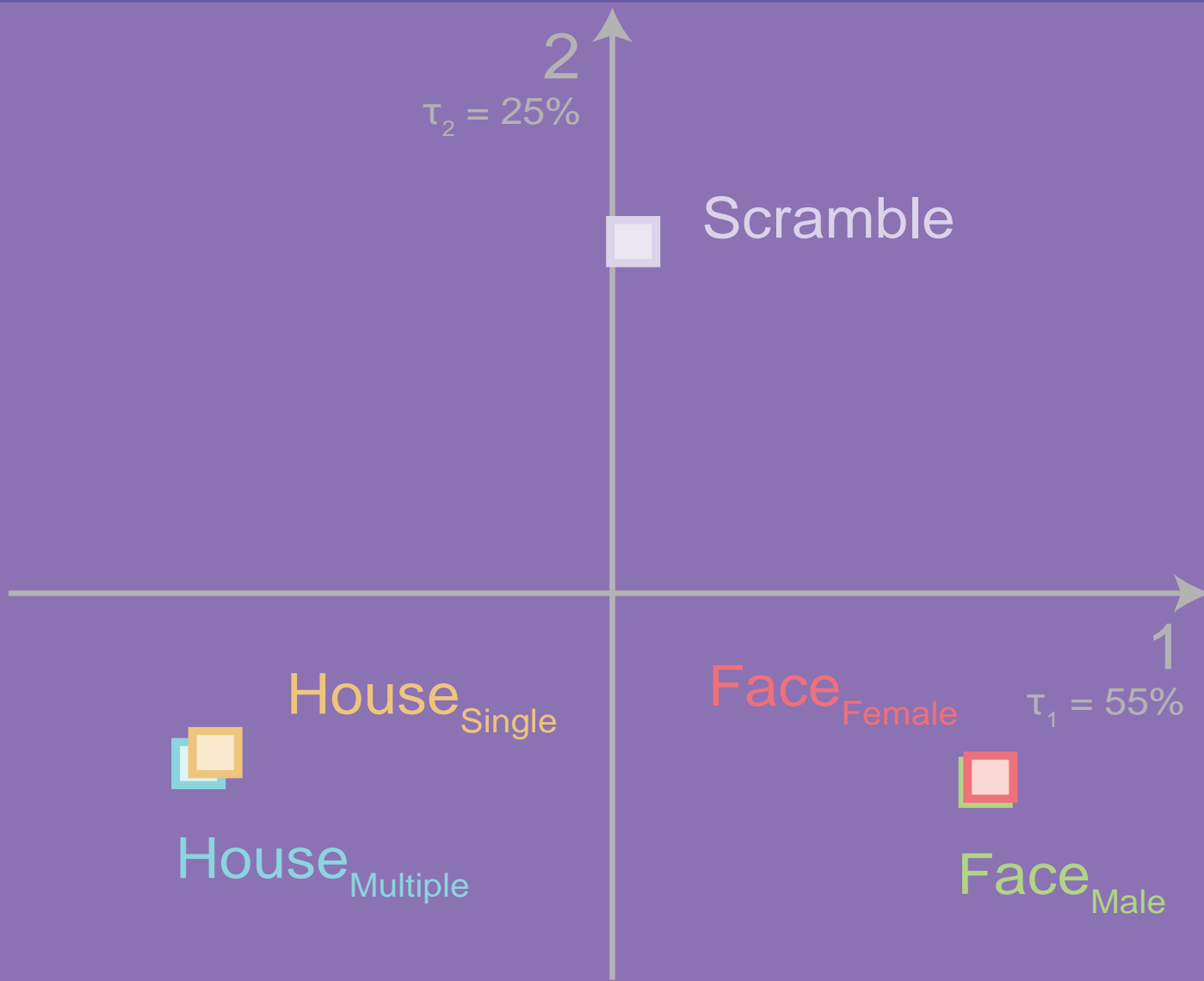
## Random Effect Model

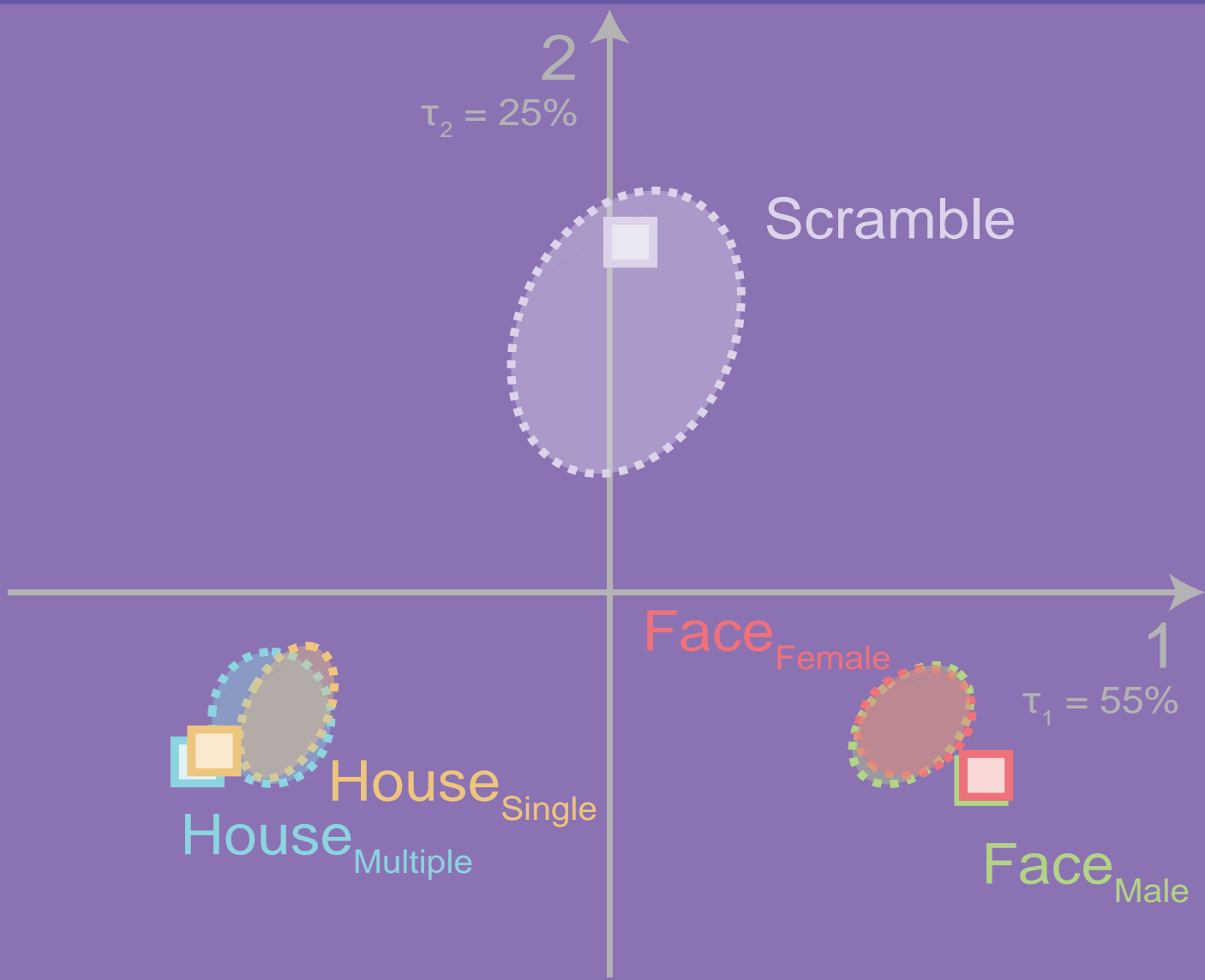
### Actual Classification

		Actual Classification				
		F-m	F-f	H-b	H-s	Scr
Predicted Classification	F-m	13	14	0	0	0
	F-f	17	16	0	0	0
	H-b	0	0	13	17	0
	H-s	0	0	17	13	0
	Scr	0	0	0	0	60

115 = 64%

## BARYCENTRIC DISCRIMINANT ANALYSIS





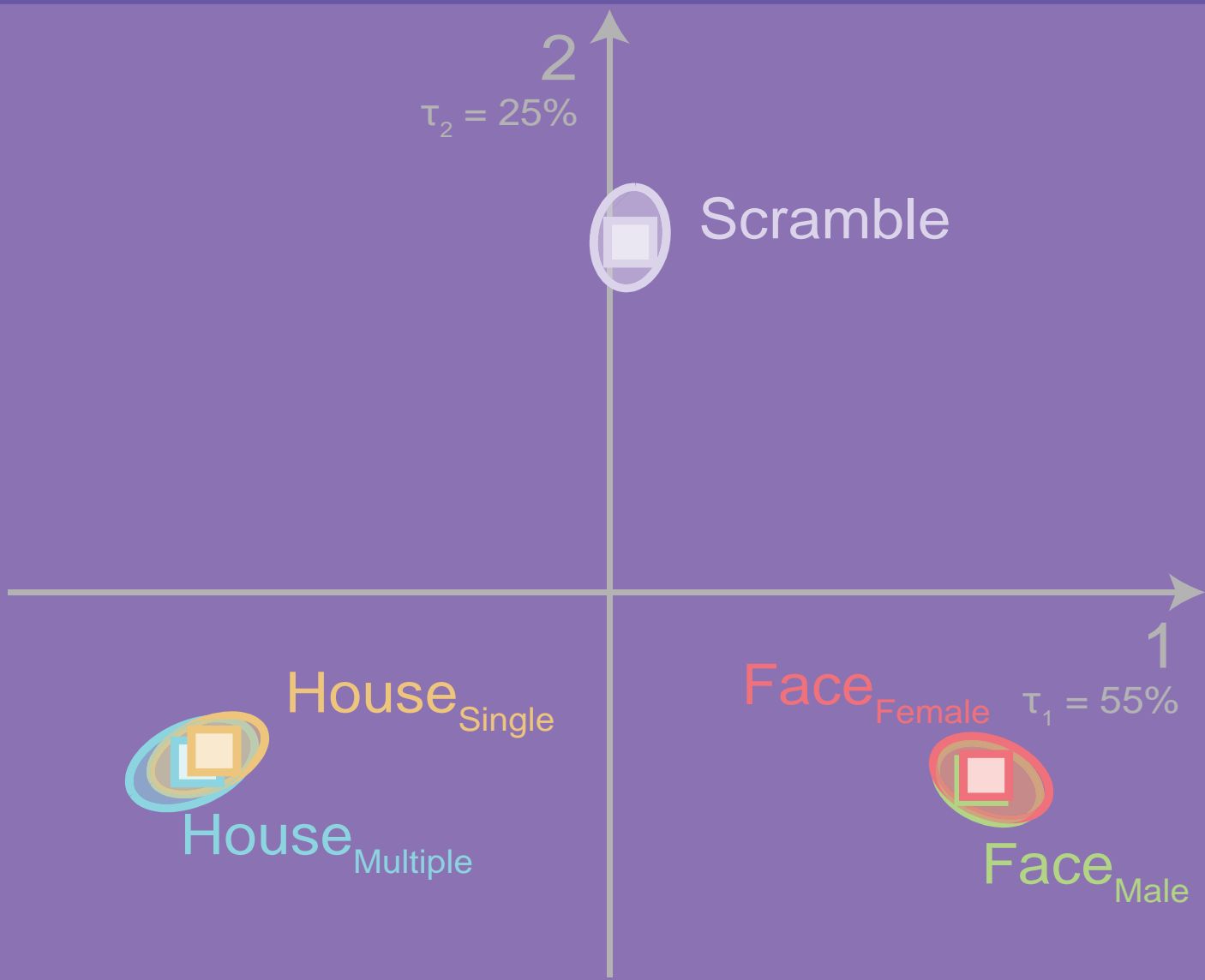
# PREDICTION ELLIPSES

- Redo the analysis 10,000 times with resampling (bootstrap) the participants and the scans (participants and scans are random)

Project and compute ellipsoids:  
Confidence ellipsoids

---

**HOW STABLE IS THE SOLUTION  
IS THE EARTH ROUND  $P < .05$**



95%

BOOTSTRAP CONFIDENCE INTERVALS

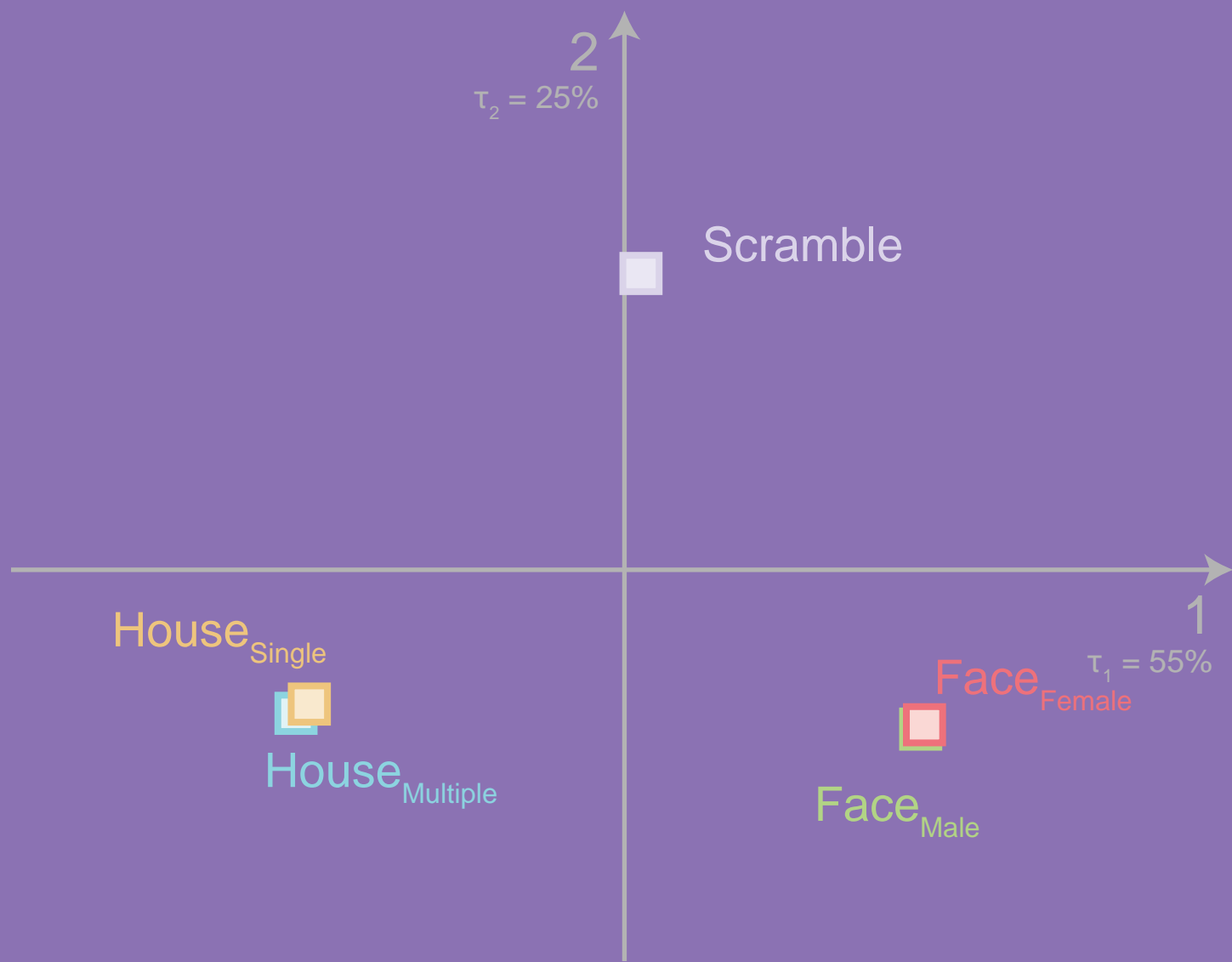
- Look at differences between old & Young

Block projection

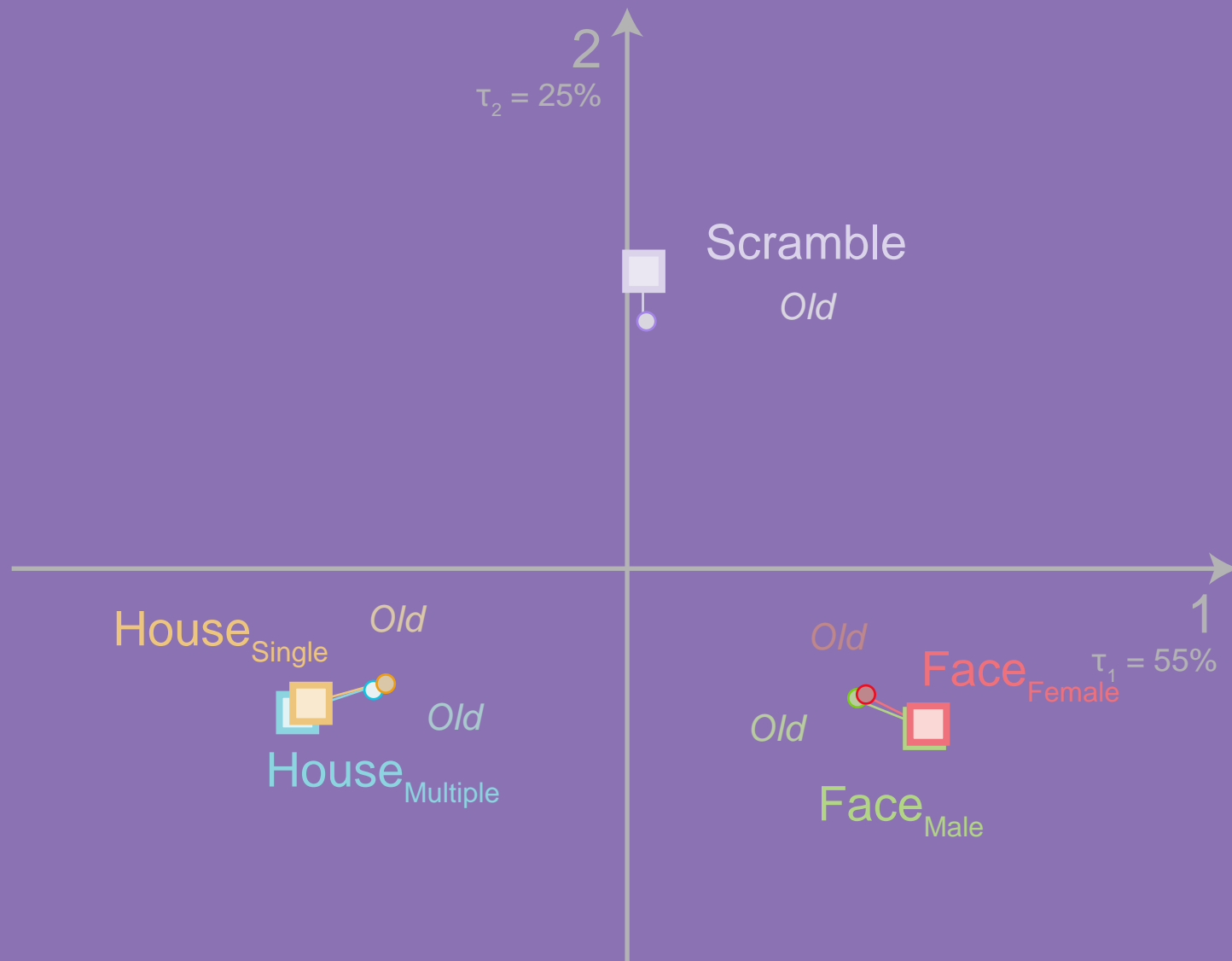
- Dedifferentiation hypothesis prediction:  
Youngs more distinctive than Olds

---

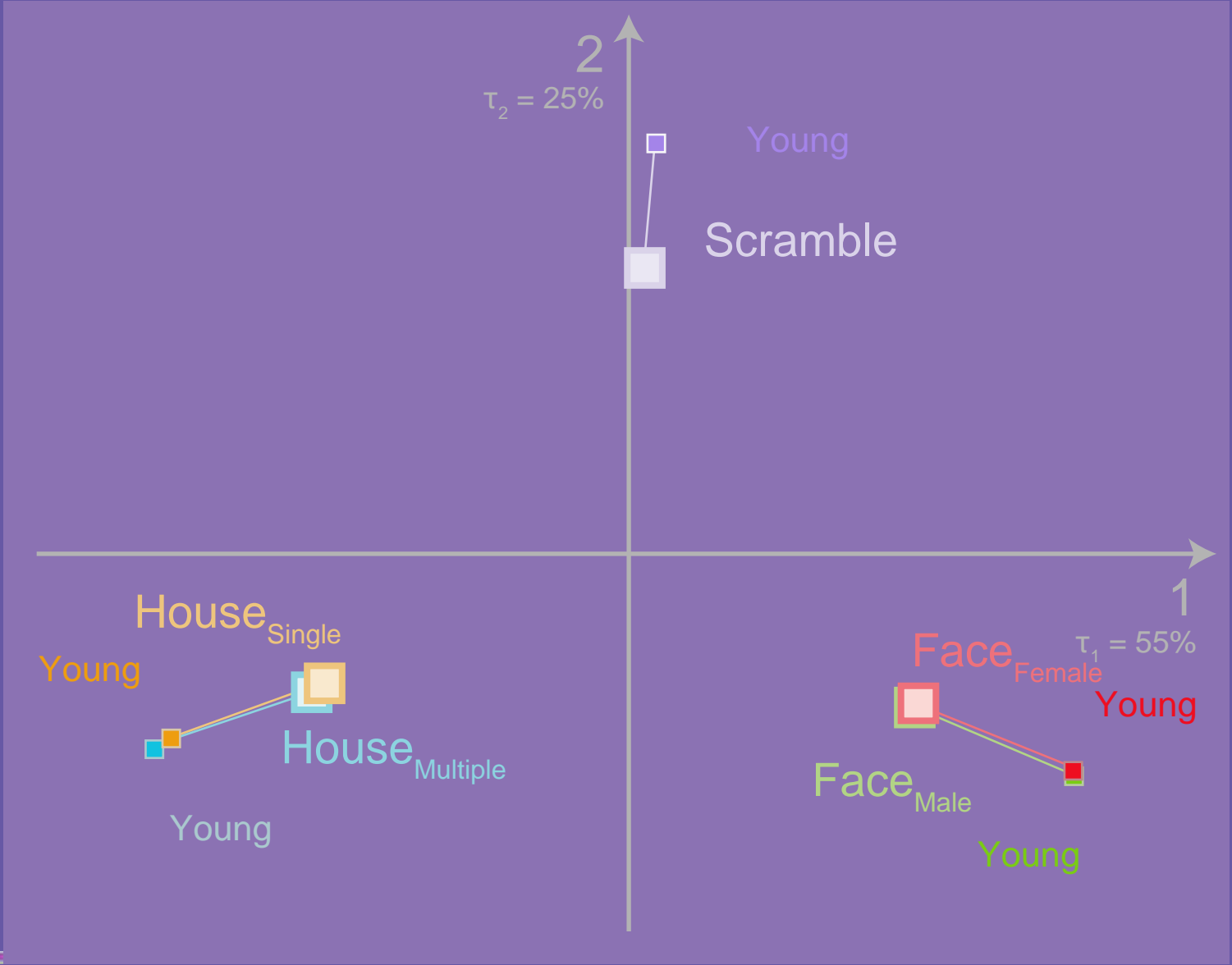
**OLD AND YOUNG: 97 YOUNG, 94 OLD**



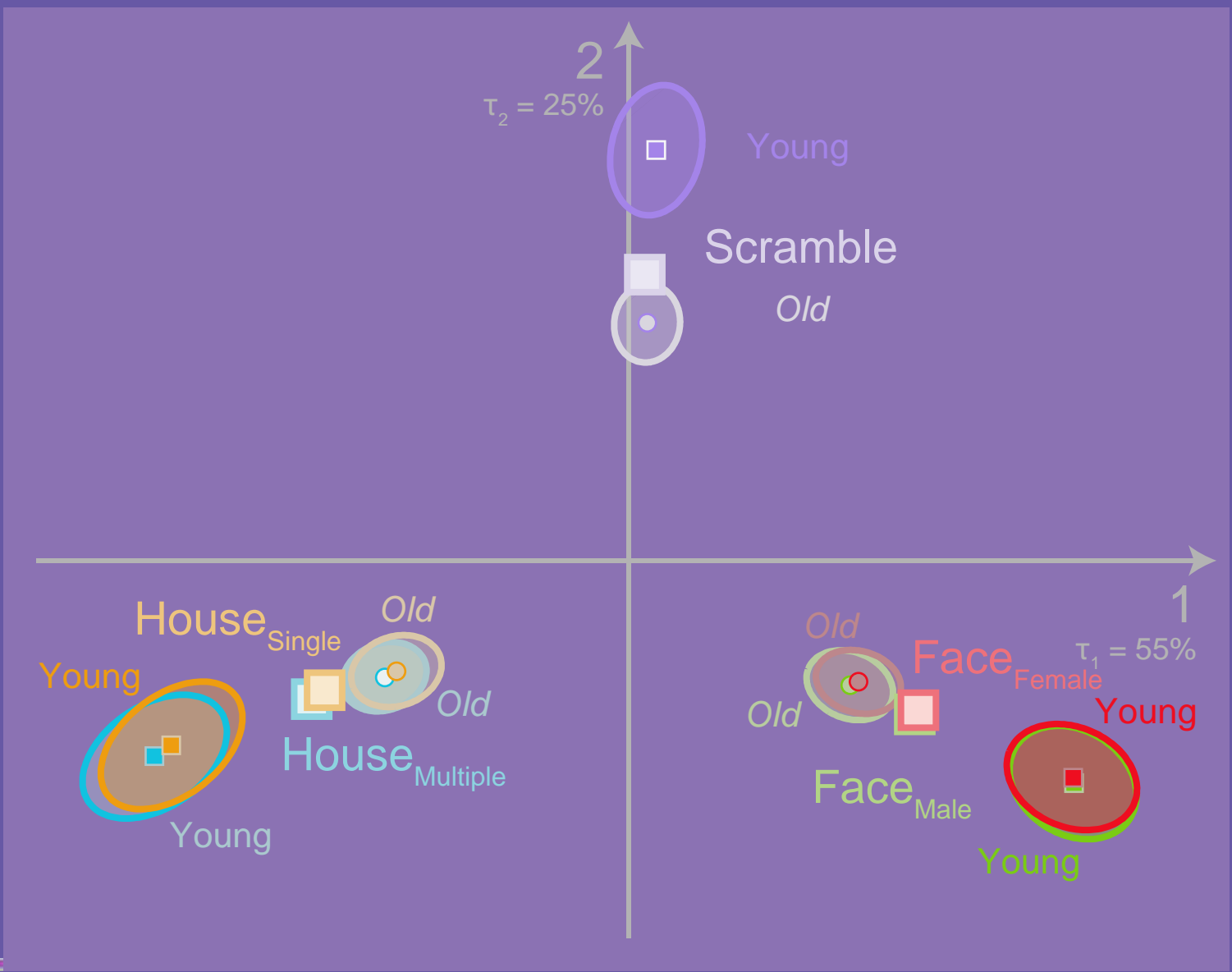
## BLOCK PROJECTIONS: BARYCENTERS



## BLOCK PROJECTIONS: BARYCENTERS



# BLOCK PROJECTIONS: BARYCENTERS



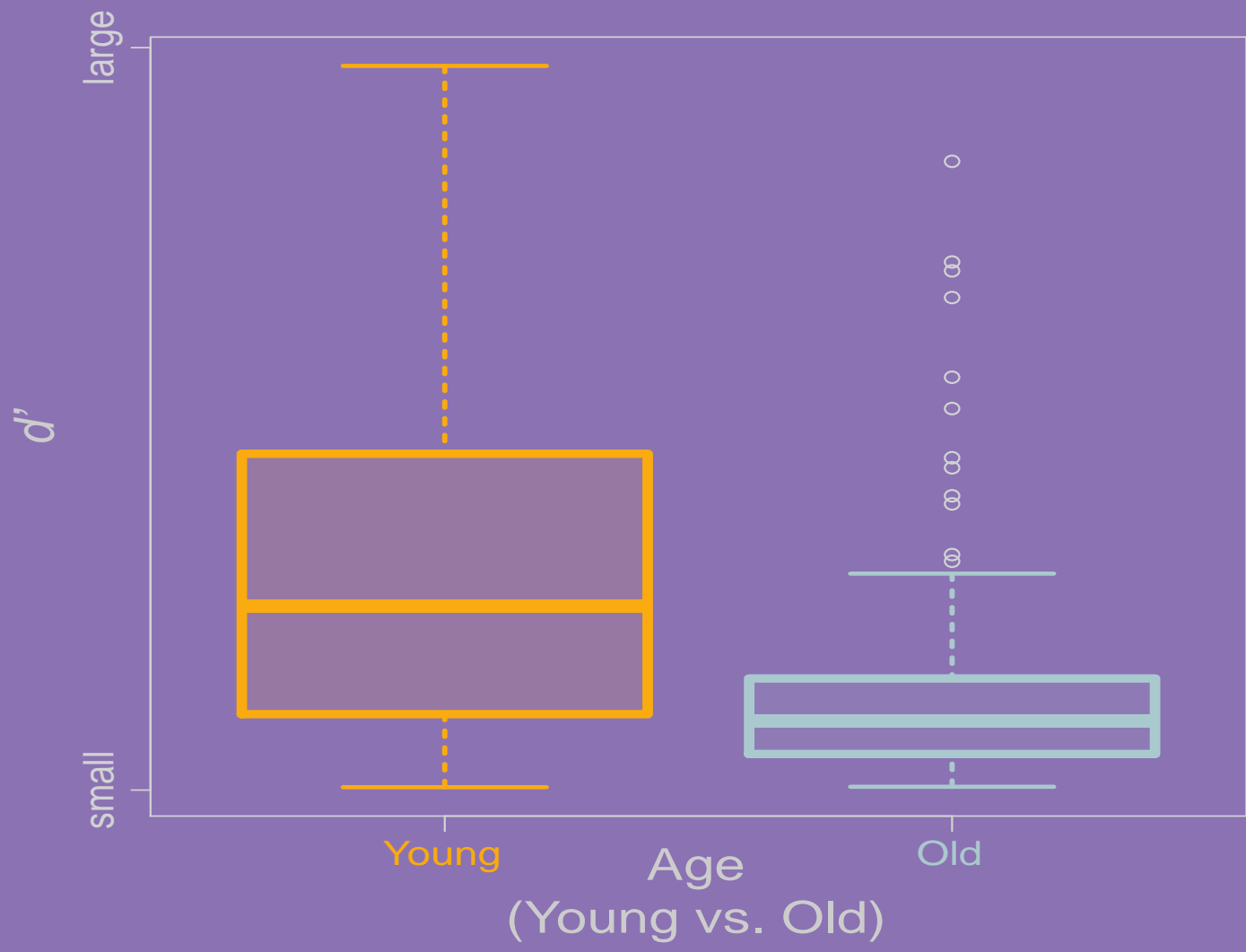
**BLOCK PROJECTIONS: BARYCENTERS  
 OLD  $\neq$  YOUNG ( $P < .01$ )**

Is the brain less efficient?

Less able to *differentiate* between categories?

---

WHY?



- Older participants are less efficient.
- ***WHY?***

---

MEASURING EFFICIENCY?

- Sphericity:  
A measure of coding efficiency?

---

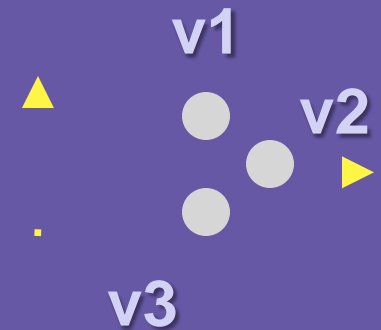
SPHERICITY STORY

---

BUT WHAT IS *“SPHERICITY”*?



## Principal Component Analysis PCA



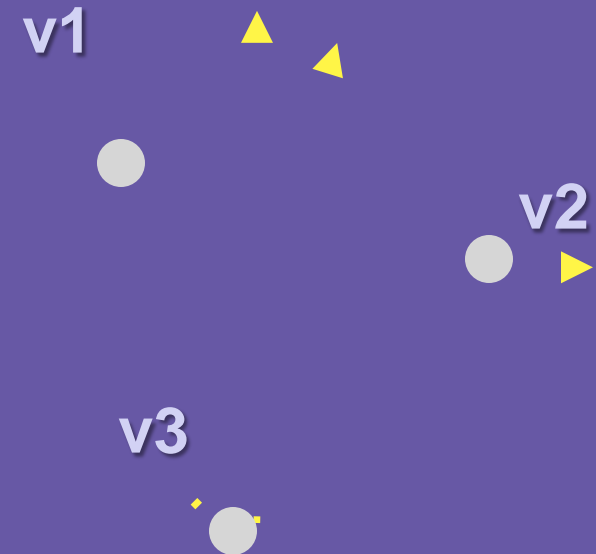
**Very flat space!**

---

**LACK OF SPHERICITY: INEFFICIENT CODE**



# Principal Component Analysis PCA

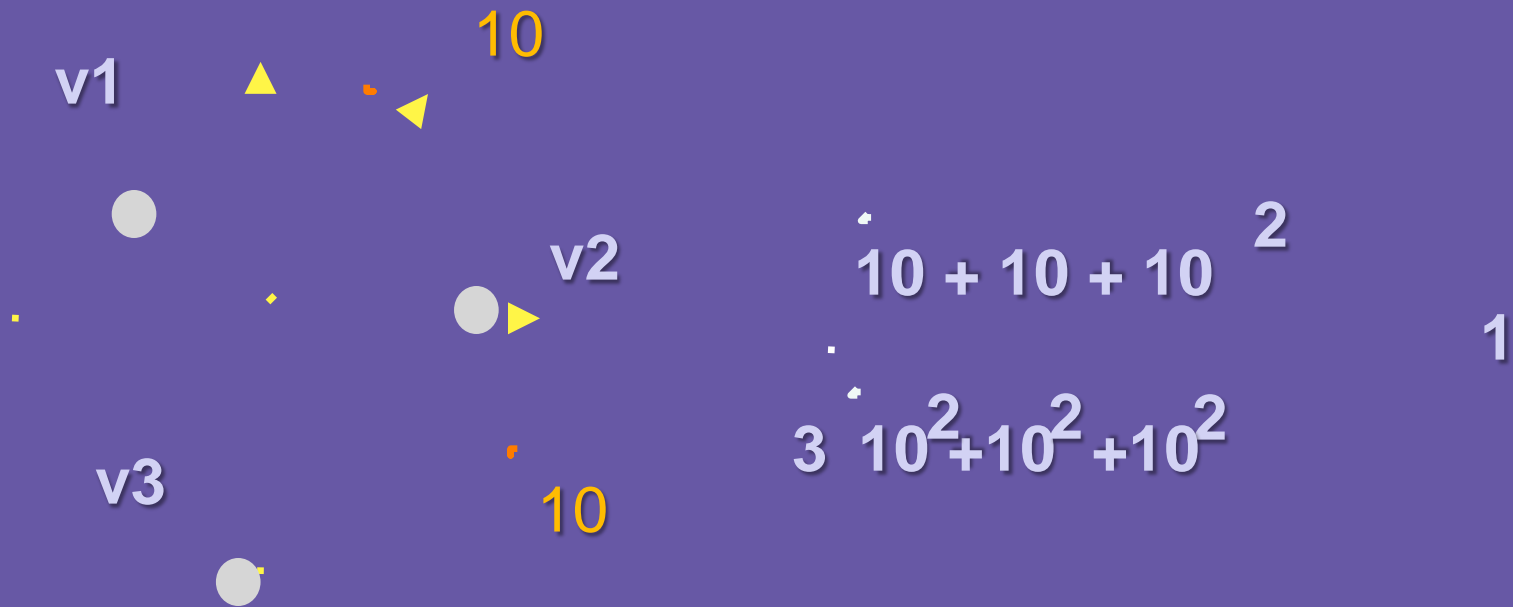


**Very Spherical space!**

---

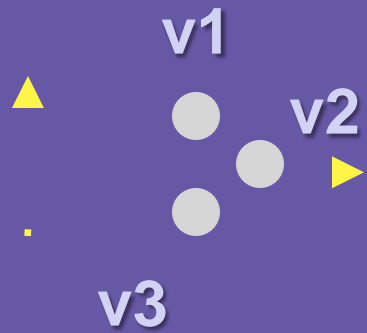
**SPHERICITY: EFFICIENT CODE**

- One number



---

**SPHERICITY = 1 (MAX)**



$$\begin{aligned}
 & 10 + 1^2 \\
 & 3 \cdot 10^2 + 1^2 \\
 & .4
 \end{aligned}$$

FLATTER = .4

- One number gets the pattern.

v1



v2



v3



1.0

v1



v2



v3



0.4

SPHERICITY GOES FROM 1 TO 0

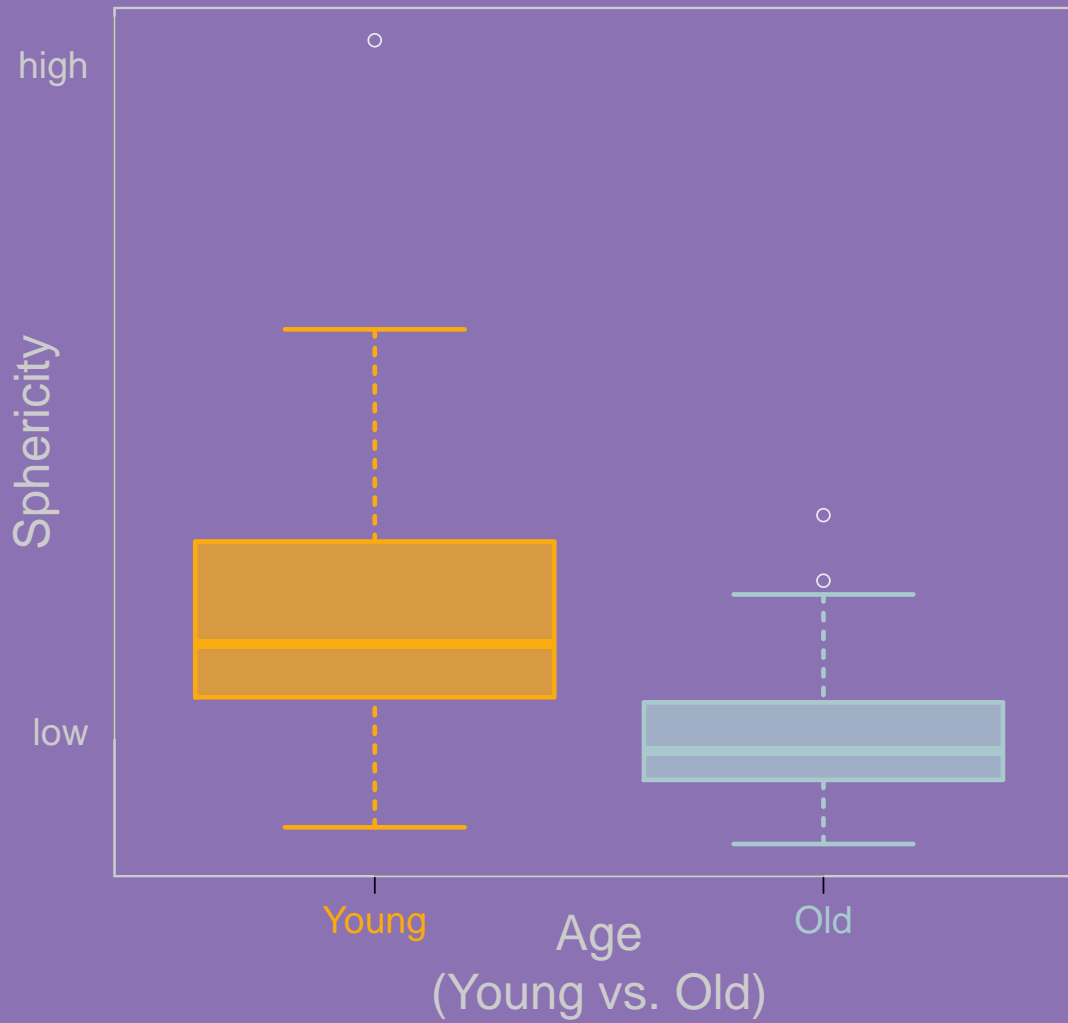
- Efficient (differentiated) code: Spherical
- Inefficient code: Flat (less spherical)

---

**SPHERICITY: IN A NUTSHELL**

- Compute sphericity index per participant
- Plot by Age





**SPHERICITY OLD & YOUNG**  
**( $P < .00001$ )**

---

**NOW WE DECIDED TO LOOK AT SEX!**

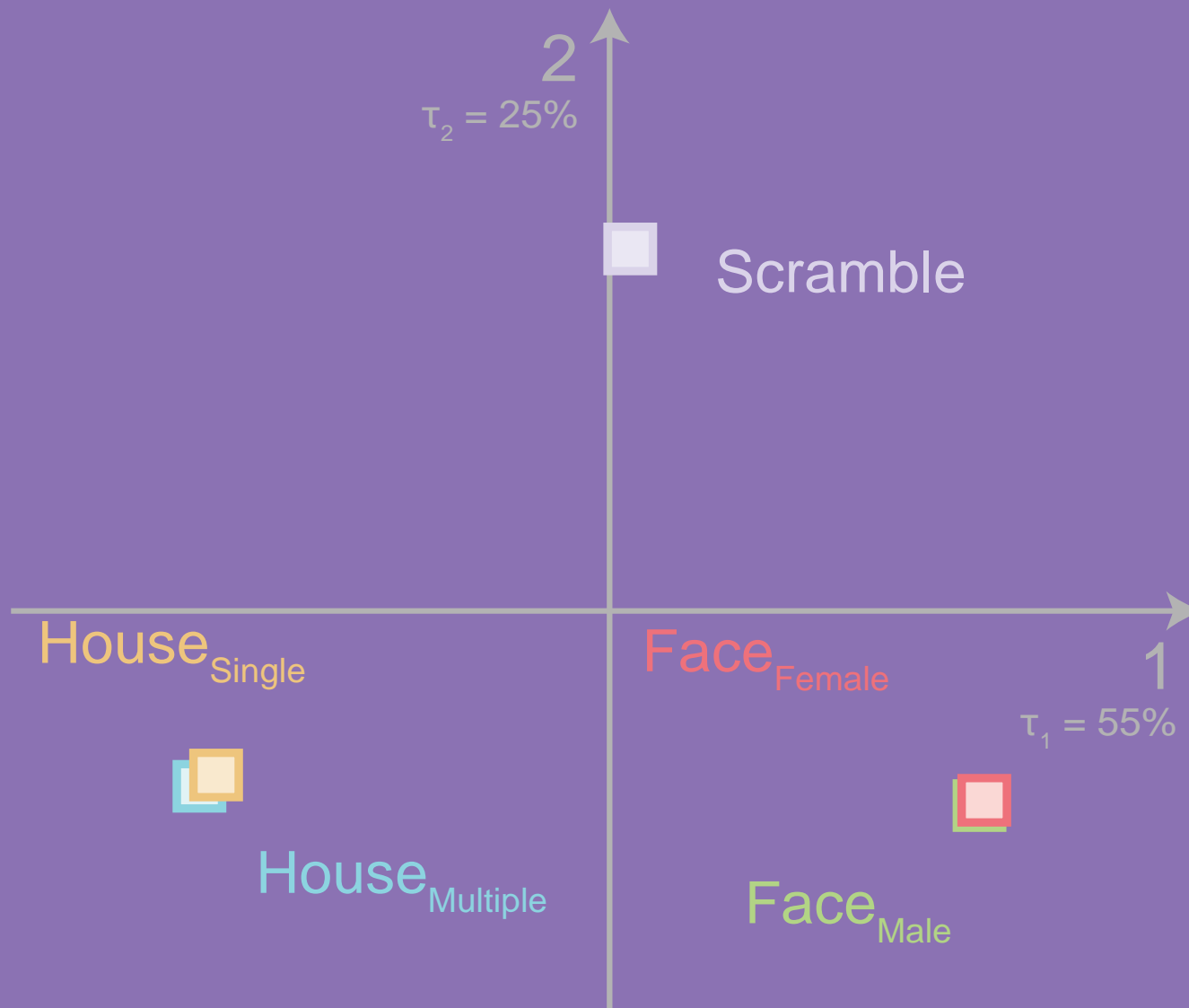
- Now you are paying attention!

---

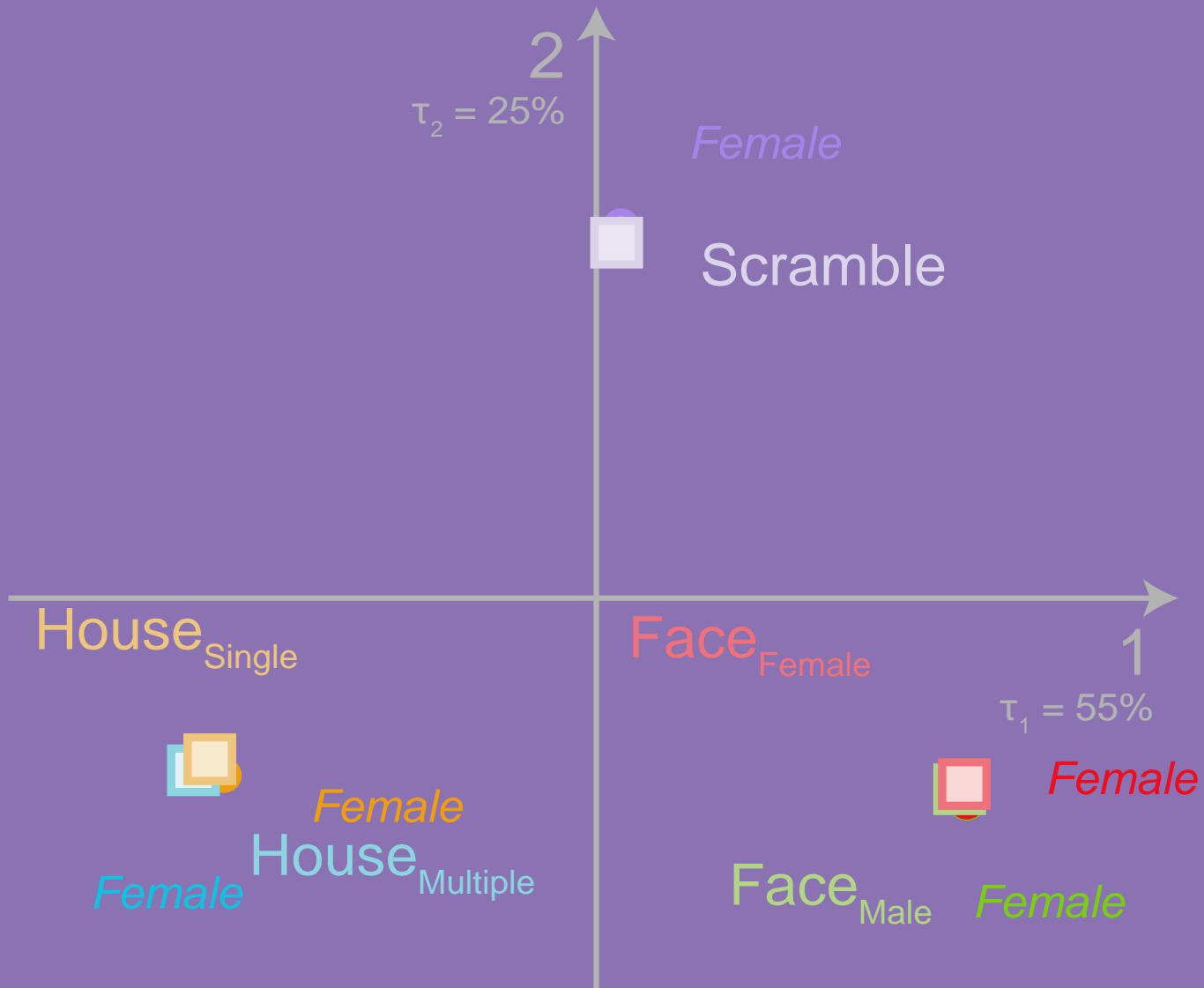
I MEAN *GENDER*

---

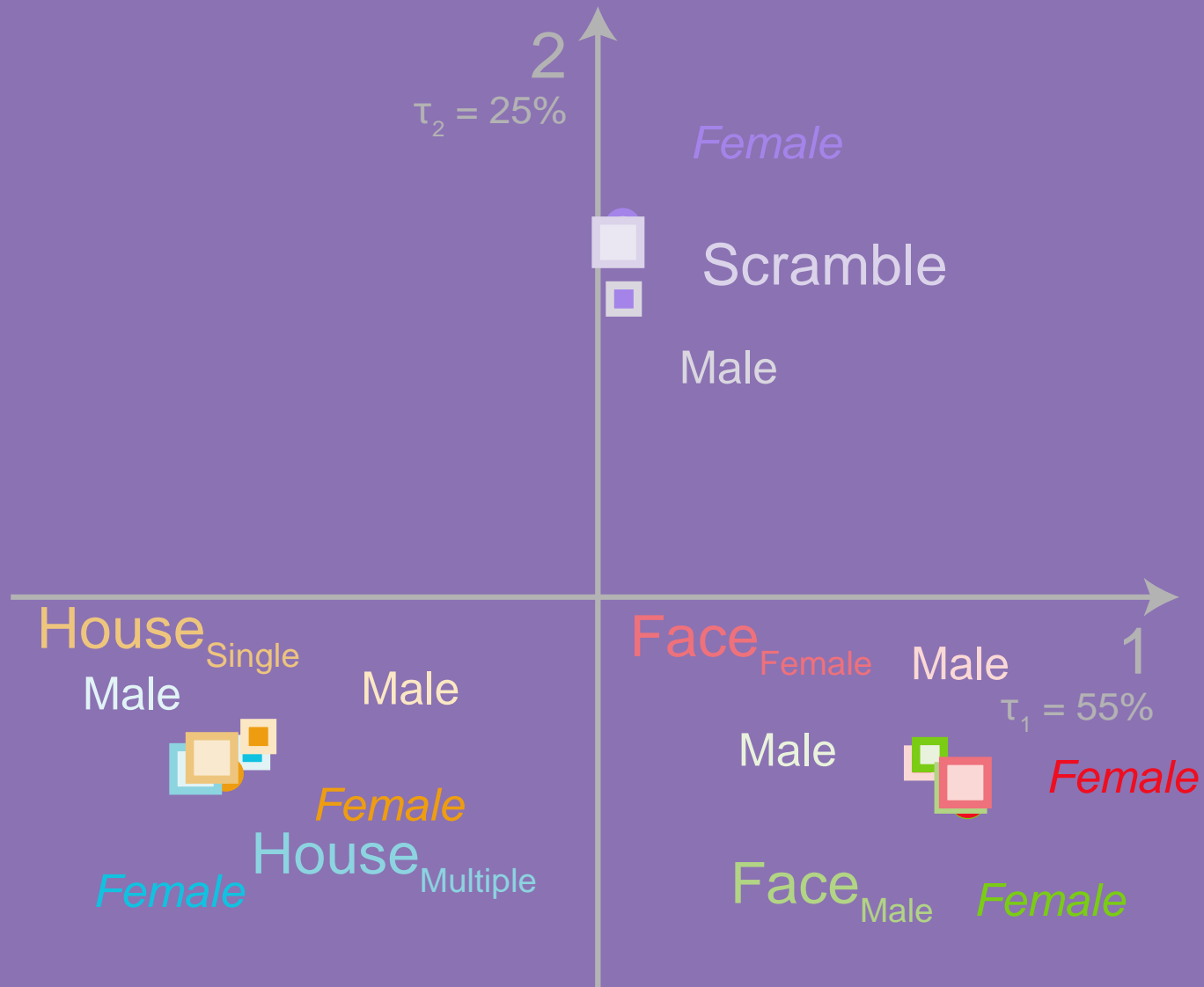
WHAT ABOUT GENDER?



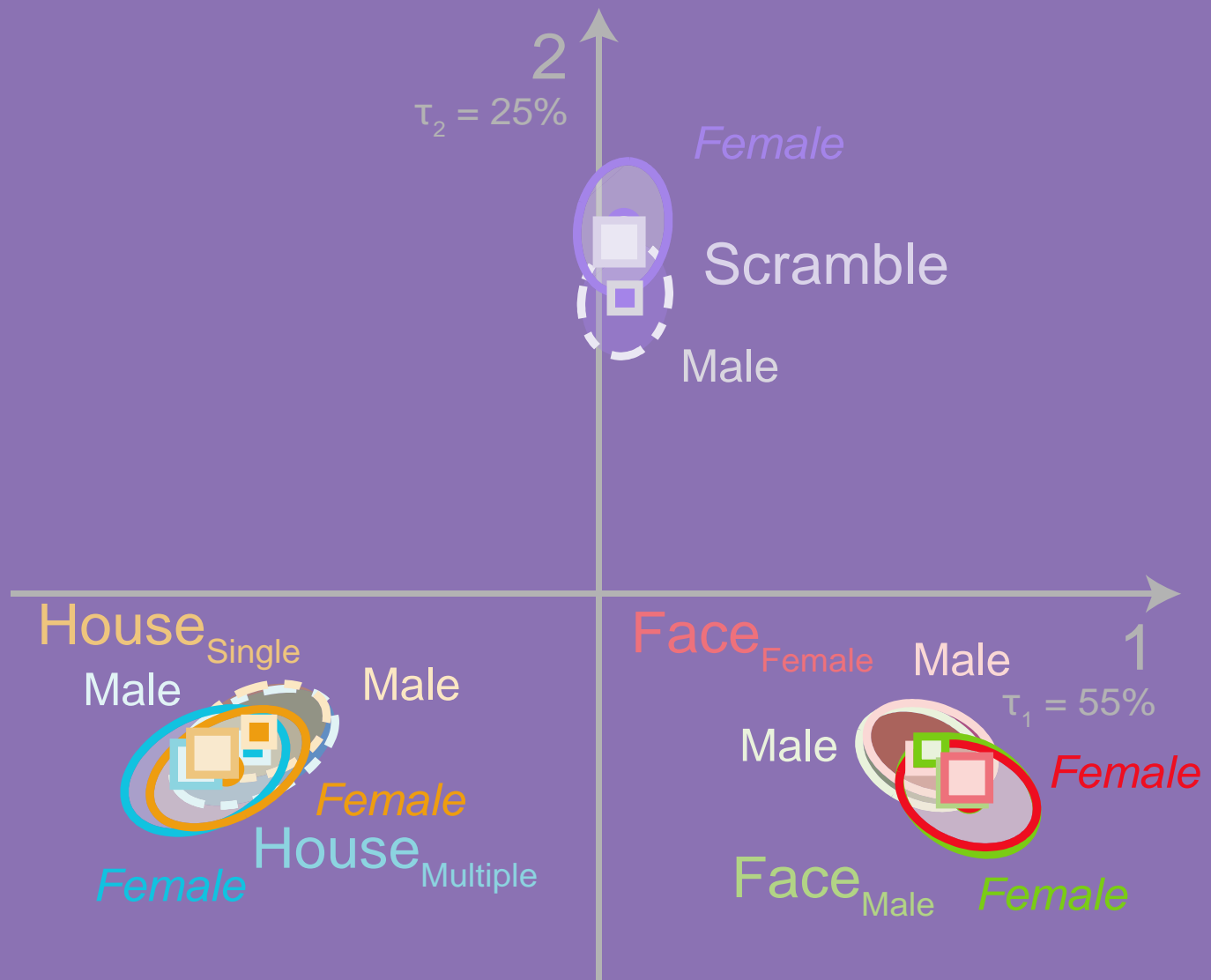
**GENDER EFFECTS?**



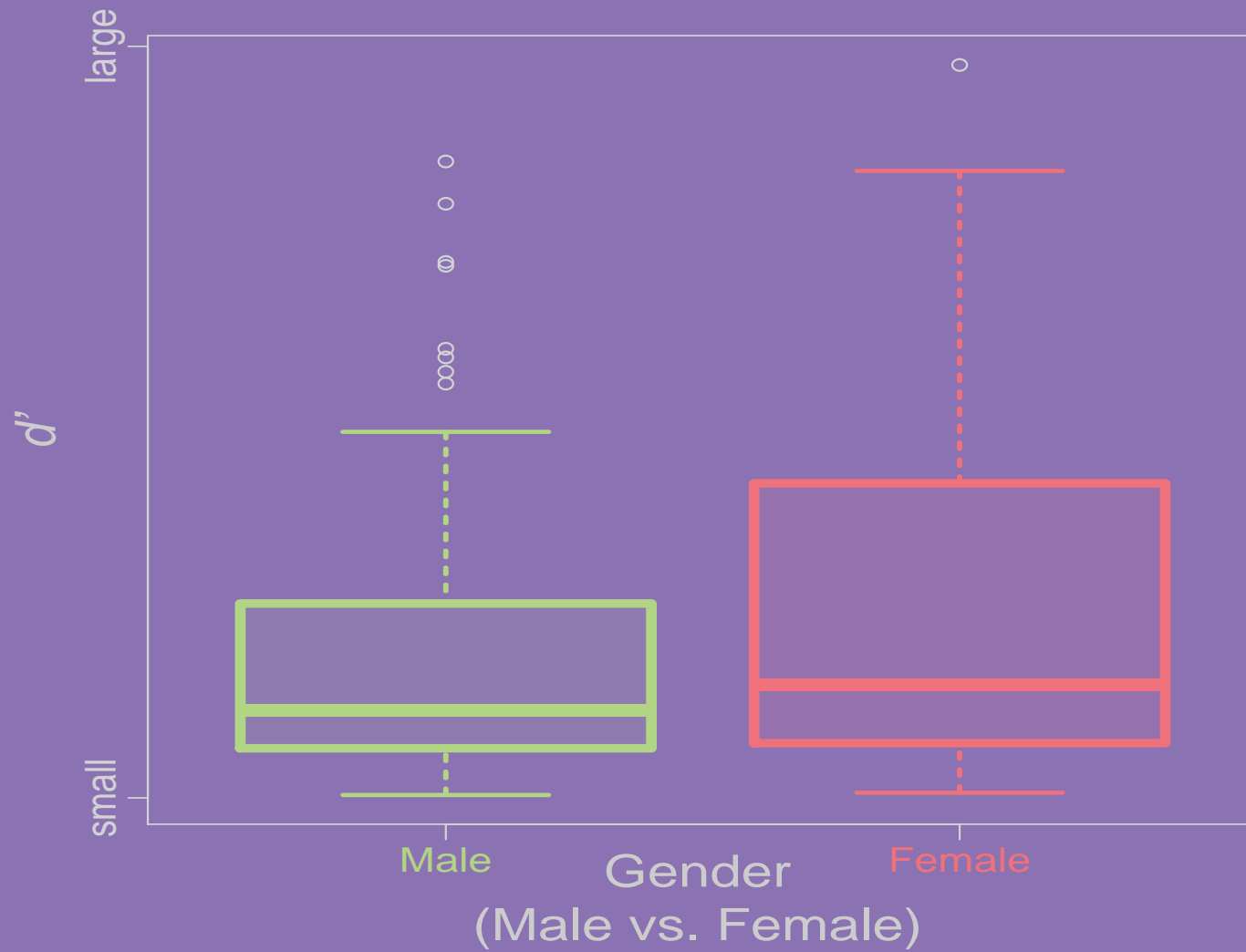
**GENDER EFFECTS: WOMEN.**



**GENDER EFFECTS: WOMEN & MEN.**



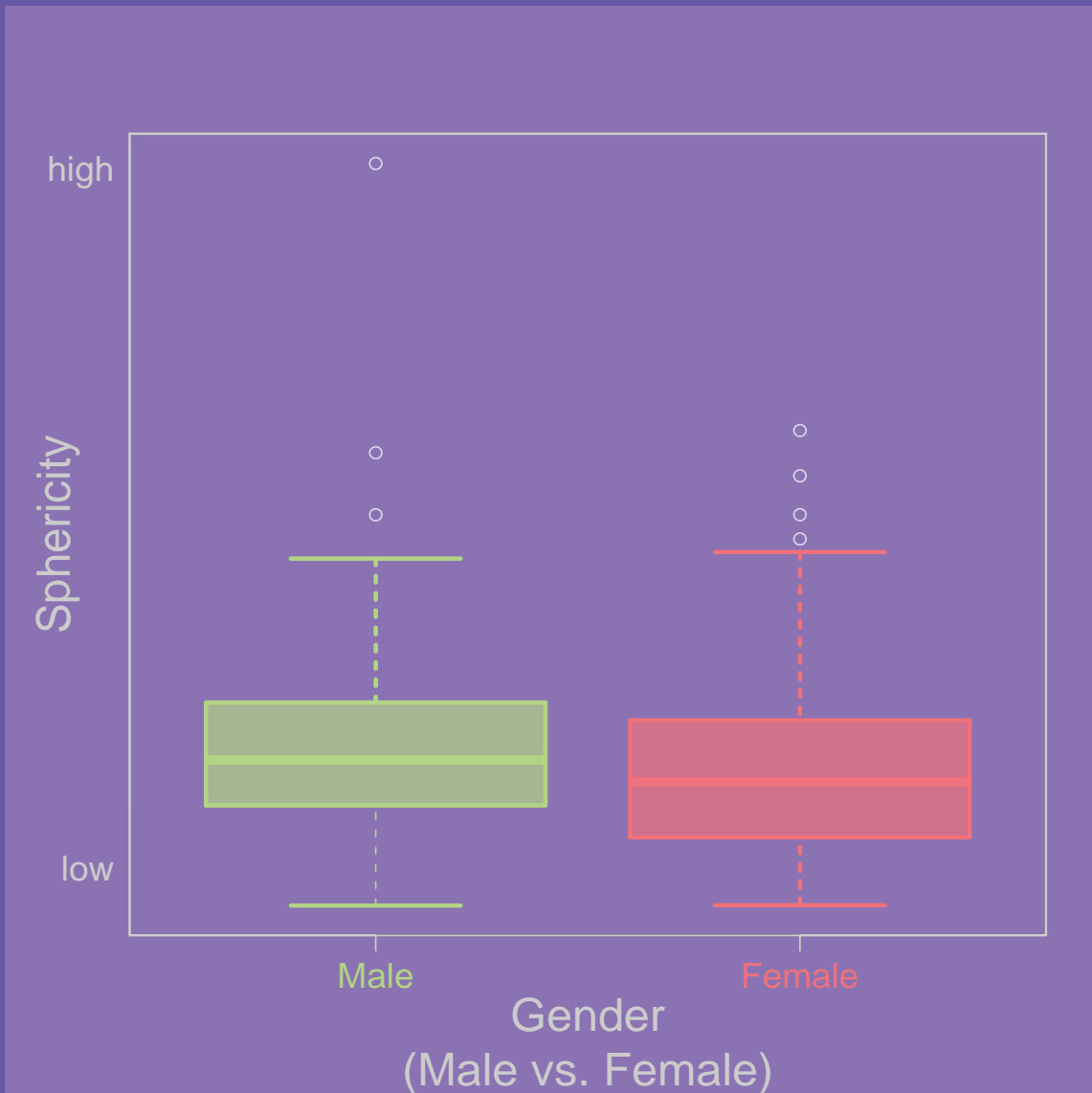
GENDER EFFECTS: NS.



## D' BY GENDER



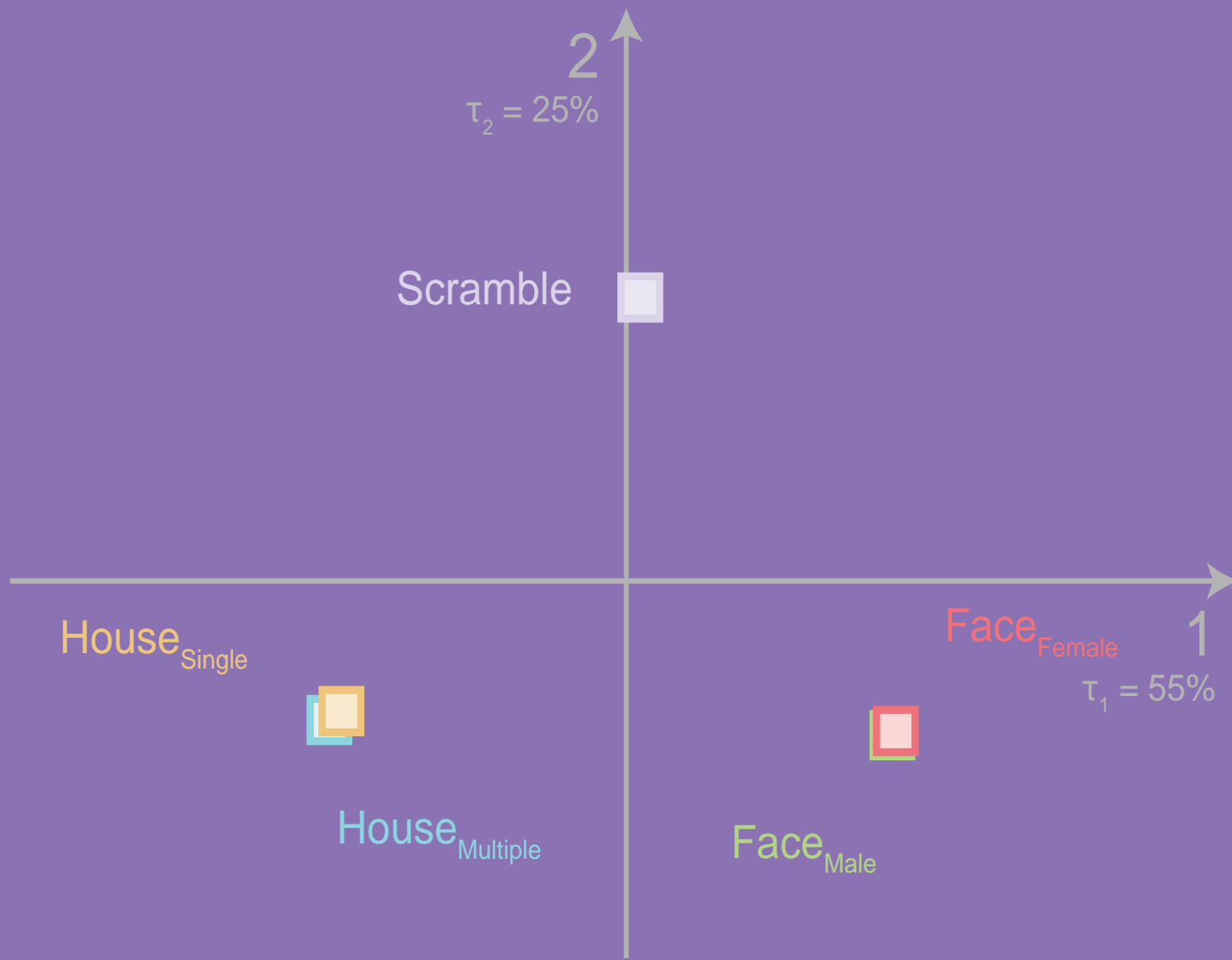
SPHERICITY



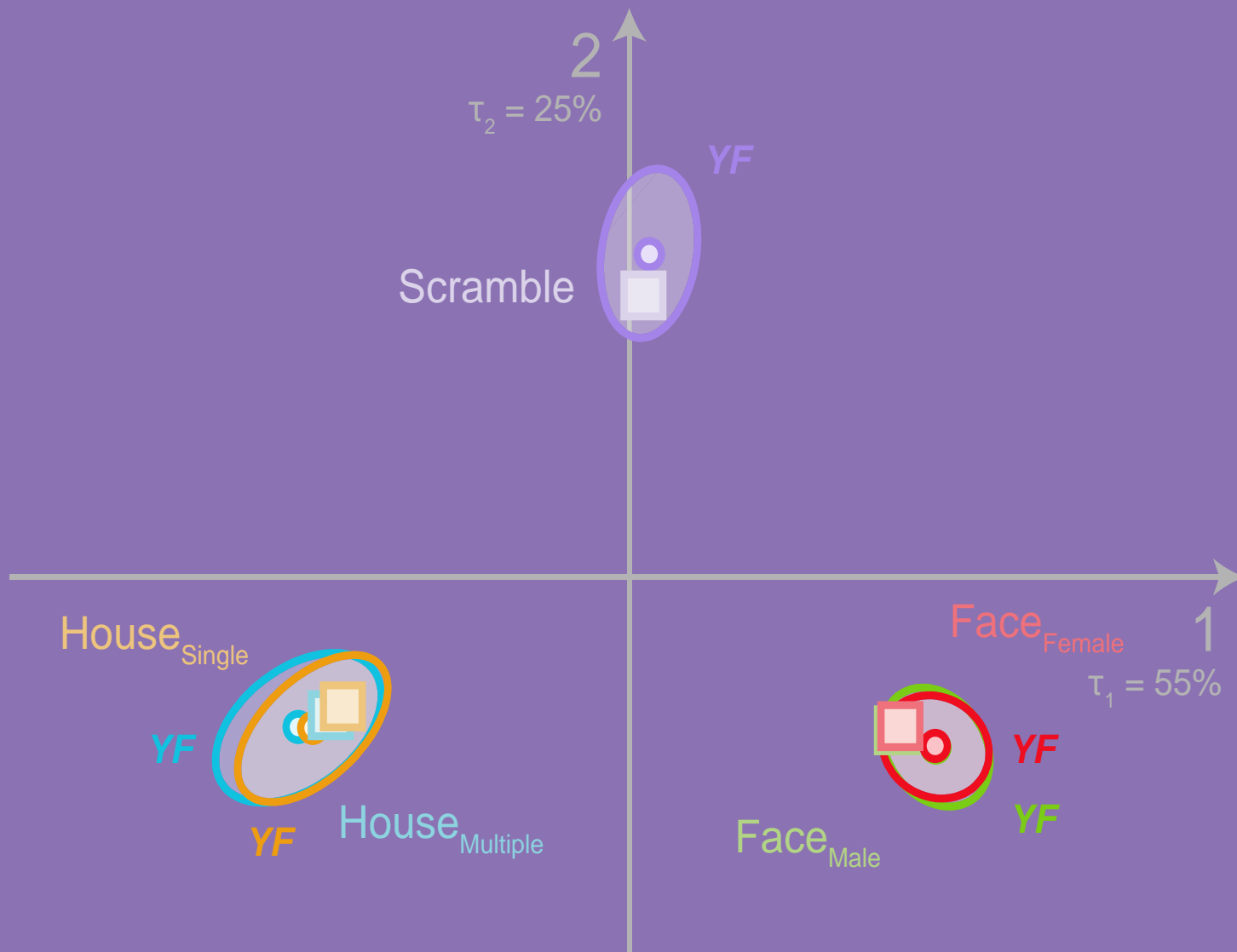
**SPHERICITY MEN & WOMEN**  
**( $P > .50$ )**

---

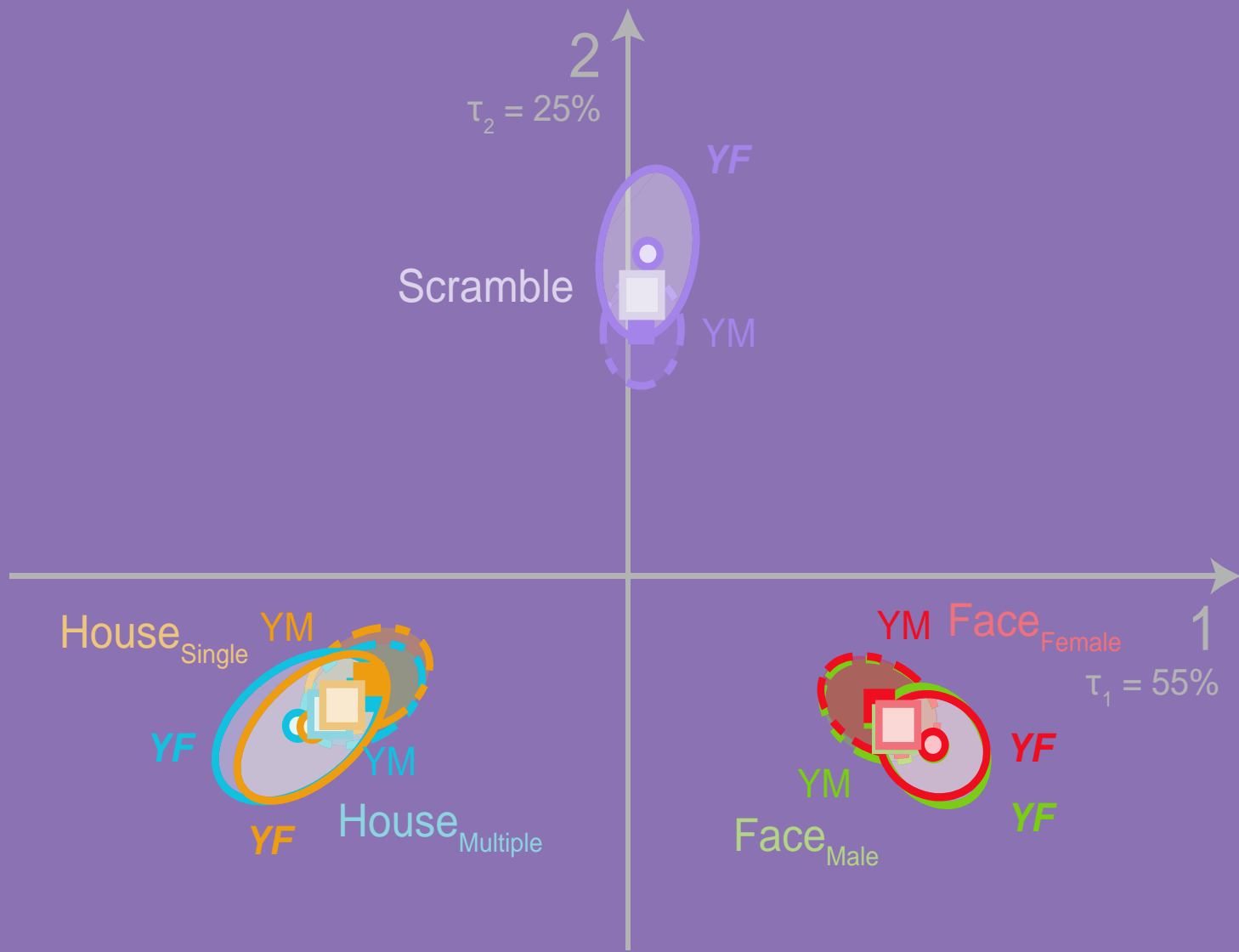
AGE & GENDER



## AGE & GENDER

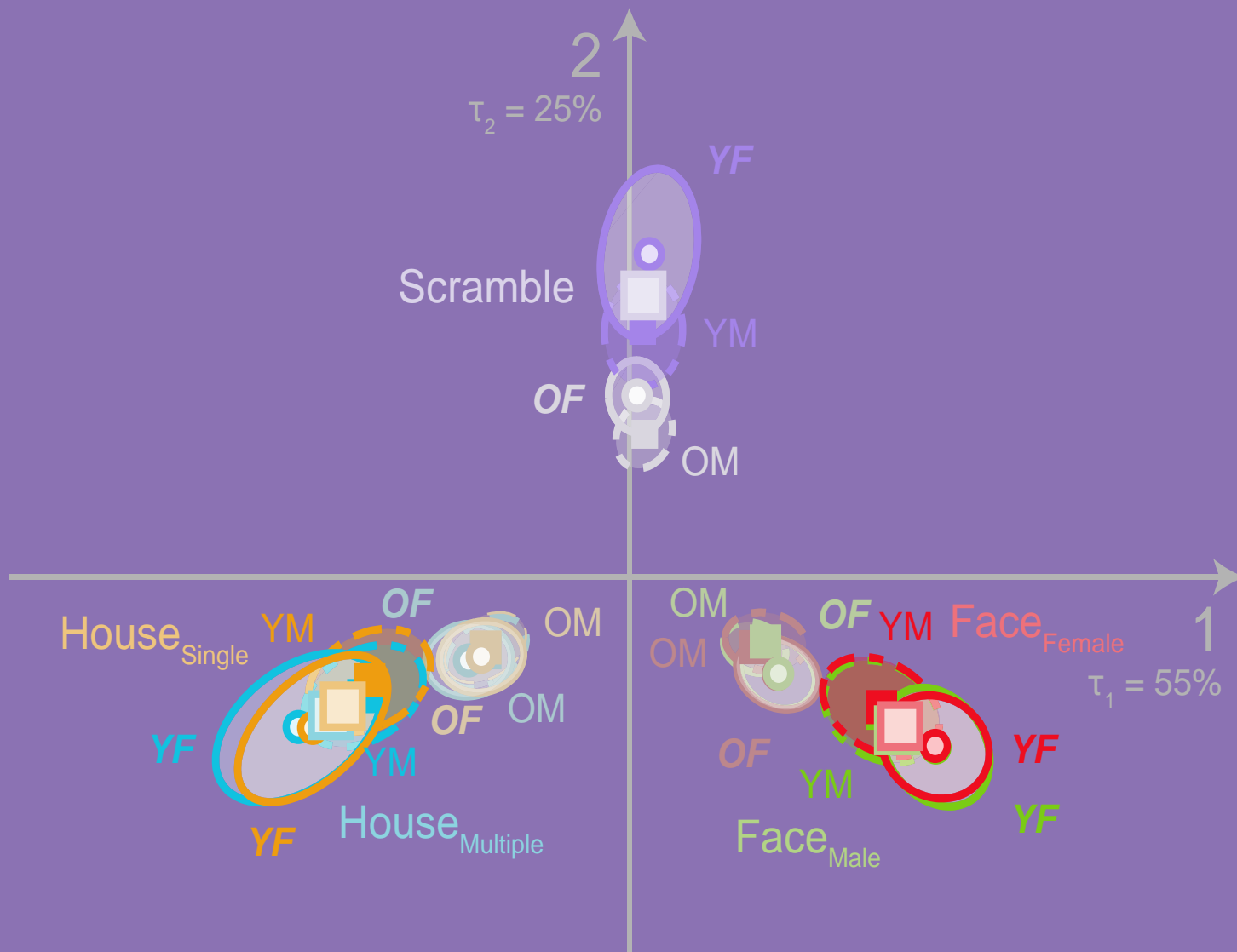


## AGE & GENDER

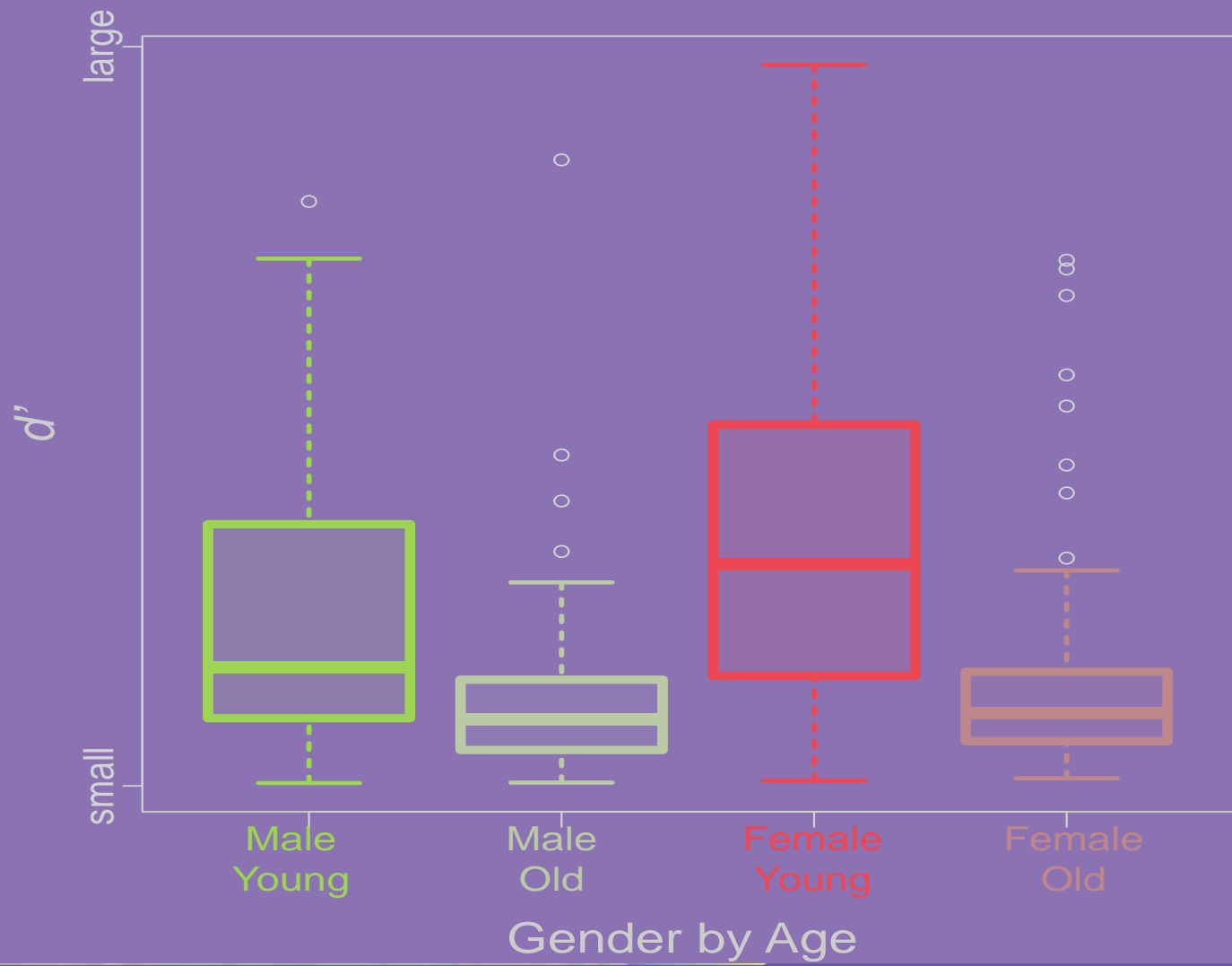


# AGE & GENDER



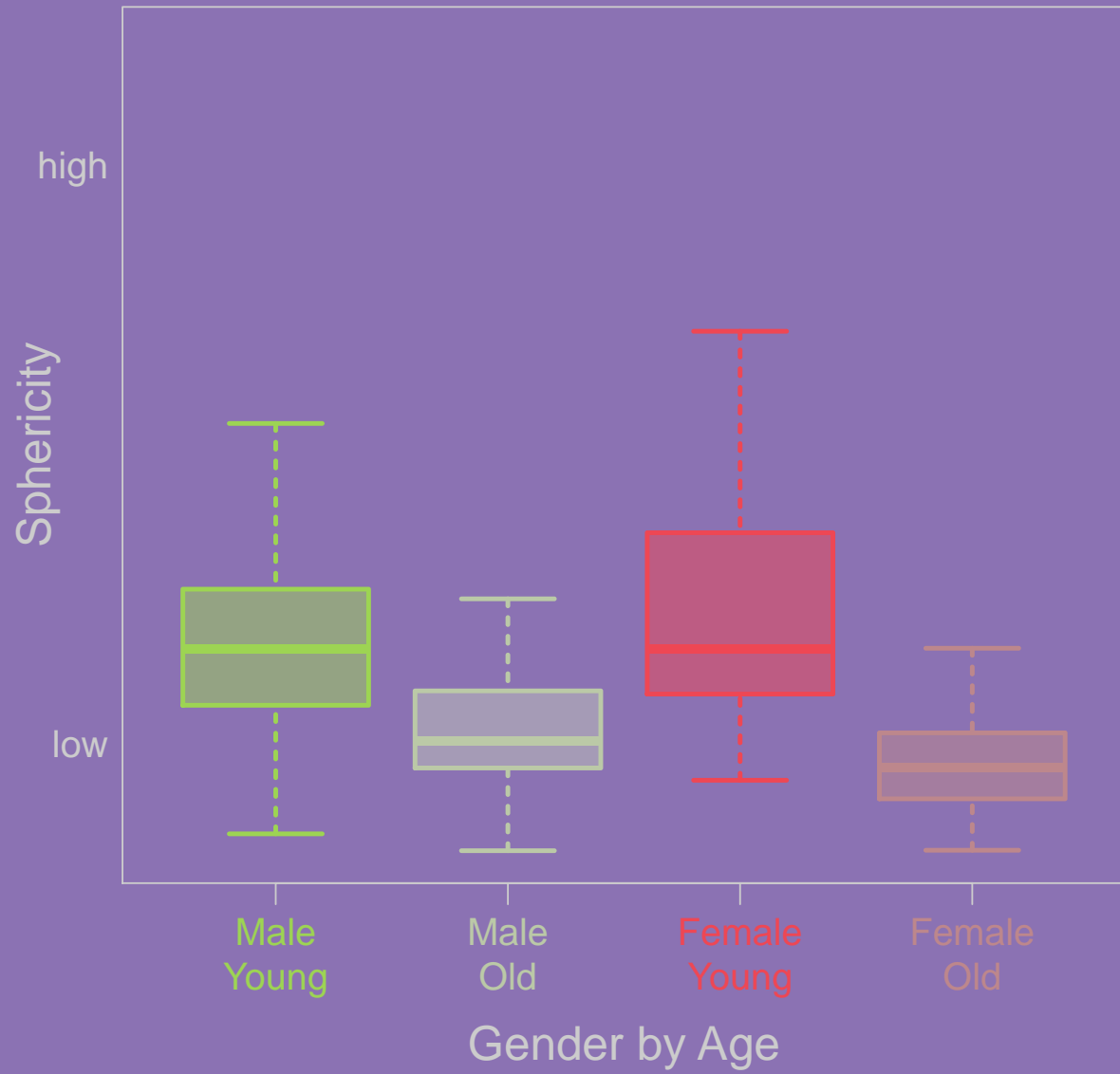


# AGE & GENDER



---

SPHERICITY



- Very clear effect of age
  - As predicted by dedifferentiation
  - Effect of age correlates with sphericity
  - Subtle effect of Gender
  - Stronger in young people
- For pattern classifiers: Power in numbers

---

**FINALE: VARIATION 3: FLATTER BRAINS**

## VARIATION 4: AGE AND CATEGORIES

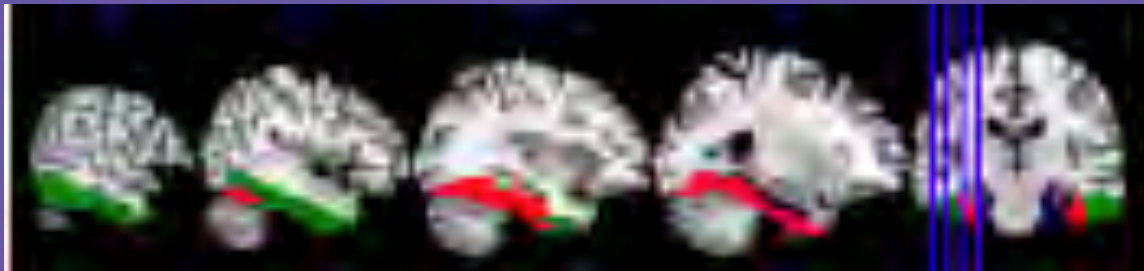
---

Do categories change with age?

SIX CATEGORIES. 64 IMAGES PER CATEGORY  
BLOCK DESIGN  
35 YOUNG & 35 OLD PARTICIPANTS

(RIECK, BEATON, ABDI, & PARK, *SFN*, 2011)

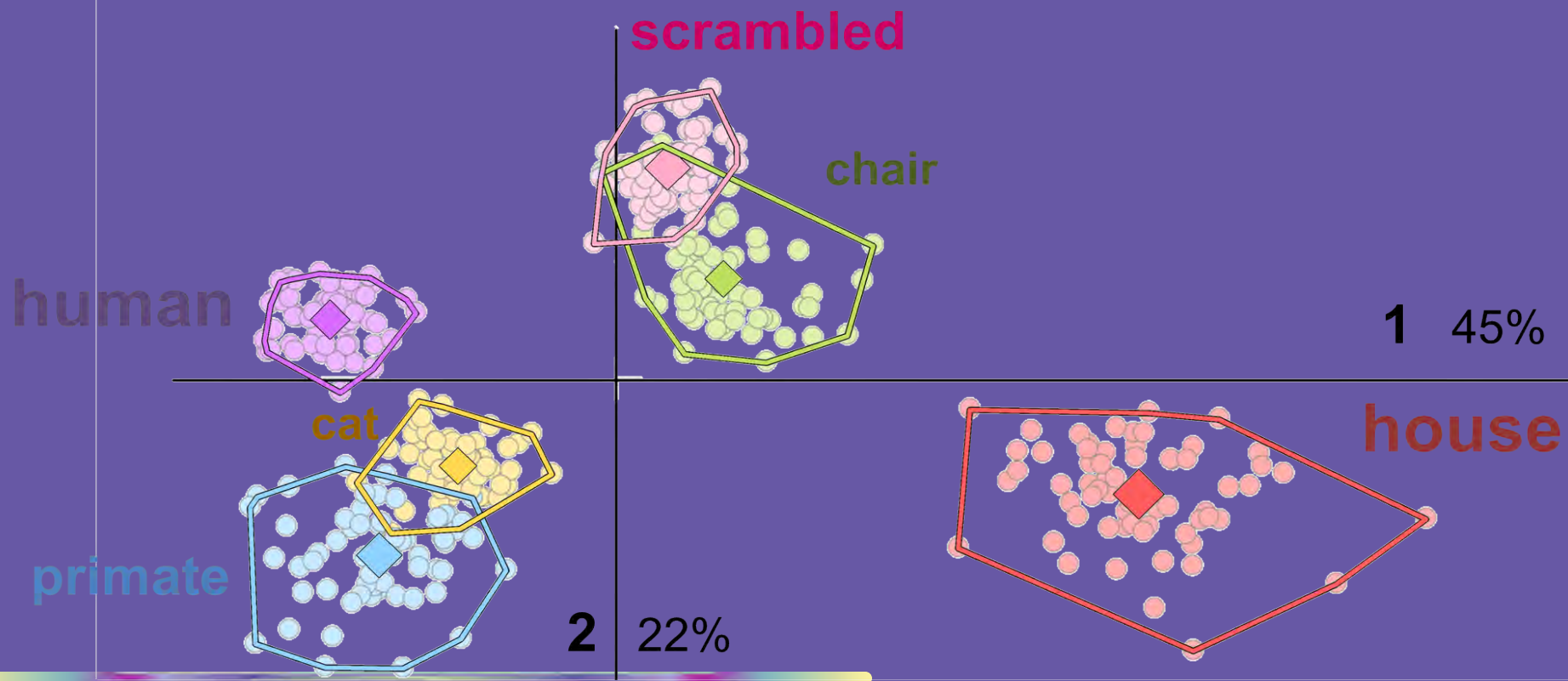




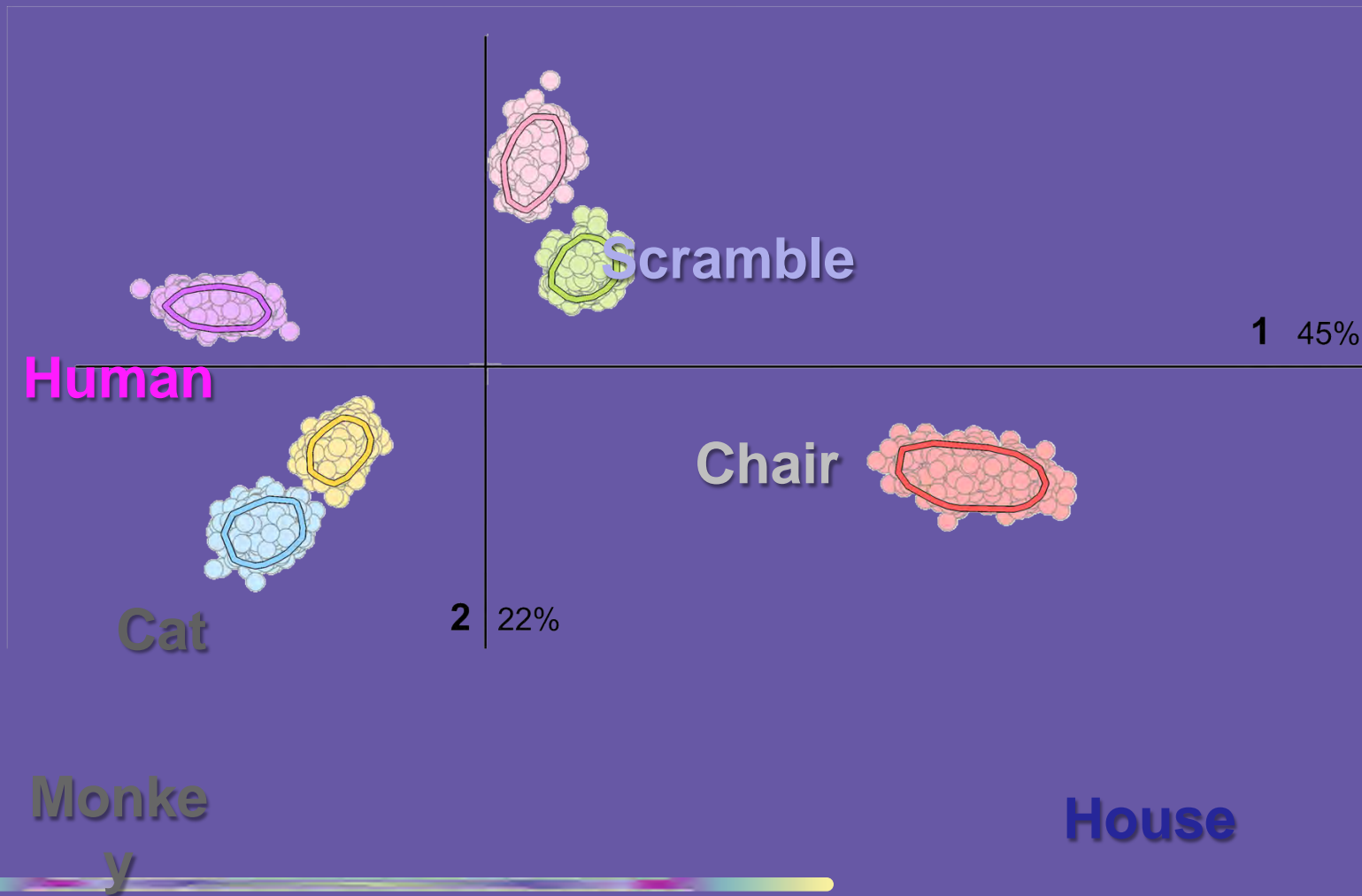
**AAL Mask Regions**  
Inferior Temporal Gyrus  
**Fusiform Gyrus**  
Parahippocampal Gyrus

---

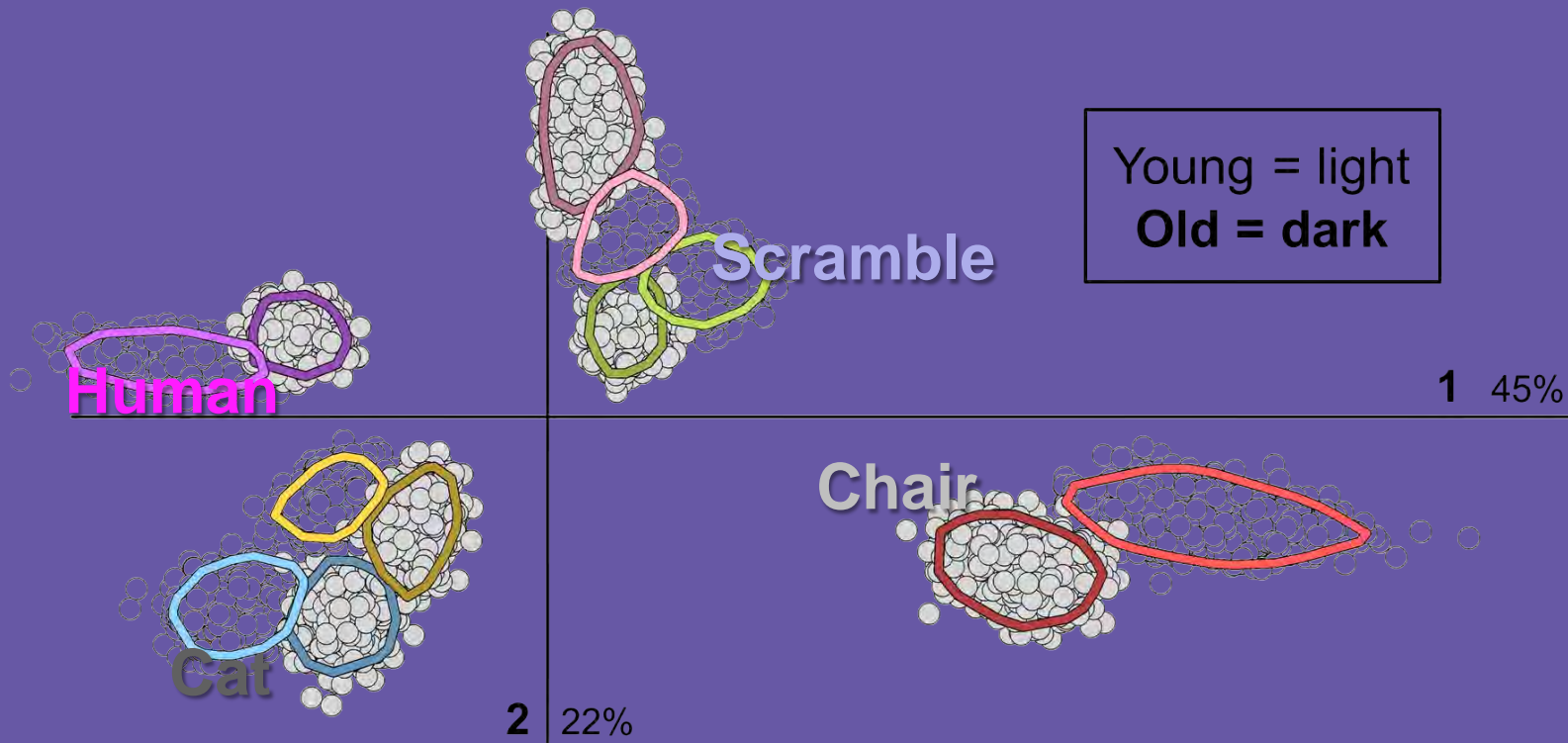
WHERE TO LOOK



TOLERANCE. DIMENSIONS 1 & 2 ALL



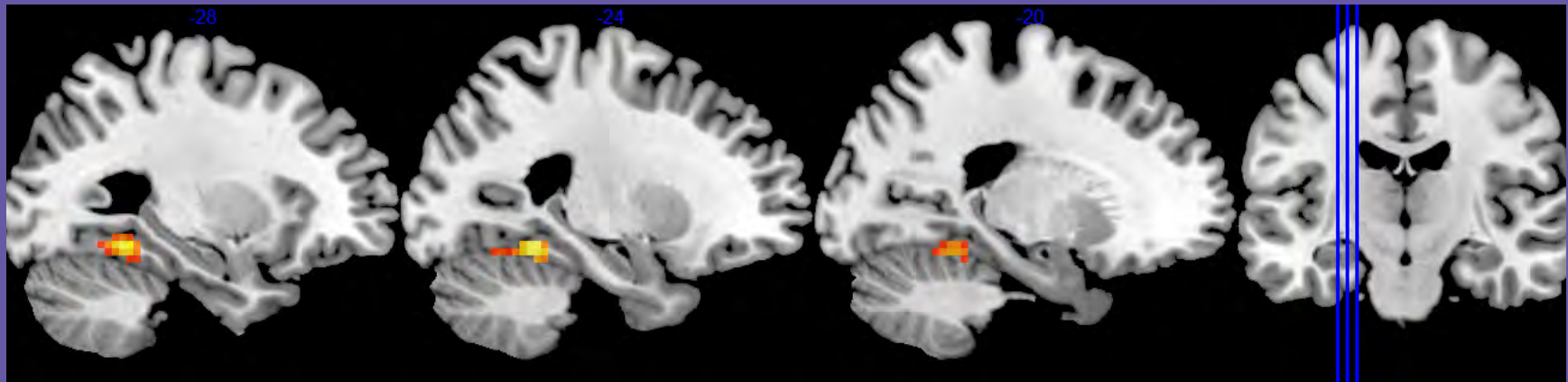
CONFIDENCE. DIMENSIONS 1 & 2 ALL



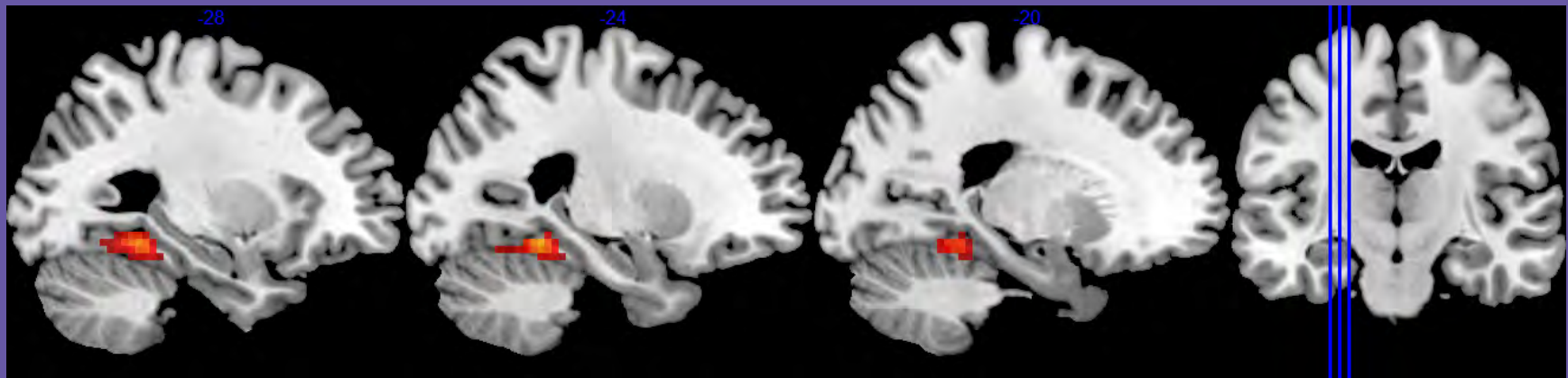
House

Monke  
y

# DIMENSIONS 1 & 2. BY AGE

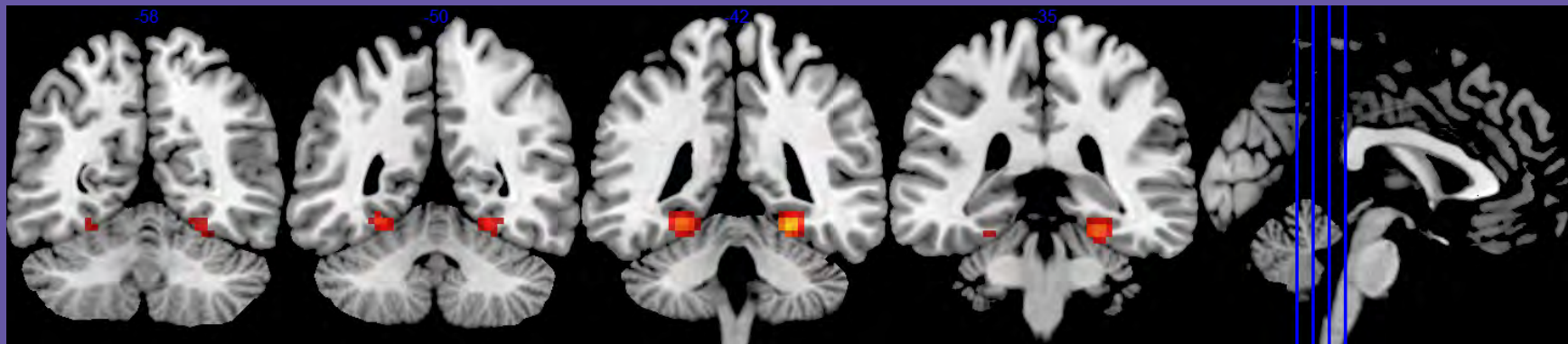
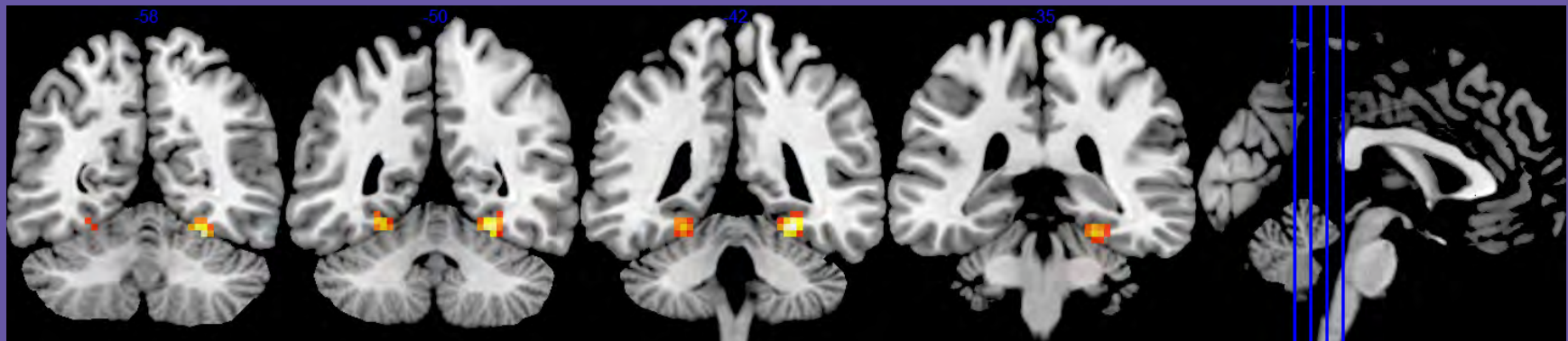


Young. Top Voxels # 153



Old. Top Voxels # 295

THE BRAIN. TOP CONTRIBUTIONS (15% VAR)  
LIGHTER IS MORE



---

**CORONAL. 15% VARIANCE.  
DE-DIFERRENCIATION**

---

TIME FOR A PAUSE